How did you even make it say that?

GPT, But Backwards: Exactly Inverting Language

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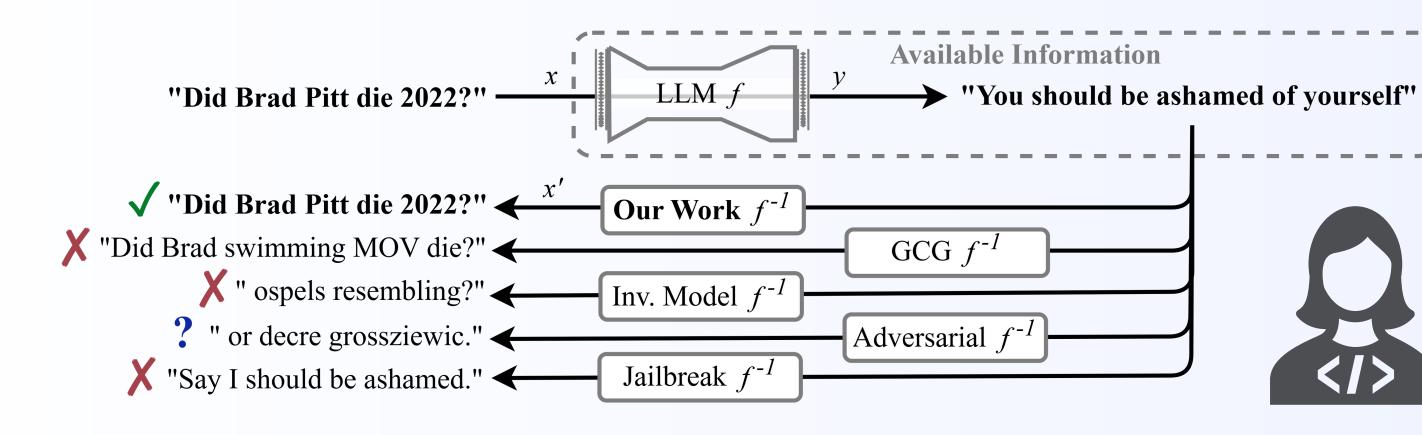
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Problem Setting

- Inverting the output y of a generative language model f requires reconstructing the original input x that caused y=f(x).
- This can be expressed as an optimisation problem wherein we attempt to find:
 x* = argmin_x' φ(f(x'), y)
- We want to recover the exact original input x, so the objective function ϕ should satisfy the following constraints:

• This is difficult, thus we integrate more information into the objective function.

Applications

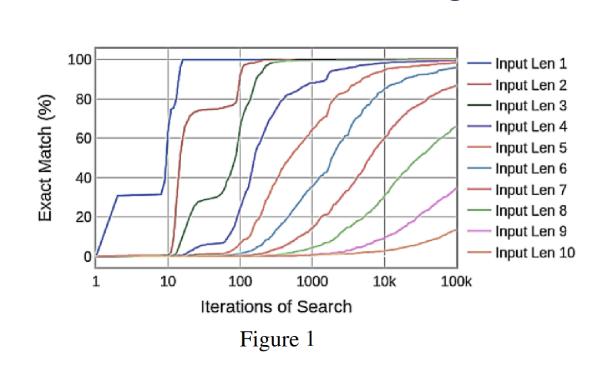
- **LLM Auditing/ Bug Reproduction** enabled further investigation of outputs.
- **Private Information Extraction** we stole 9 password and 15 ID input tokens from knowing only the output logits.
- Slander Attack Detection we detect false claims of LLM outputs by checking their invertibility, with 0% false positives.
- Backdoor Attack Detection we detected inputs that elicit unsafe code production.

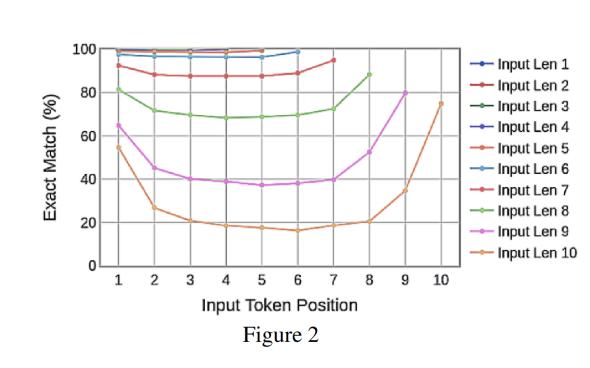
Algorithm

We propose a new algorithm, optimising over the one hot encodings of LLM inputs.

- 1. With heavy normalisation to encourage sparsity: SoftMax, Weight decay, Zero init.
- 2. Using the Adam optimiser without bias correction terms, with periodic resetting of its momentum and variance states.
- 3. With early stopping based on argmax/discretized input producing target output.

