

# Collapse-Proof Non-Contrastive Self-Supervised Learning



Emanuele



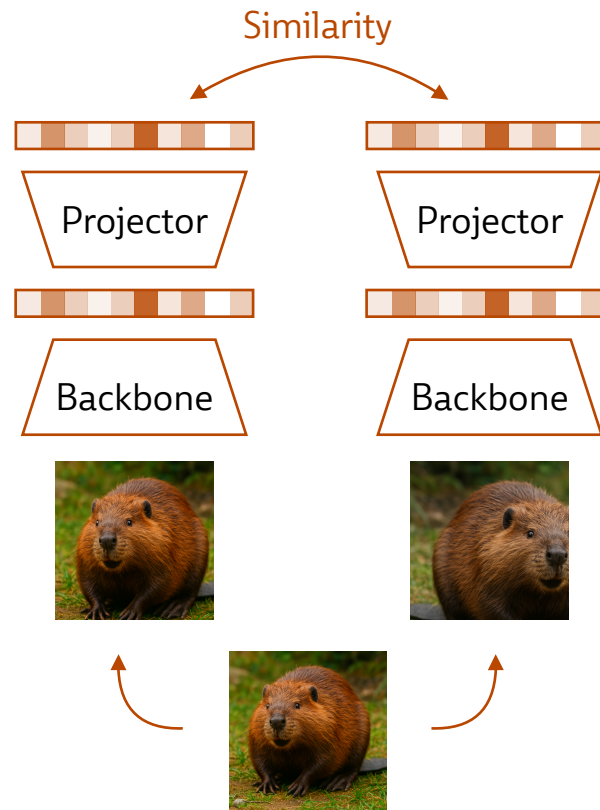
Tim



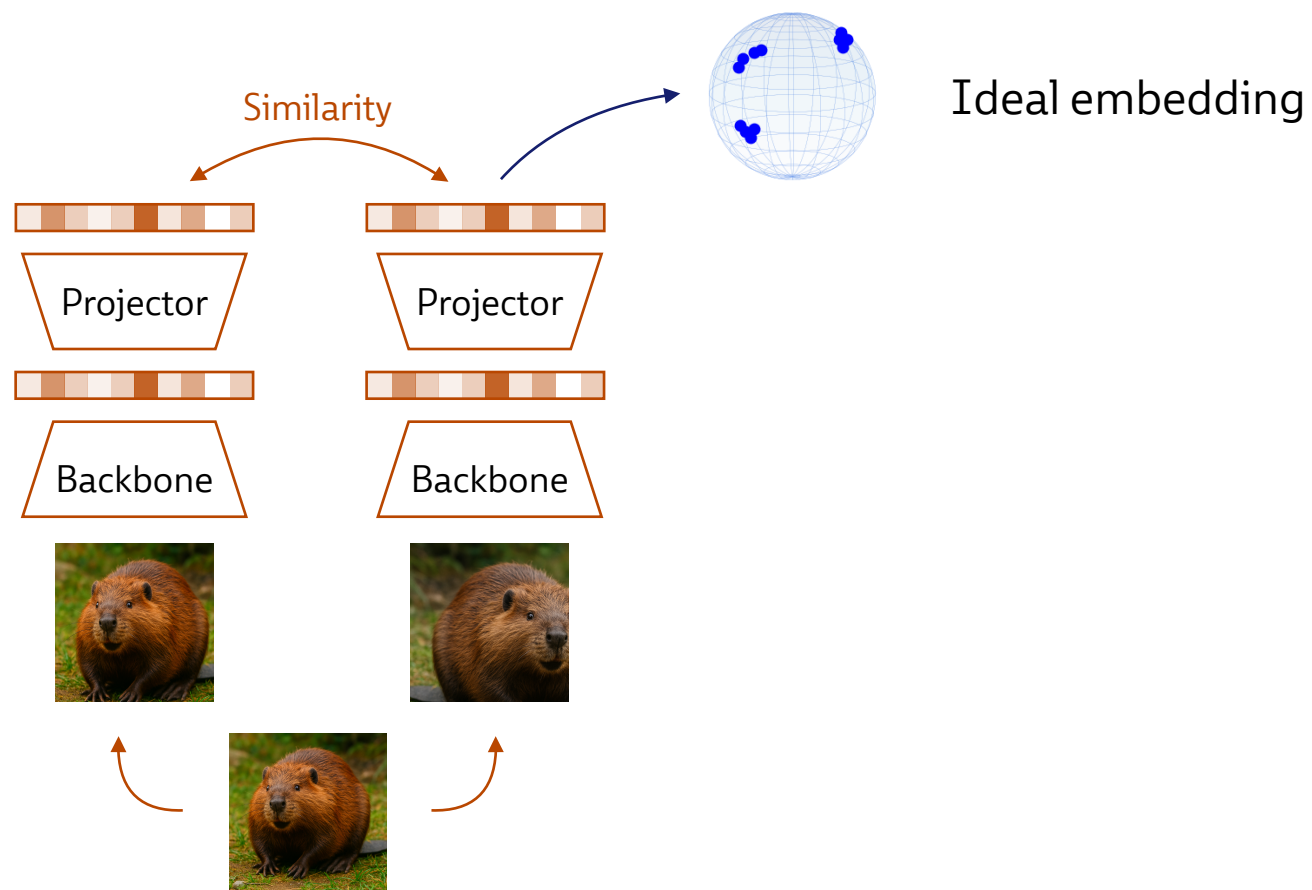
Tinne



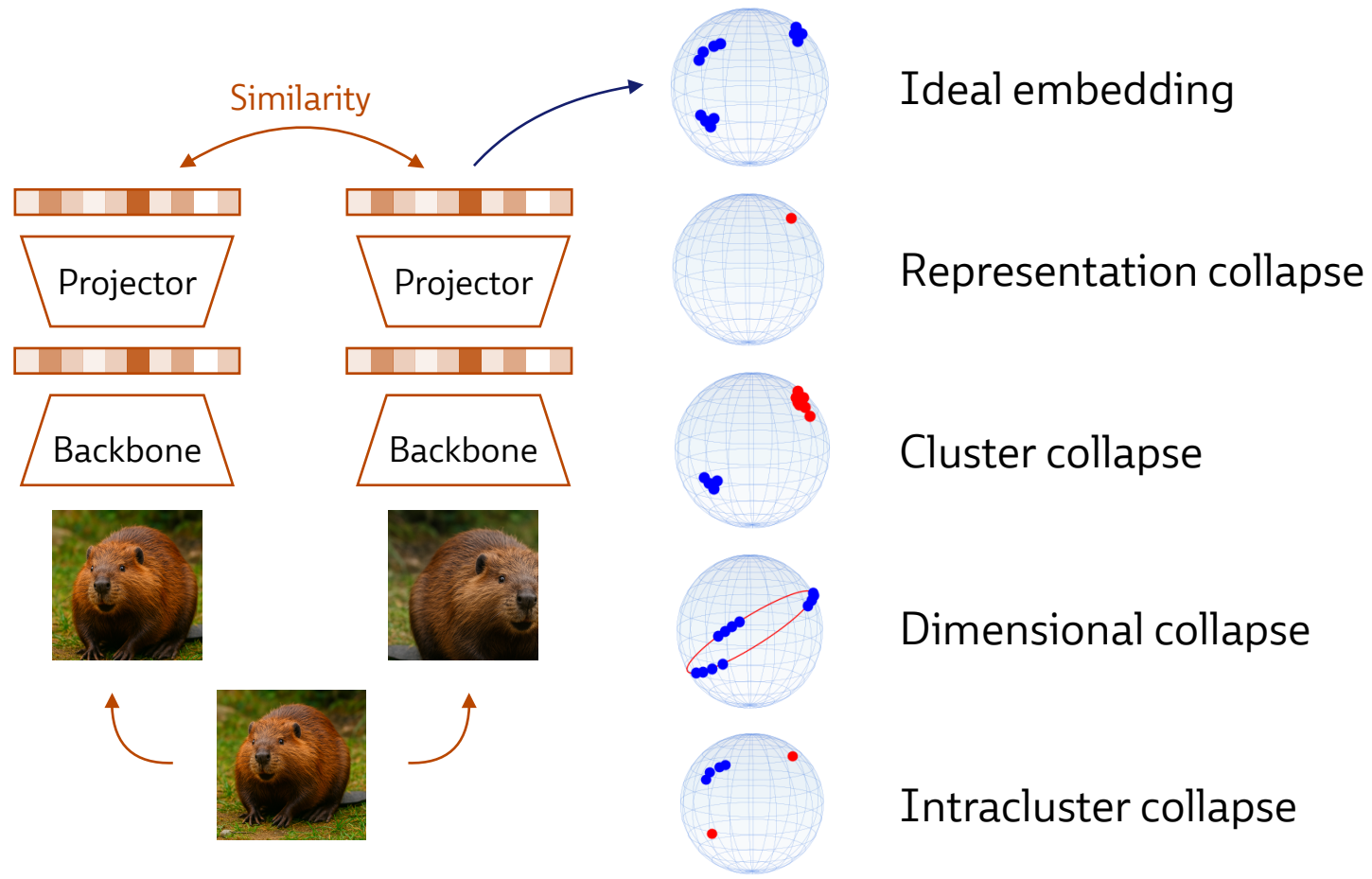
# Non-Contrastive Learning ?



# What Can Go Wrong ?



# What Can Go Wrong ?





# What Are The Main Non-Contrastive Strategies ?

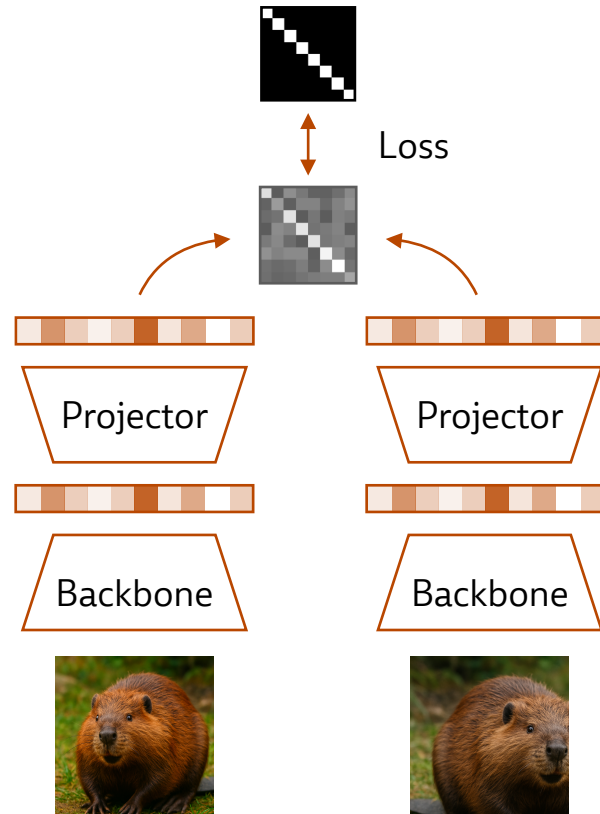
