# Language Models over Canonical Byte-Pair Encodings





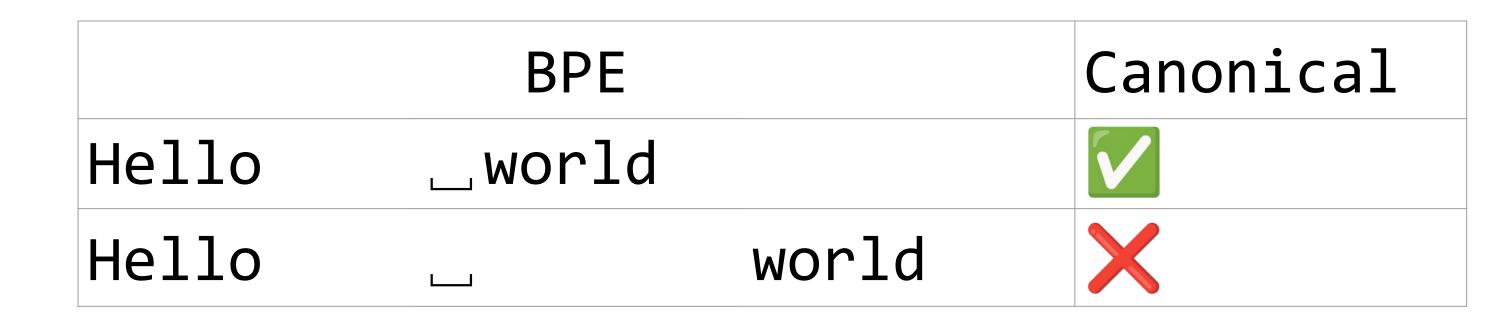


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# Background

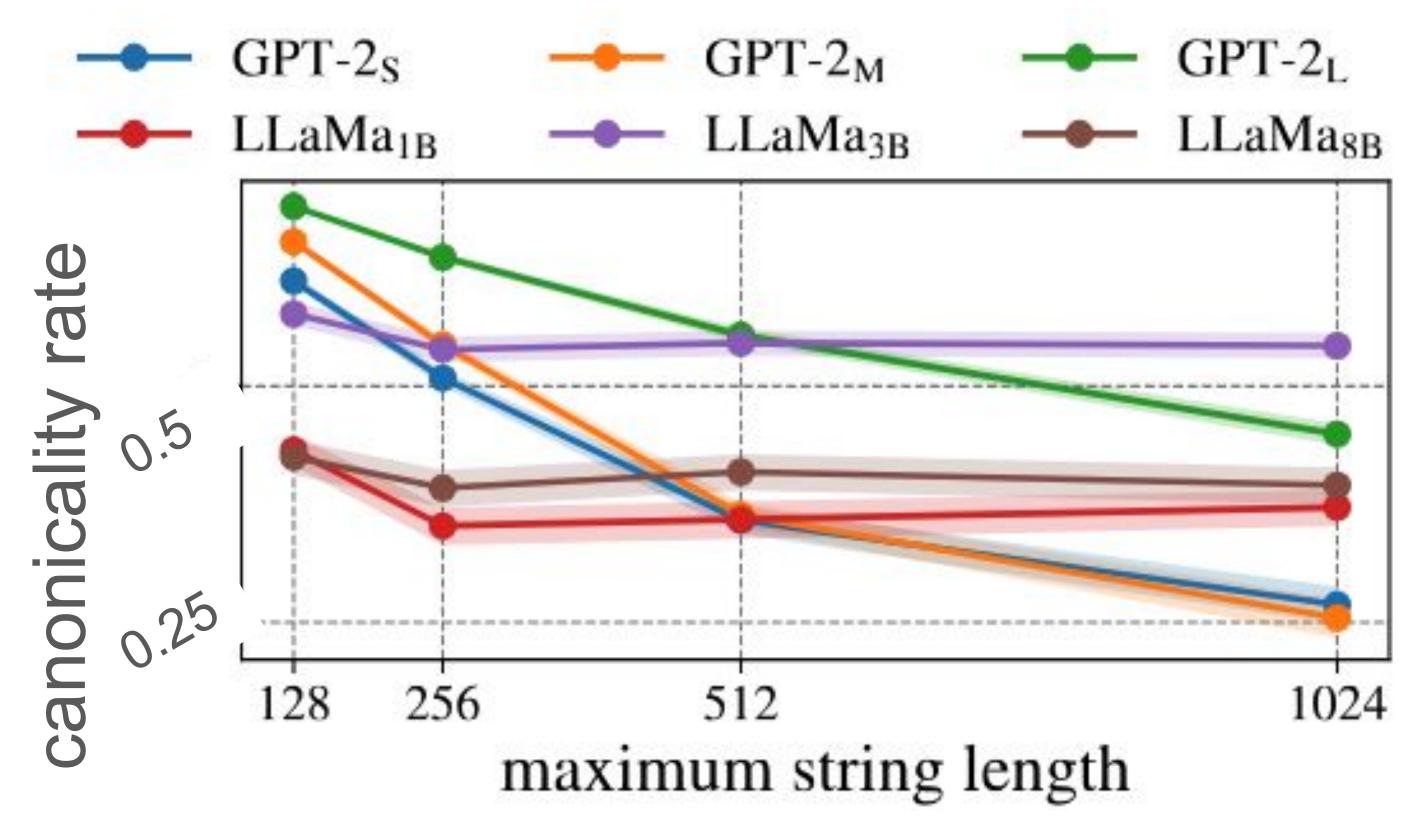
In byte-pair encodings (BPE), some token combinations never appear during training, but might appear during decoding.