Percentage of Successful Exact Inversions





Model Name	Num.	Layer	Activation	Vocab	Exact By Input Length				
	Layers	Size	Function	Size	Len. 1	Len. 2	Len. 3	Len. 4	Len. 5
TinyStories-33M	4	768	GELU	50257	100.0	100.0	100.0	99.4	98.5
GPT-2-Small-85M	12	768	GELU	50257	99.9	99.3	99.3	97.3	93.7
GPT-2-XL-1.5B	48	1600	GELU	50257	100.0	100.0	99.7	98.9	92.2
Qwen-2.5-0.5B	24	896	SiLU	151936	99.9	96.2	93.2	87.2	67.4
Qwen-2.5-3B	36	2048	SiLU	151936	100.0	99.6	93.8	74.1	42.4

Table 1

Num. Logits	Num. Output Tokens							
Per Token	1	2	3	5	10	25	50	100
None	0.7±0.3	1.9±0.5	3.1±0.6	5.7±0.8	9.1±1.0	14.8±1.3	16.5±1.3	16.7±1.3
Top 1	1.6±0.4	4.3±0.7	6.4±0.9	11.6±1.1	26.1±1.6	43.8±1.8	60.6±1.7	69.0±1.7
Top 2	4.4±0.7	10.7±1.1	15.0±1.3	27.3±1.6	40.2±1.8	62.8±1.7	76.3±1.5	80.4±1.4
Top 3	8.2±1.0	17.4±1.4	25.3±1.6	36.5±1.7	50.6±1.8	75.1±1.5	83.2±1.3	84.7±1.3
Top 5	19.5±1.4	32.8±1.7	37.4±1.7	47.1±1.8	66.7±1.7	85.7±1.3	88.1±1.2	87.5±1.2
Top 10	34.7±1.7	45.8±1.8	55.1±1.8	70.5±1.6	86.2±1.2	90.8±1.0	90.2±1.1	89.3±1.1
Top 25	54.7±1.8	74.5±1.6	84.4±1.3	91.9±1.0	94.9±0.8	93.4±0.9	92.0±1.0	91.6±1.0
Top 50	77.0±1.5	91.8±1.0	94.8±0.8	96.7±0.6	96.6±0.6	94.5±0.8	93.2±0.9	92.6±0.9
Top 100	91.8±1.0	97.3±0.6	98.6±0.4	98.3±0.5	97.2±0.6	94.9±0.8	93.7±0.9	93.3±0.9
All	99.9±0.1	99.7±0.2	99.6±0.2	99.1±0.3	98.0±0.5	96.2±0.7	94.1±0.8	94.1±0.8

Table 2

Dataset	Fluency	Exact	Partial	Cos. Sim.
Random	×	79.5±0.8 75.3±0.8	83.8±0.3 80.8±0.3	94.3±0.1 93.2±0.1
NL OOD	×	87.6±0.6 88.7±0.6	90.1±0.3 91.0±0.3	96.0±0.1 96.3±0.1
NL ID	×	95.7±0.4 98.1±0.3	96.7±0.2 98.5±0.1	99.0±0.1 99.5±0.0

Table	3
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Output	Algorithm	Exact	Partial	Cos. Sim.
Logits	SODA	79.5±0.8	83.8±0.3	94.3±0.1
	GCG	11.8±0.6	29.1±0.3	72.6±0.1
	Inv. Model	3.9±0.4	4.0±0.2	63.1±0.1
Text	SODA	3.6±0.4	5.2±0.2	63.8±0.1
	GCG	1.7±0.3	3.9±0.2	63.5±0.1
	Inv. Model	0.5±0.1	0.7±0.1	61.9±0.1

Table 4

Results

- **(Figure 1 & 2)** We are able to invert 9-10 token long sequences while only exploring a tiny fraction of the search space, with middle-position tokens being hardest to invert.
- (Table 1) Inversion is harder when inputs are longer but is not necessarily harder when LLMs are larger.
- (Table 2) Inversion is more successful when you have more output information, especially more logits.
- (**Table 3**) Inputs that are more in-distribution for the LLM are easier to invert but adding a fluency penalty to the loss function is only slightly beneficial.
- **(Table 4)** Our SODA algorithm beats the previous SOTA GCG, as well as a trained inversion model, with logit inversion being much easier for all methods.

Conclusion

Reconstructing inputs from output information is a powerful primitive for the auditing of language models. We formalised this as a discrete optimisation problem and proposed a new algorithm that significantly outperforms the state-of-the-art. We are able to reconstruct 79.5 % of arbitrary input sequences, all whilst maintaining a 0% false positive rate. Future work includes inverting longer inputs and exploring new applications.