## Feature Decorrelation

Barlow Twins [Zbontar et al. ICML 2021] , ...

## Clustering

SwAV [Caron et al. NeurIPS 2020] , ...

# What Are The Main Non-Contrastive Strategies ?



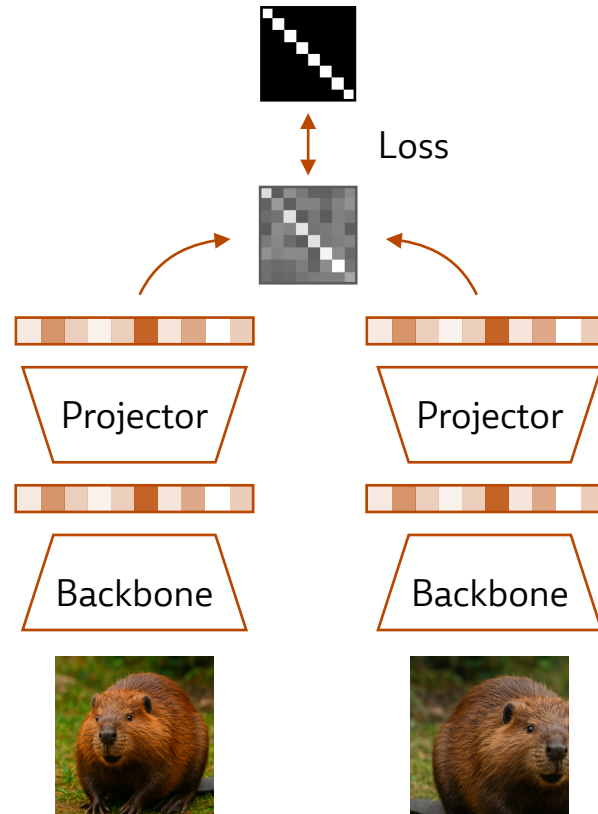
## Feature Decorrelation

Barlow Twins [Zbontar et al. ICML 2021] , ...

