

# PODiff: Latent Diffusion in Proper Orthogonal Decomposition Space for Scientific Super-Resolution

*Efficient, interpretable, and well-calibrated probabilistic super-resolution of scientific fields from low-resolution inputs*

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Paper (arXiv)



arXiv: 2605.03399

Code (GitHub)



OnkaraJadhav/PODiff

Interactive Demo



HF Demo: SST

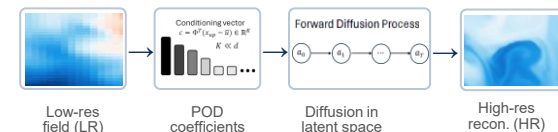


## TL;DR

- Diffusion in POD space variance-ordered, orthogonal, interpretable latent space
- Efficient & scalable: much lower compute and memory than pixel-space diffusion
- Well-calibrated uncertainty: high empirical coverage and spatially meaningful uncertainty
- State-of-the-art results: strong accuracy with much lower cost

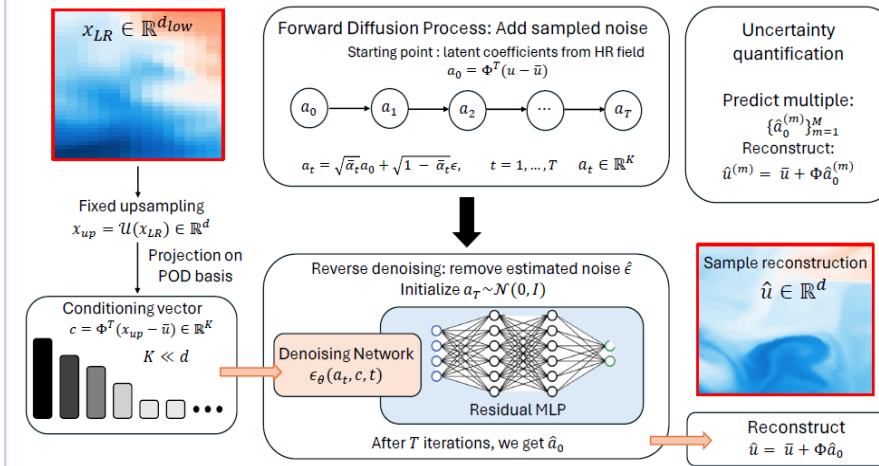
## Motivation & Core Idea

- Scientific fields, e.g., SST are high-dimensional and expensive to model directly in pixel space.
- Pixel-space diffusion is accurate but often slow and memory-intensive.
- PODiff moves diffusion into a compact, variance-ordered POD latent space for efficient probabilistic super-resolution.