Example: "Hello world"



This misallocation is both erroneous, as noncanonical strings never appear in training data, and wasteful!

Much of the probability mass is misallocated to noncanonical sequences!



Most sequences sampled from most language models are noncanonical!

Longer sequences are more vulnerable to this

probability mass leakage..

## **Theoretical Guarantees**

Enforcing canonicality is guaranteed to make language models better (closer to the ground-truth distribution of sentences).

# Reduction in KL divergence to the ground-truth LM

$p_{\Delta}$	LM before canonicalization
$p^{\star}_{\Delta}$	Ground-truth LM
$\boldsymbol{g}$	LM after canonicalization

$$\mathrm{KL}(p_{\Delta}^{\star} \parallel p_{\Delta}) - \mathrm{KL}(p_{\Delta}^{\star} \parallel g) = \underbrace{-\log Z}_{\geq 0}$$

Where Z is the canonicality rate of the LM before canonicalization

# **Enforcing Canonicality**

We propose two ways to enforce canonicality in LMs.

# 1. Canonicality by conditioning

Without retraining the language model, we develop an efficient algorithm that forces only canonical sequences to be generated.

#### 2. Canonicality by construction

We finetune a language model to get a parameterization that guarantees canonical outputs.

## The Algorithm

For two any two tokens  $\delta$  and  $\delta$ ' in the vocabulary  $\Delta$ , we compute find\_conflict( $\delta$ , $\delta$ ') to check if it causes a noncanonicality. The find\_conflict function can be pre-computed for all tokens as masks. And we use the masks in a logits processor to avoid generating any tokens that lead to a noncanonical sequence.

Improvement = log(canonicality rate)

/4	Model				
			Baseline	Local	Global
PTB	-2	small	201.0	200.7	199.1
	GPT	medium	195.1	194.5	193.1
	g	large	189.4	188.9	188.2
	Llama	1B	171.2	171.1	169.7
		3B	165.0	165.0	164.2
	T	8B	161.5	161.5	160.1
WikiText	-2	small	369.2	367.0	367.3
	M	medium	334.1	333.2	332.2
	g	large	320.8	319.1	319.6
	1a	1B	286.7	284.4	285.2
	Llama	3B	264.6	262.0	263.7
	Г	8B	248.2	245.8	246.8

# Results

We observe improvements in language modeling log-likelihood on all models on PTB and WikiText, without any finetuning.

The gain is large when the LM has lower canonicality rate. Also, the gain is larger when modeling longer sequences.

paper:

