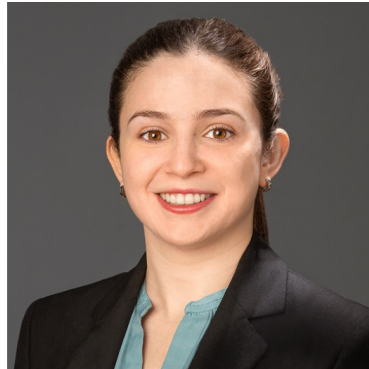


# Confounder-Free Continual Learning via Recursive Feature Normalization



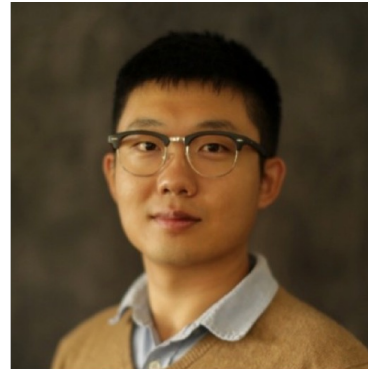
Yash Shah<sup>1</sup>



Camila Gonzalez<sup>1</sup>



Mohammad H. Abbasi<sup>1</sup>



Qingyu Zhao<sup>2</sup>



Kilian M. Pohl<sup>1</sup>



Ehsan Adeli<sup>1</sup>

<sup>1</sup>Stanford University  
<sup>2</sup>Weill Cornell Medicine

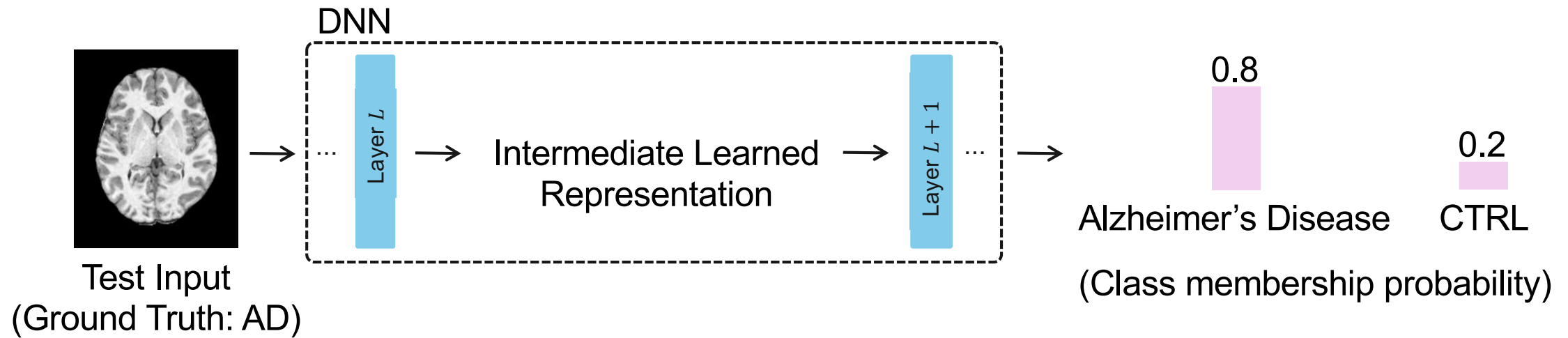