## Clustering

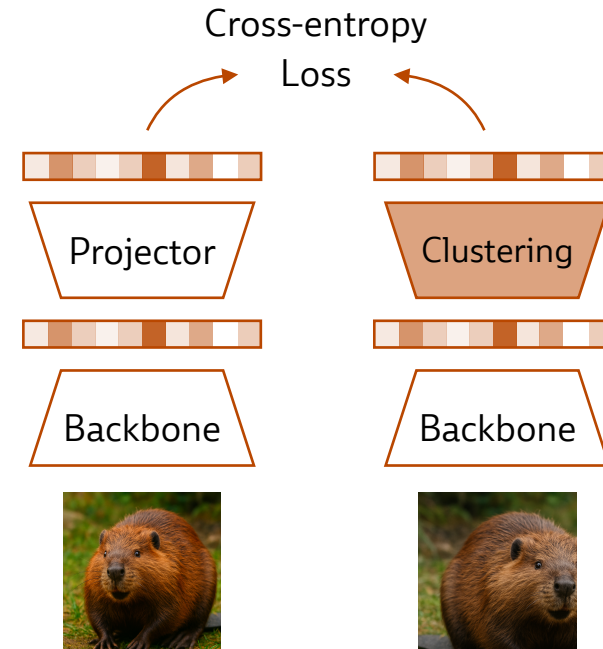
SwAV [Caron et al. NeurIPS 2020] , ...

# What Are The Main Non-Contrastive Strategies ?



Feature Decorrelation

Barlow Twins [Zbontar et al. ICML 2021] , ...



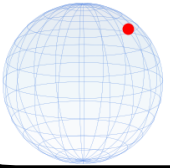
Clustering

SwAV [Caron et al. NeurIPS 2020] , ...

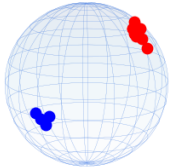
# Are Existing Strategies Collapse-Proof?

Feature Decorrelation

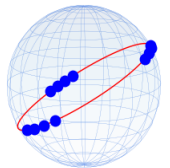
Clustering



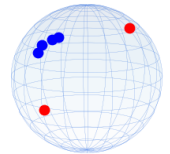
Representation collapse



Cluster collapse

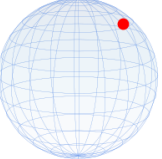
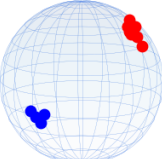
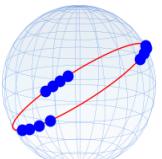
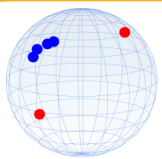


Dimensional collapse



Intracluster collapse

# Are Existing Strategies Collapse-Proof?

	Feature Decorrelation	Clustering
 Representation collapse	✓	✓
 Cluster collapse	✗	✓
 Dimensional collapse	✓	✗
 Intracluster collapse	✗	✗

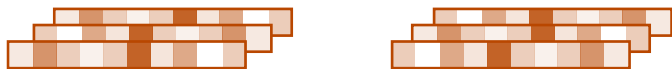
# Key Contributions

1. Sufficient conditions for avoiding collapses

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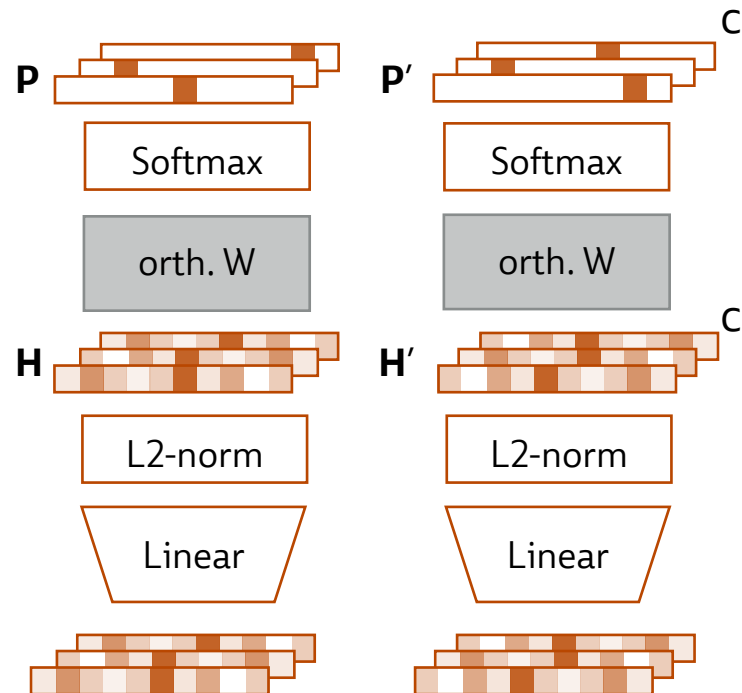
1. Sufficient conditions for avoiding collapses
2. Design guidelines for the projector and the loss function based on hyperdimensional computing