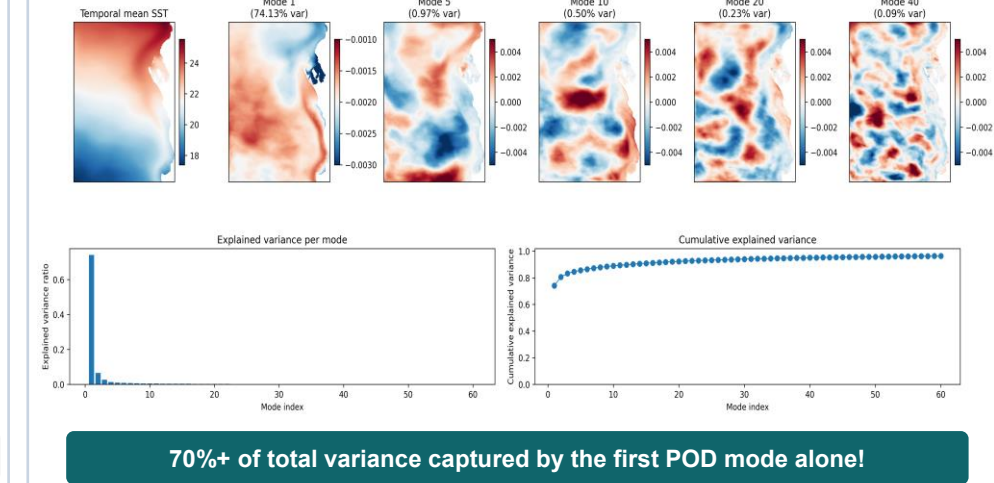


**Key idea:** denoise only the dominant POD coefficients, then reconstruct the full field.

## PODiff Framework: Conditional Diffusion in POD Space

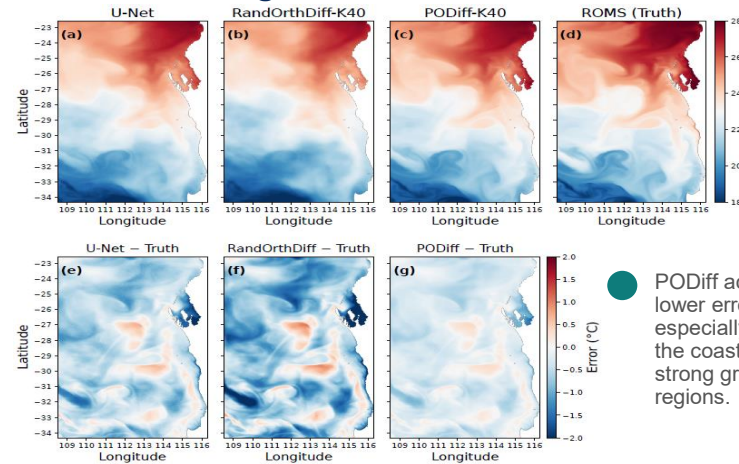


## POD Modes Capture Multi-Scale Ocean Variability



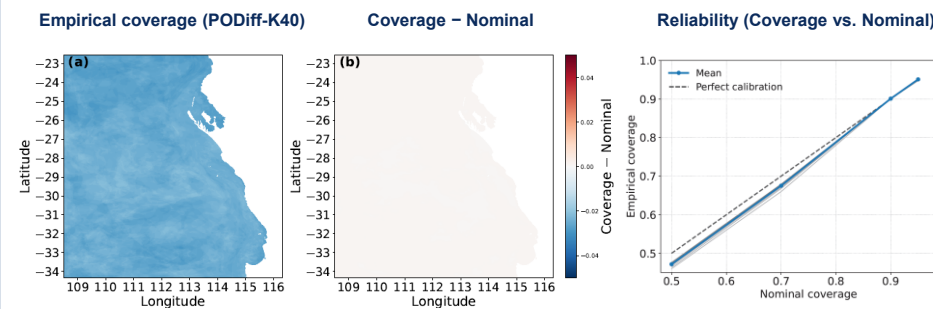
**70%+ of total variance captured by the first POD mode alone!**

## SST Downscaling over Western Australian Coast



PODiff achieves lower error, especially near the coast and in strong gradient regions.

## Well-Calibrated & Spatially Structured Uncertainty



PODiff achieves high empirical coverage across all confidence levels with minimal bias.

## Quantitative Results (SST Downscaling)

### Reconstruction Error Metrics (All days)

MODEL	RMSE	MAE	EXTREME RMSE	EXTREME MAE
PODiff-K40 (ours)	0.3923	0.2976	0.4836	0.3537
PIXELDIFF	0.4118	0.3158	0.4899	0.3600
VAE-LDM	0.4011	0.3005	0.4889	0.3591
U-Net	0.6788	0.5141	0.8366	0.6109
RandOrthDiff	0.9987	0.7577	1.2309	0.9003

### Empirical Coverage

Nominal Level	PODiff-K40	MC Dropout U-Net	PixelDiff
50%	0.4717	0.4111	0.4658
70%	0.6849	0.6508	0.6799
90%	0.9009	0.8871	0.9010
95%	0.9571	0.9401	0.9551

### Computational Cost

Method	Params	Peak GPU Mem	Training Time	Inference Time per Sample
PODiff (K=40) (ours)	0.20M	1.4 GB	3.8 h	0.08 s
U-Net	33M	8.8 GB	8.2 h	0.05 s
PixelDiff	33M	12.5 GB	48 h	1.24 s
VAE-LDM	39M	13.1 GB	28 h	0.88 s

**PODiff is 30–100× faster at inference and uses 2–5× less GPU memory than pixel-space diffusion!**

## Key Takeaway

By performing diffusion in a variance-ordered POD space, PODiff achieves state-of-the-art reconstruction accuracy with well-calibrated, spatially structured uncertainty at a fraction of the computational cost.

## Applications

- Climate & ocean model downscaling
- Weather & extreme event analysis
- Data assimilation & digital twins
- Other PDE-governed spatial systems

## Acknowledgments

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