**Stanford**  
**Translational**  
**AI (STAI) Lab**  
in medicine and mental health

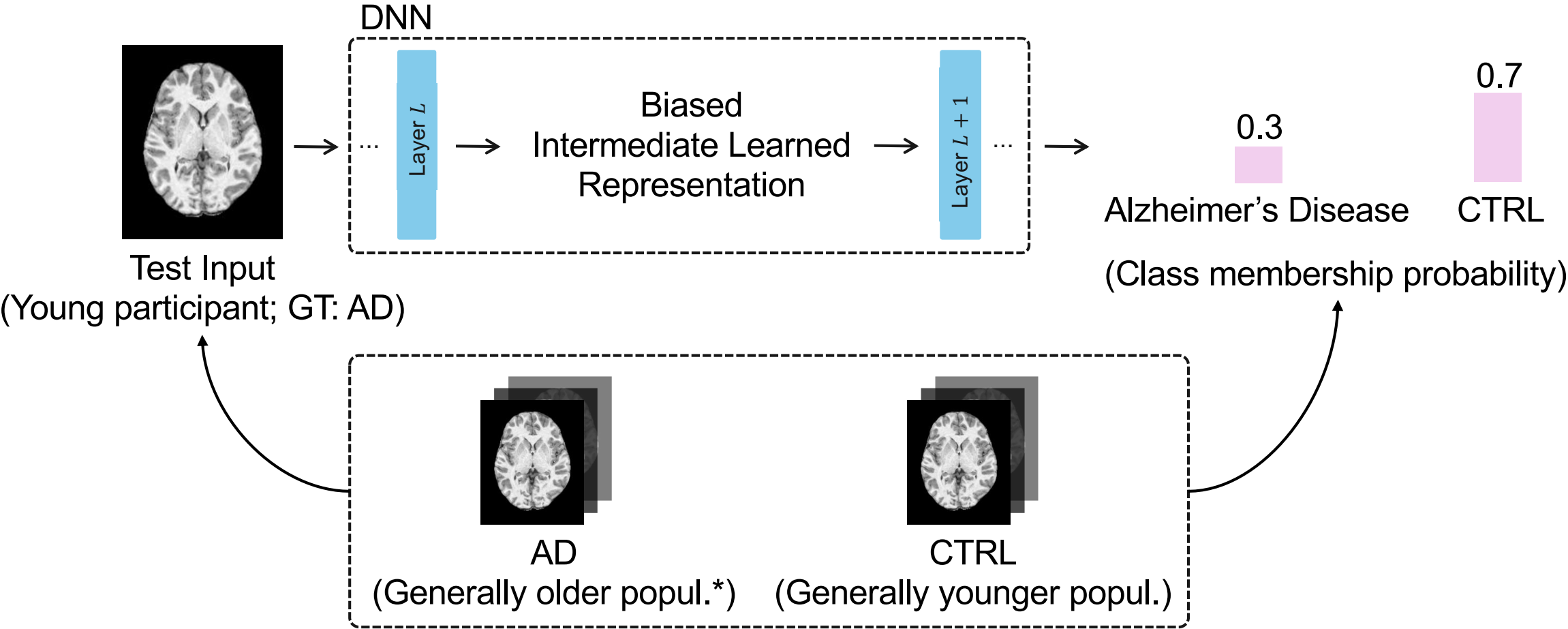


**Weill Cornell**  
**Medicine**

# Confounders

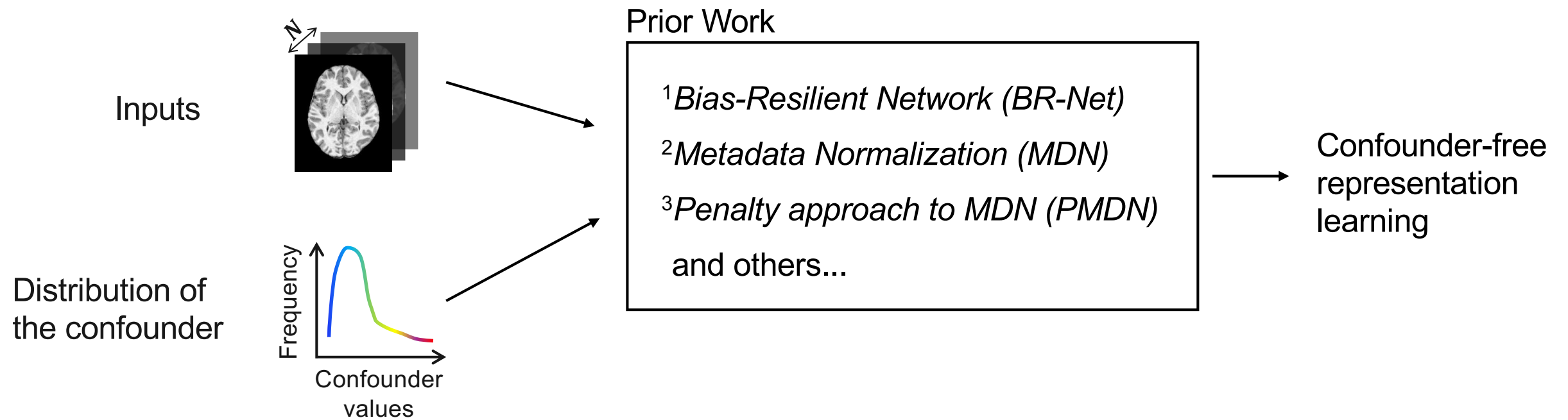


# Confounders



\*Rajan et al. *Population estimate of people with clinical Alzheimer's disease and mild cognitive impairment in the United States (2020-2060)*. In *Alzheimers Dement*, 2021.