# Proposed Design of Projector and Loss Function

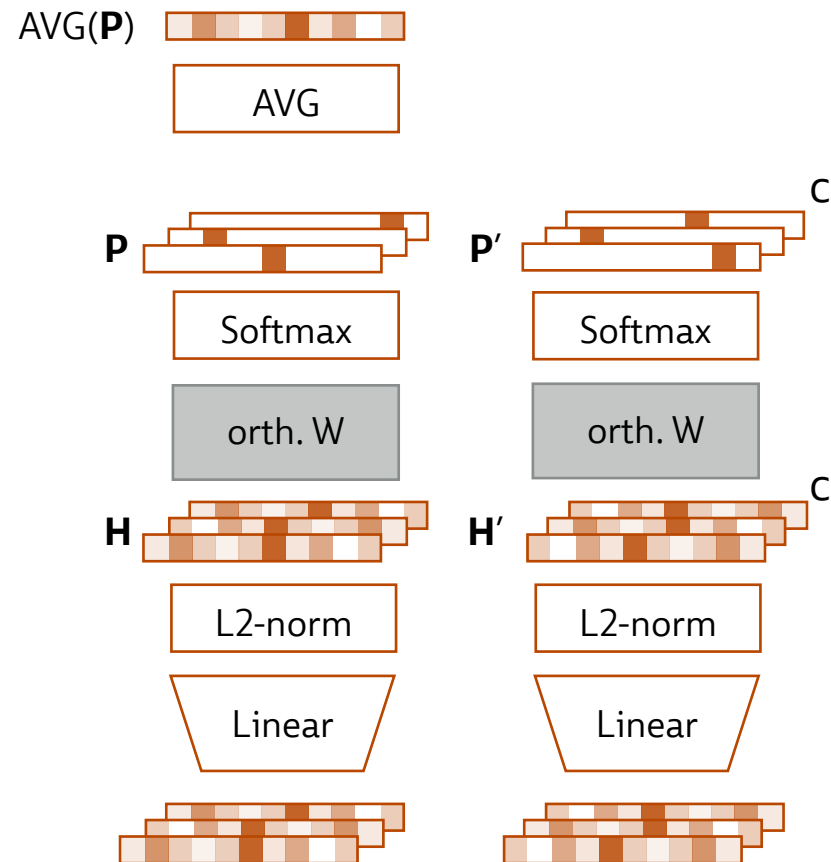




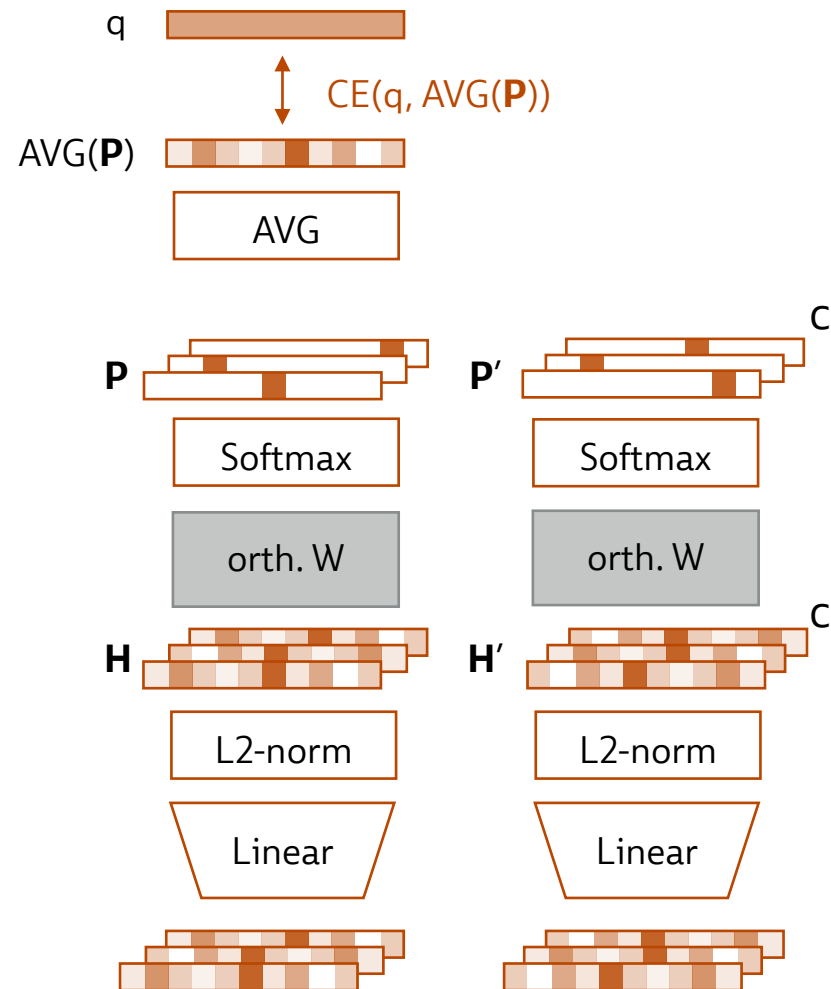
# Proposed Design of Projector and Loss Function



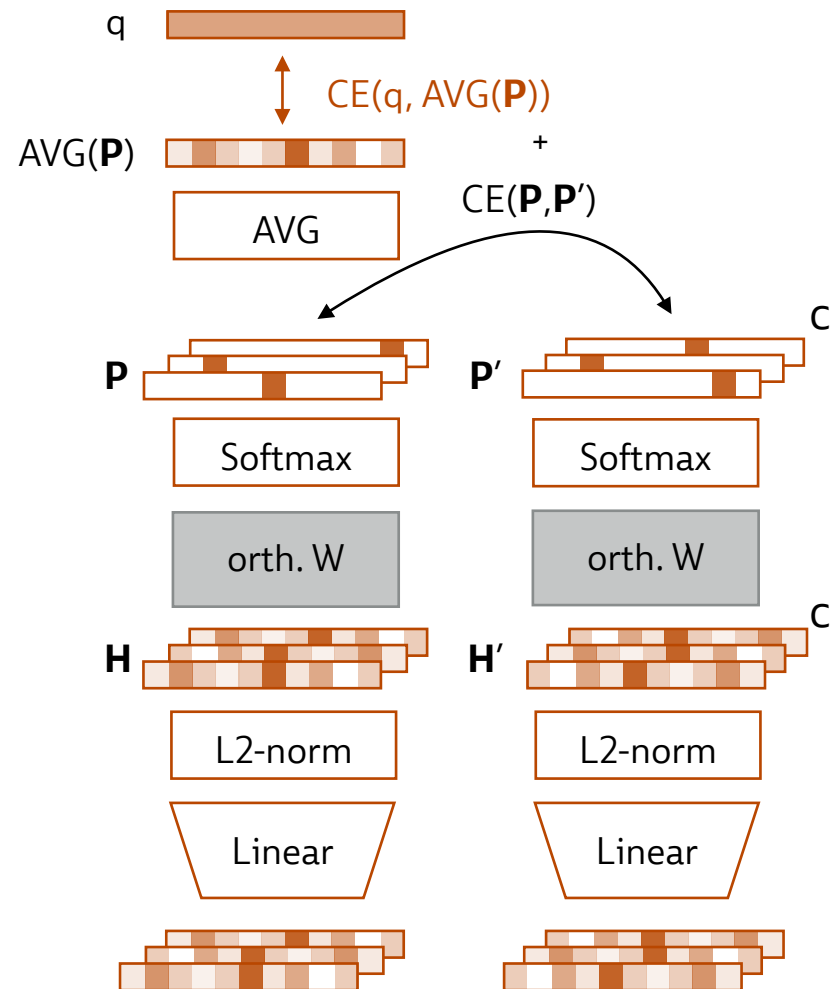
# Proposed Design of Projector and Loss Function



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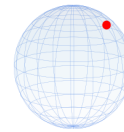
# Properties of The Loss Function



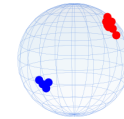
# Properties of The Loss Function



(Lemma) If optima are attained, then:



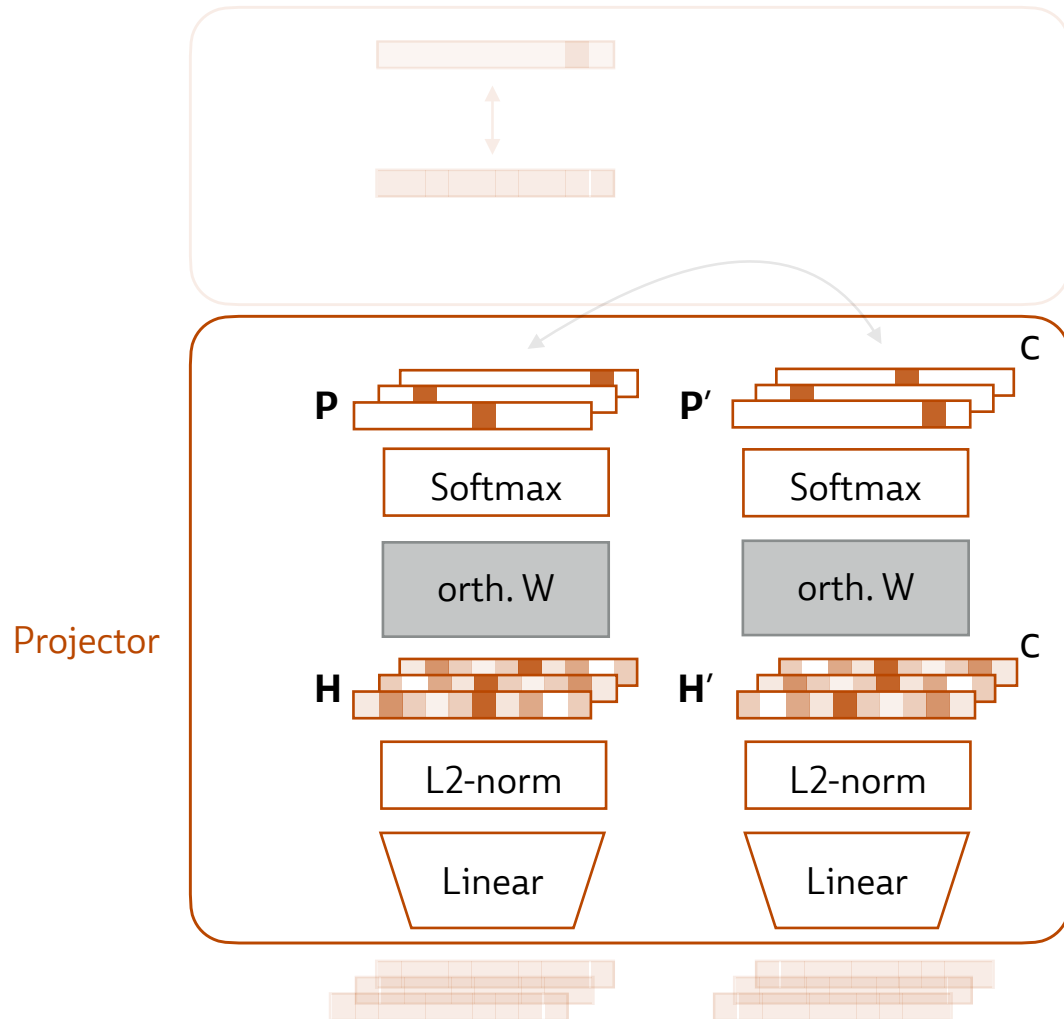
Representation collapse



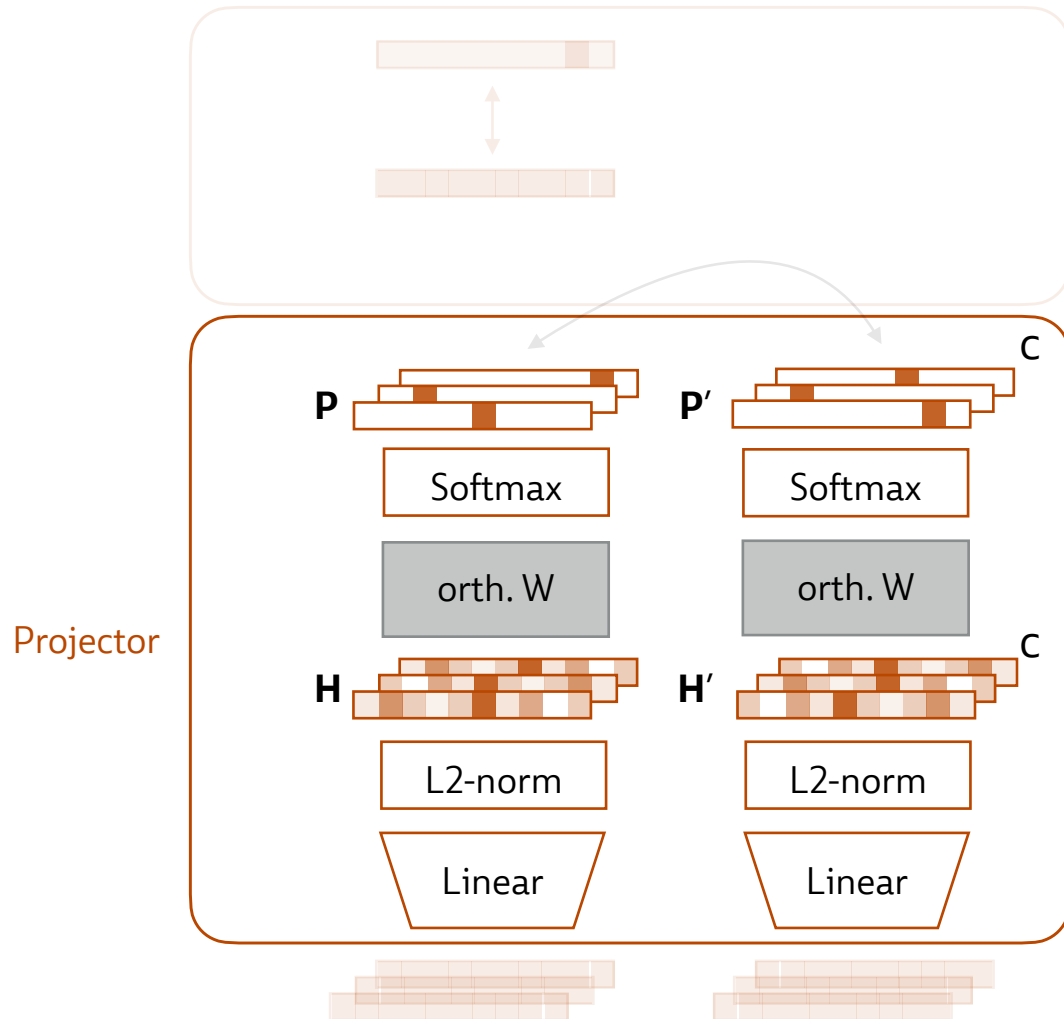
Cluster collapse



# Properties of The Projector



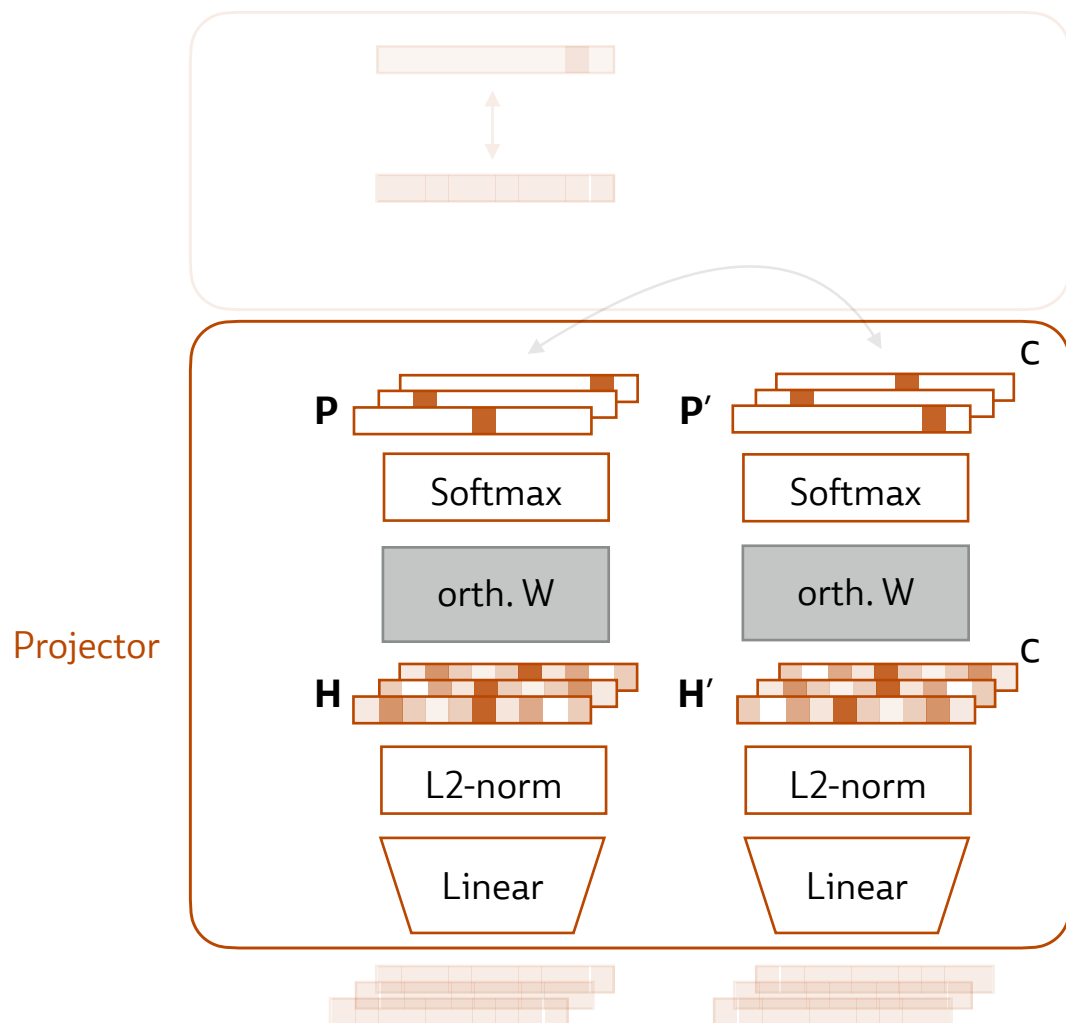
# Properties of The Projector



(Embedding Theorem) If optima of the loss are attained and  $c \rightarrow \infty$ :

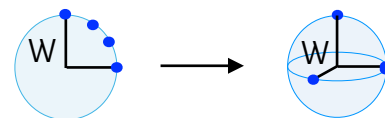


# Properties of The Projector



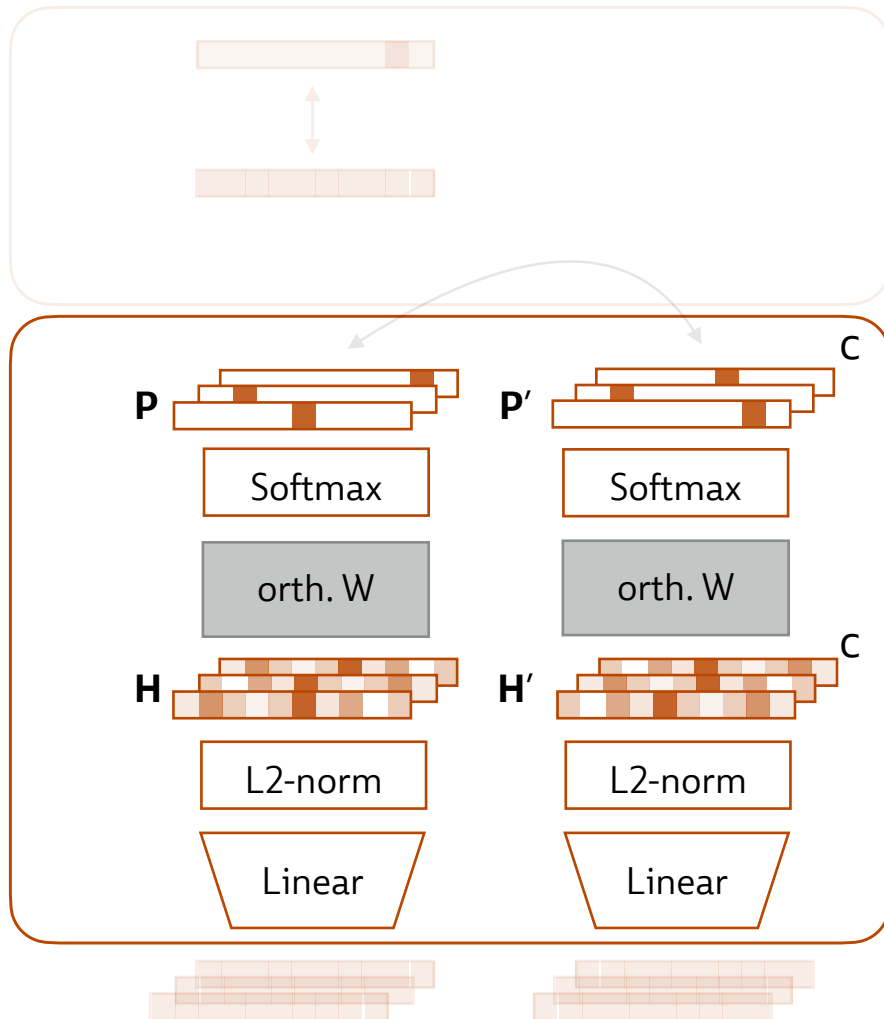
(Embedding Theorem) If optima of the loss are attained and  $c \rightarrow \infty$ :

1. Perfect alignment



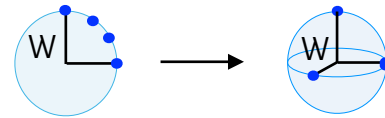
# Properties of The Projector

Projector



(Embedding Theorem) If optima of the loss are attained and  $c \rightarrow \infty$ :

1. Perfect alignment



2. Sample covariance  $(\mathbf{H})^T \mathbf{H} = \mathbf{I}$  is diagonal

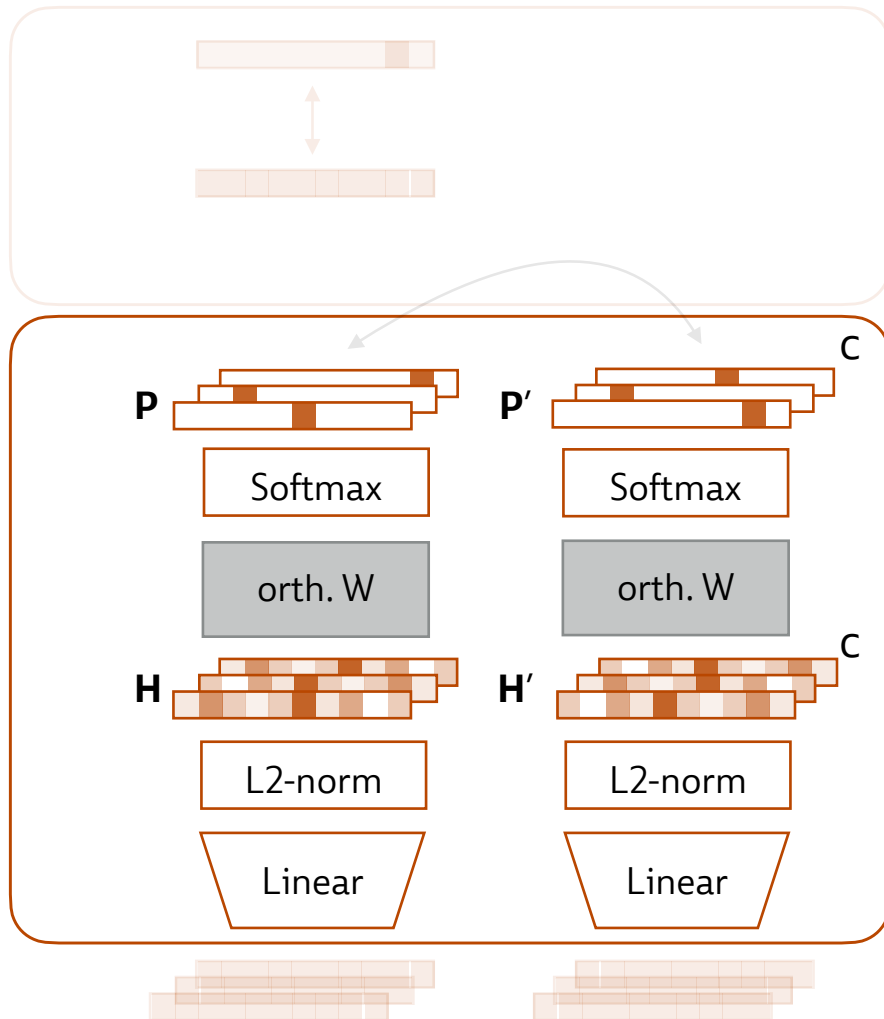


Dimensional collapse



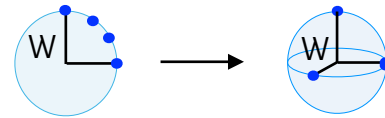
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Projector



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Dimensional collapse



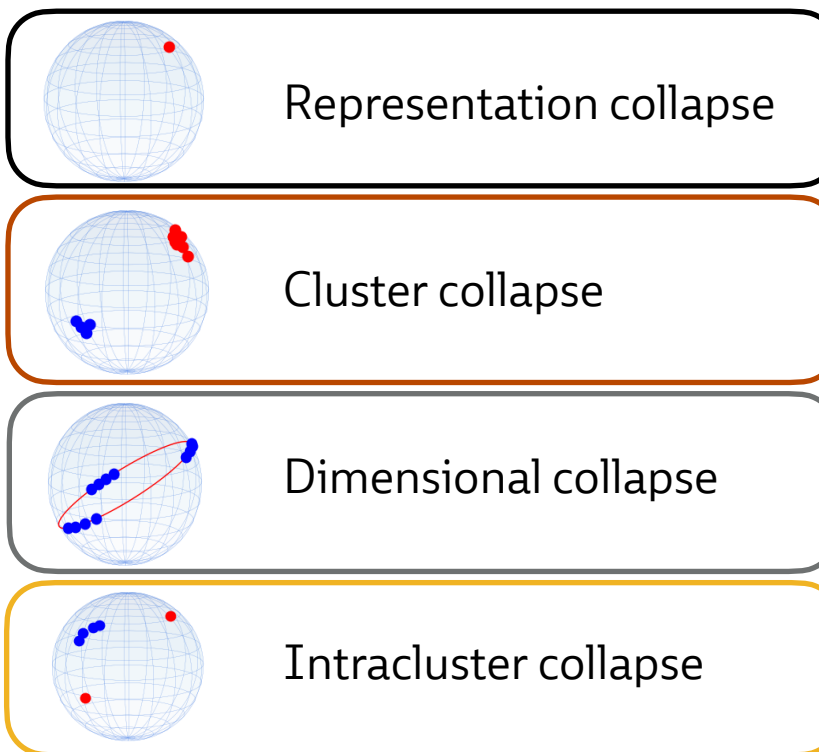
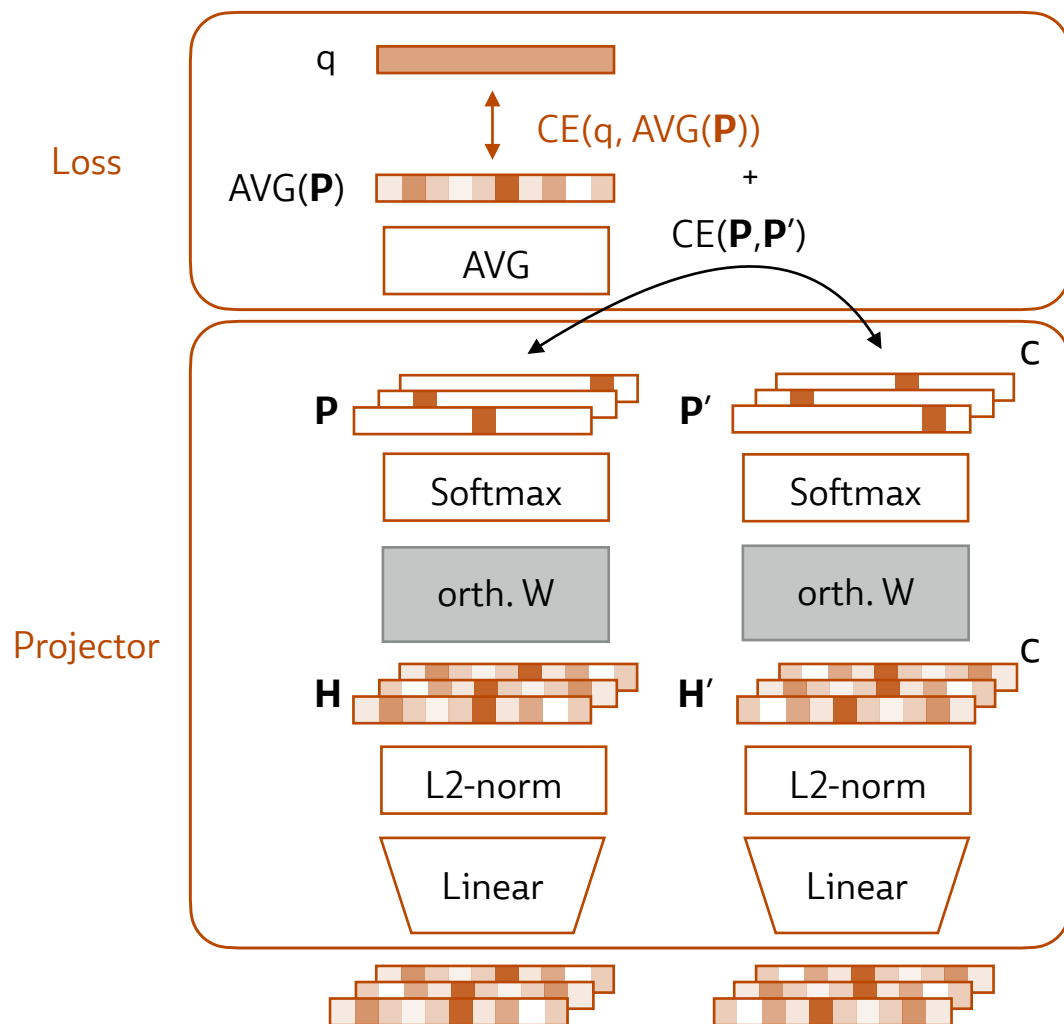
3. Adjacency  $\mathbf{H}(\mathbf{H})^T$  is block-diagonal and block-size  $\rightarrow 0$