# Static Learning



<sup>1</sup>Adeli et al. *Bias-Resilient Neural Network*. Preprint, 2020.

<sup>2</sup>Lu et al. *Metadata Normalization*. In CVPR, 2021.

<sup>3</sup>Vento et al. *A penalty approach for normalizing feature distributions to build confounder-free models*. In MICCAI 2022, vol. 13433 of Lecture Notes in Computer Science.

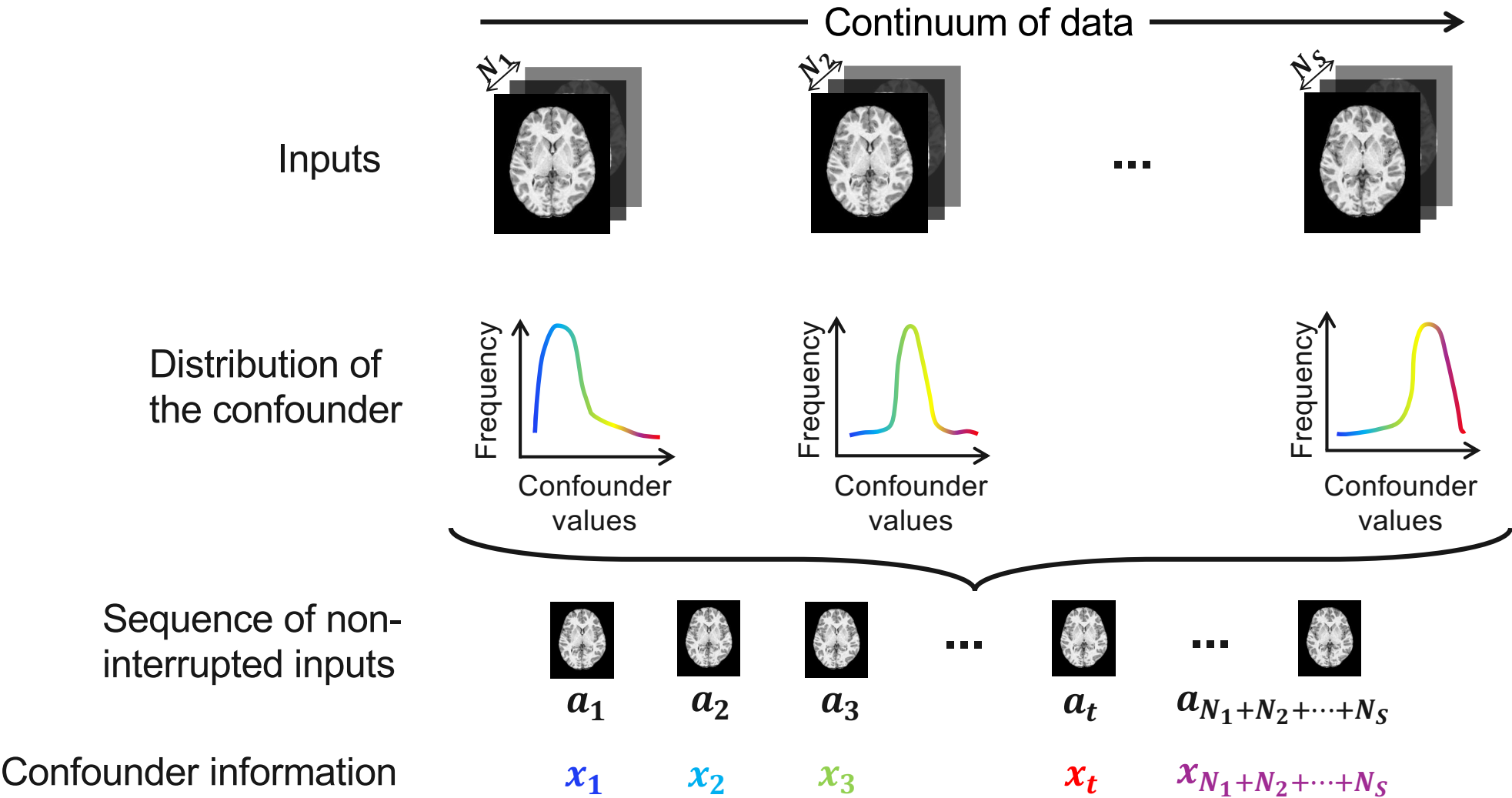
# Parameter Updates for MDN\*

Say we have  $N$  training examples.  $X$  is the confounder matrix, and  $z$  is the vector of intermediate learned feature representation of the model.

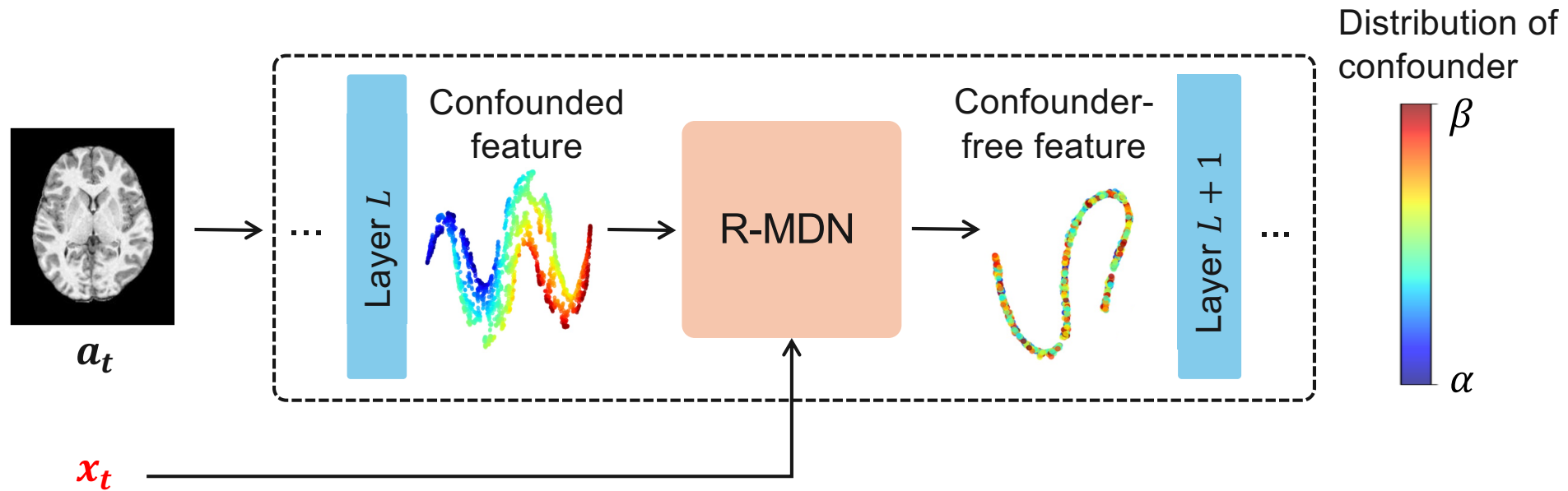
Ordinary Least Squares: 
$$\beta = \left( \sum_{i=1}^N X_i X_i^T \right)^{-1} \left( \sum_{i=1}^N z_i X_i \right)$$

\*Lu et al. *Metadata Normalization*. In CVPR, 2021.

# Continual Learning



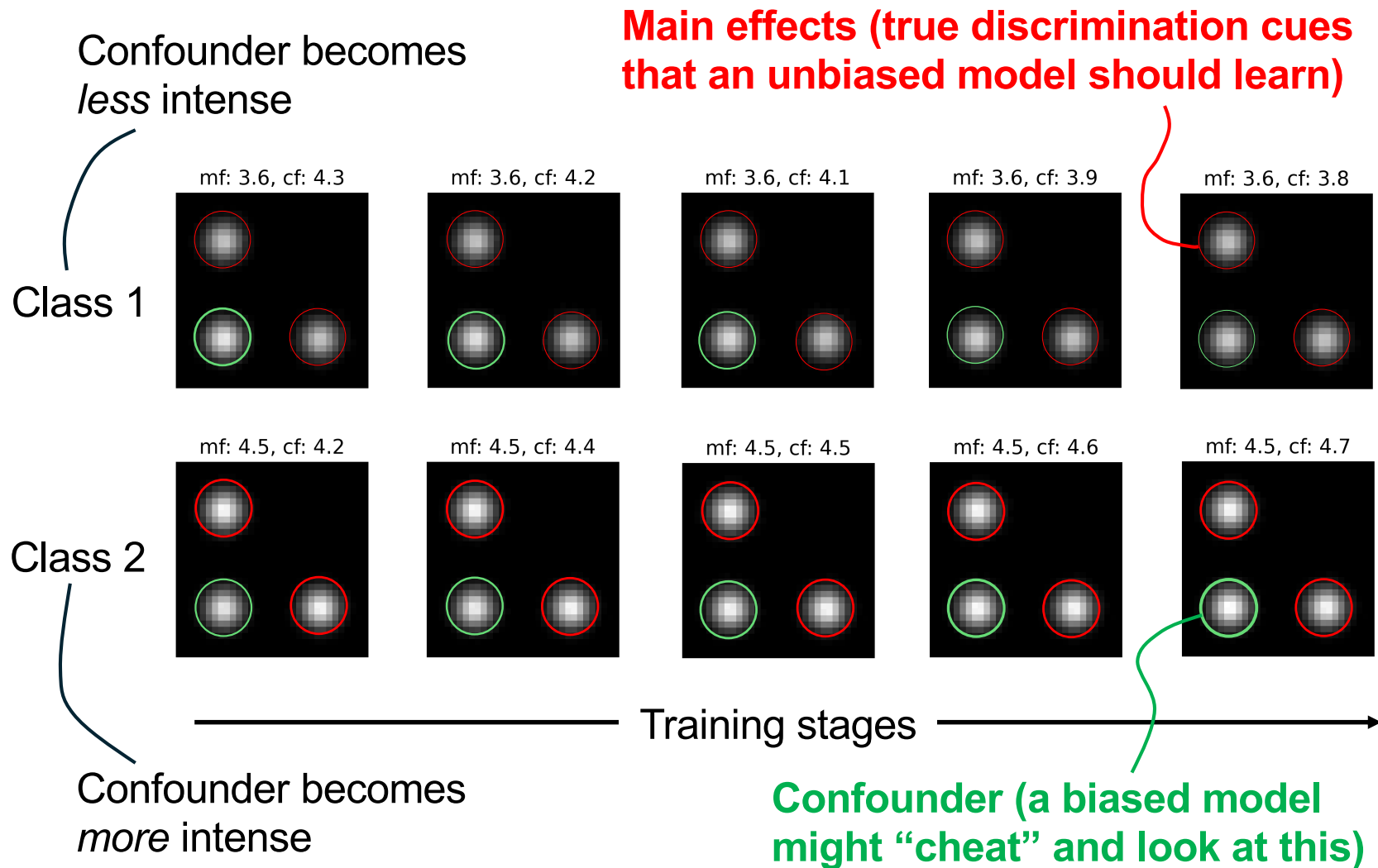
# Recursive Metadata Normalization



**Parameter Updates:**  $\beta(N + 1) = \beta(N) + K(N + 1)e(N + 1),$

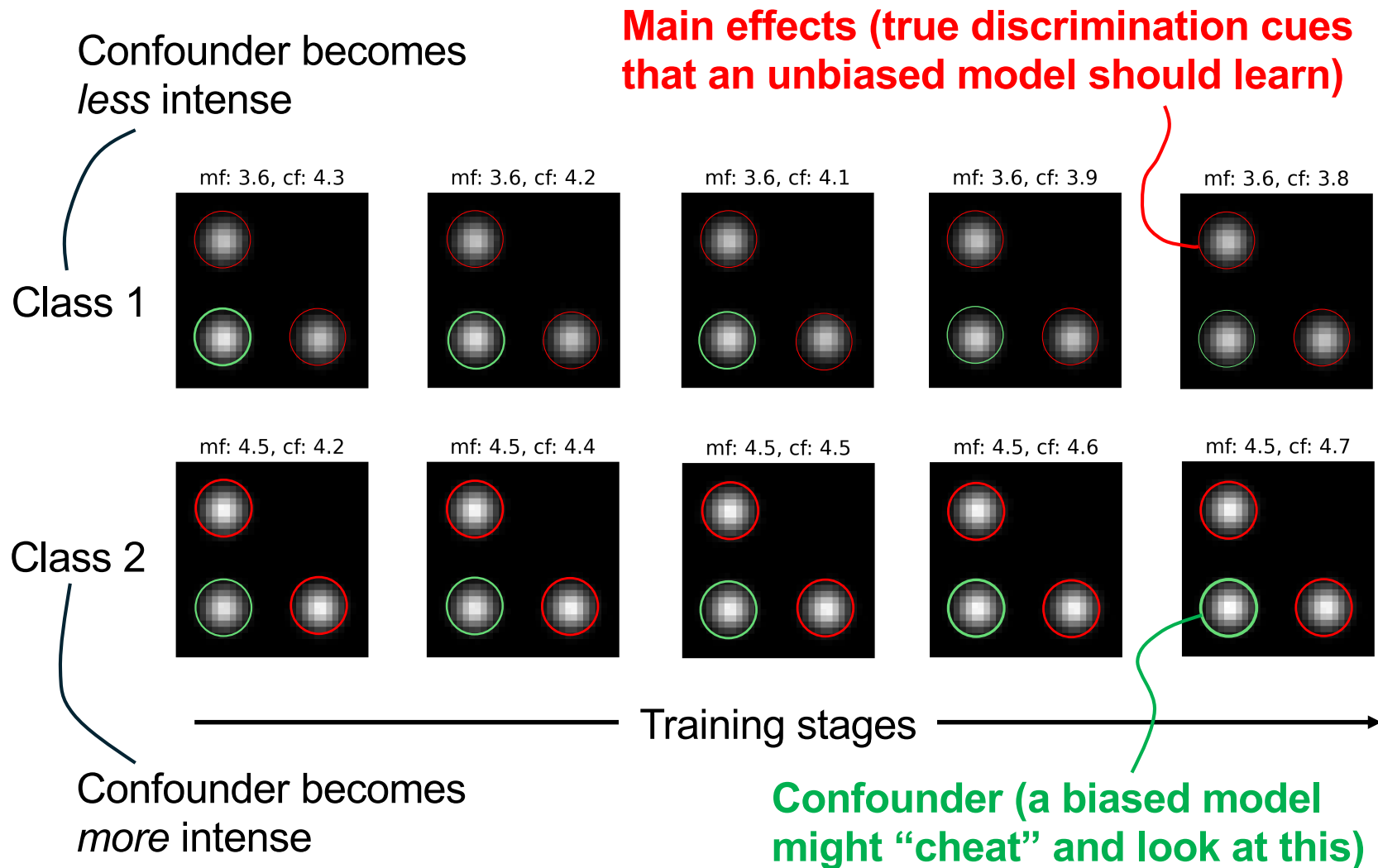
where  $e(N + 1) = z_{N+1} - X_{N+1}^T \beta(N)$  is the a priori error  
and  $K(N + 1)$  is the Kalman Gain at the  $N + 1$  step

# R-MDN effectively removes confounder influence from learned DNN features





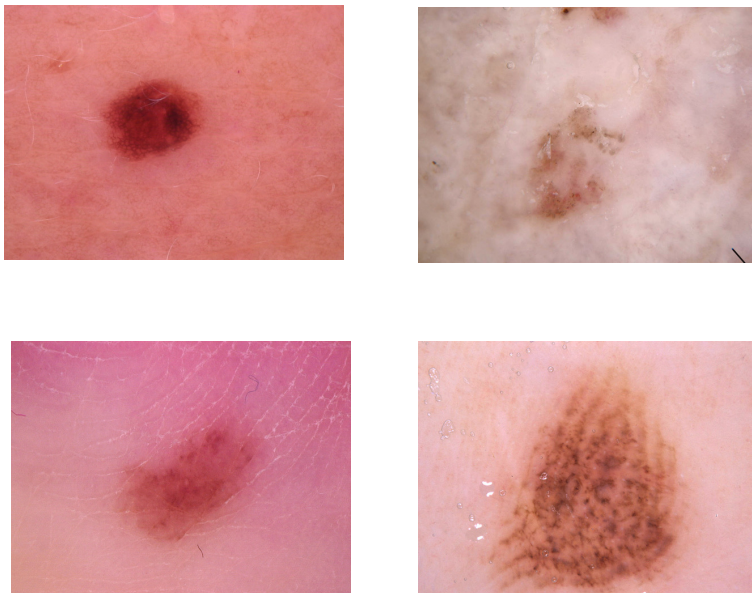
# R-MDN effectively removes confounder influence from learned DNN features



Method	Deviation of accuracy from (↓) theoretical accuracy
CNN Baseline	$0.18 \pm 0.00$
BR-Net	$0.04 \pm 0.03$
Stage-specific MDN	$0.25 \pm 0.00$
P-MDN	$0.04 \pm 0.01$
R-MDN	$0.02 \pm 0.01$

# R-MDN is a normalization layer and can be tacked on to various model architectures

Skin lesion classification on HAM10K<sup>1</sup> dataset, with age as confounder



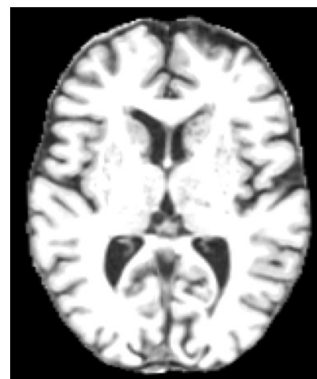
Example images from HAM10K

Method	Accuracy	Average dcor <sup>2</sup> (↓)
ViT Baseline	$0.7095 \pm 0.0626$	$0.0864 \pm 0.0336$
BR-Net (Adeli et al., 2020a)	$0.7247 \pm 0.0627$	$0.0544 \pm 0.0534$
P-MDN (Vento et al., 2022)	$0.6750 \pm 0.0945$	$0.2595 \pm 0.0620$
R-MDN (A)	$0.5503 \pm 0.0541$	$0.0928 \pm 0.0630$
R-MDN (B)	$0.5288 \pm 0.0571$	$0.0739 \pm 0.0555$
R-MDN (C)	$0.6919 \pm 0.0723$	<b><math>0.0475 \pm 0.0247</math></b>
EWC (Kirkpatrick et al., 2017)	$0.6437 \pm 0.0586$	$0.0938 \pm 0.0506$
EWC + R-MDN (C)	$0.6739 \pm 0.0686$	$0.0592 \pm 0.0488$
LwF (Li & Hoiem, 2017)	$0.7356 \pm 0.0757$	$0.0512 \pm 0.0407$
LwF + R-MDN (C)	$0.7186 \pm 0.0736$	$0.0354 \pm 0.0210$
PackNet (Mallya & Lazebnik, 2018)	$0.6849 \pm 0.0745$	$0.0470 \pm 0.0304$

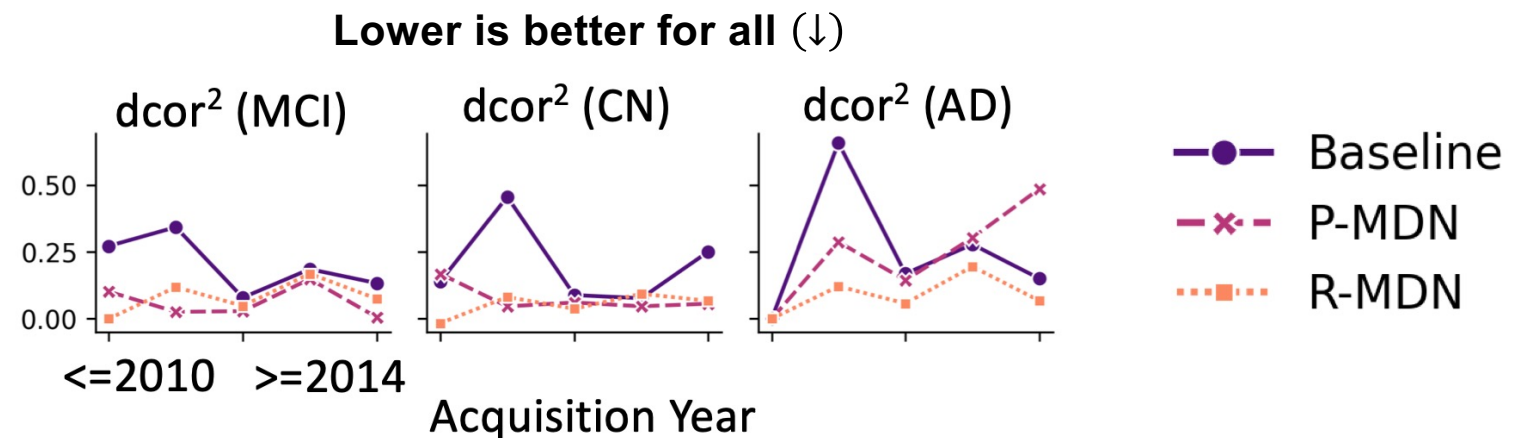
<sup>1</sup>Tschandl et al. *The HAM10000 dataset, a large collection of multi-source dermoscopic images of common pigmented skin lesions*. In Scientific Data, 2018.

# R-MDN can remove the influence from multiple confounders

Diagnostic classification on ADNI<sup>1,2</sup> dataset, with both age and sex as confounders



Example images from ADNI

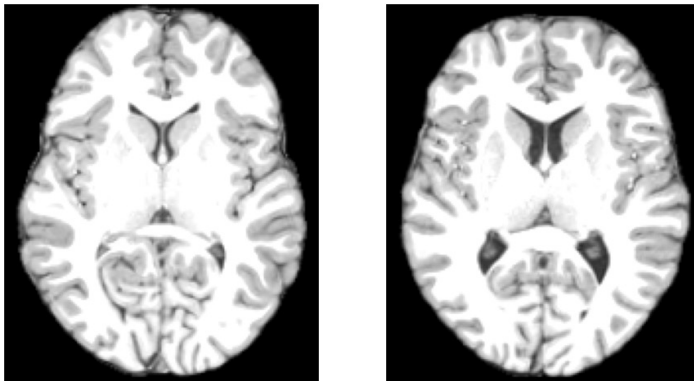


<sup>1</sup>Mueller et al. *The Alzheimer's Disease Neuroimaging Initiative*. In *Neuroimaging Clinics of North America*, 2005.

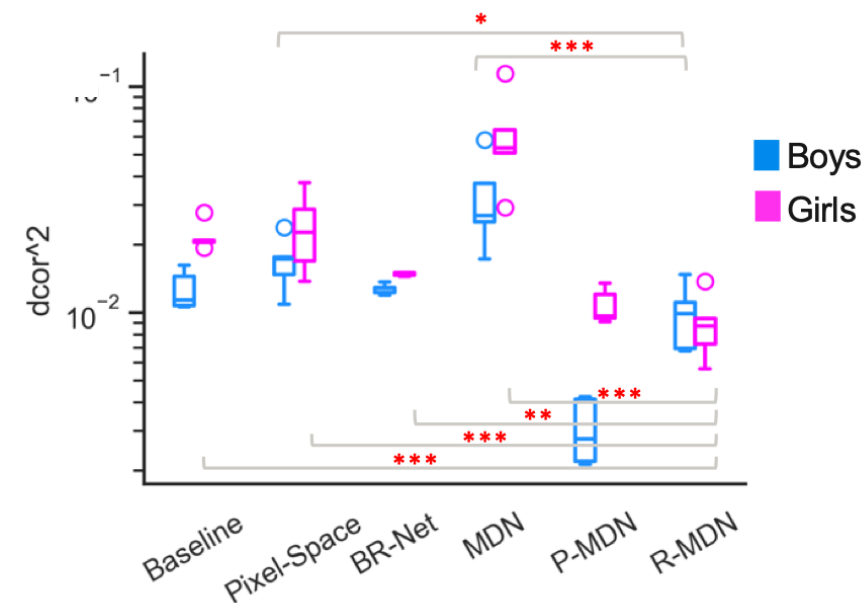
<sup>2</sup>Peterson et al. *Alzheimer's Disease Neuroimaging Initiative (ADNI) Clinical Characterization*. In *Neurology*, 2010.

# R-MDN makes equitable predictions across population groups

Sex classification on ABCD<sup>1</sup> dataset, with Pubertal Development Score (PDS) as confounder

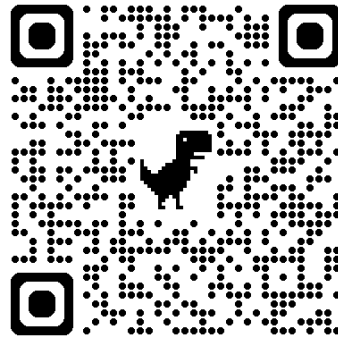
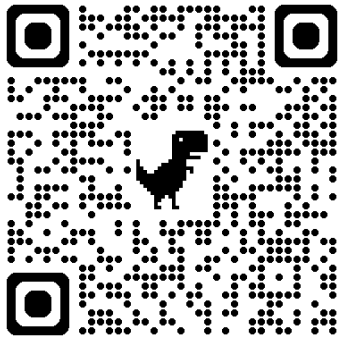


Example images from ABCD



<sup>1</sup>Casey et al. *The Adolescent Brain Cognitive Development (ABCD) Study: Imaging Acquisition across 21 sites*. In *Developmental Cognitive Neuroscience*, 2018.

# Interested in knowing more?



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