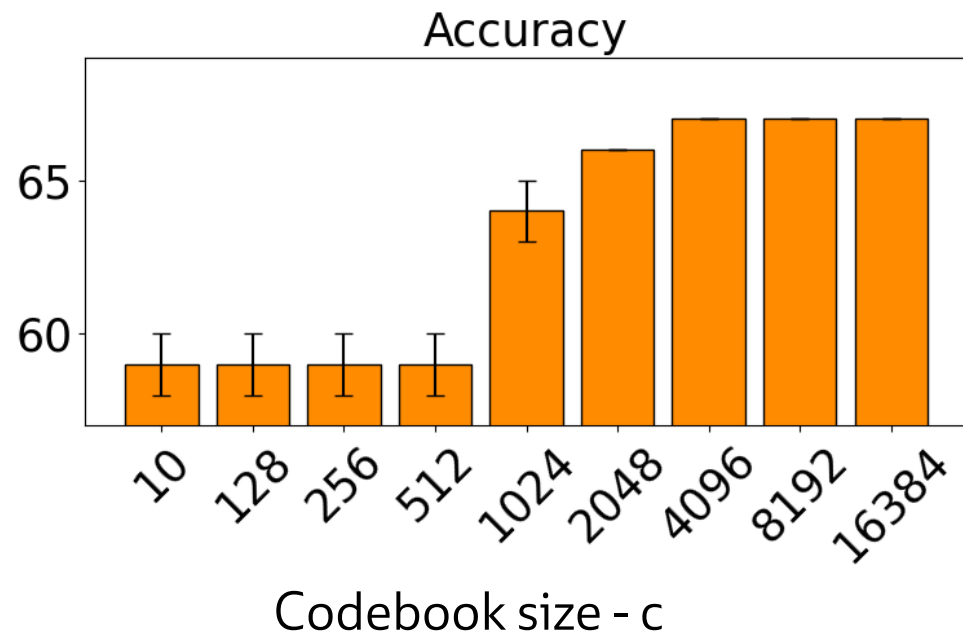
Intracluster collapse



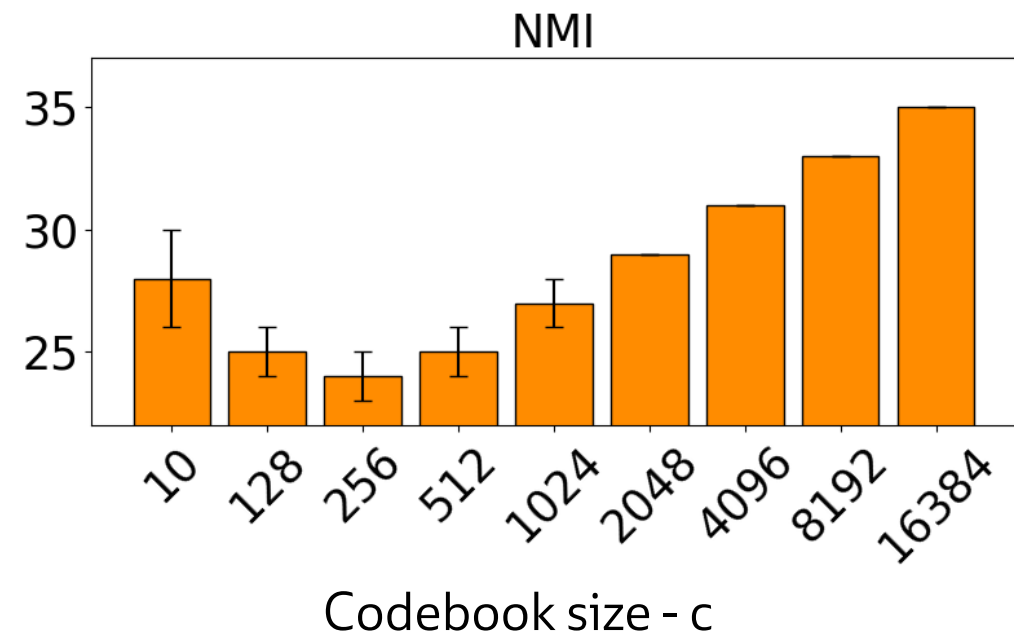
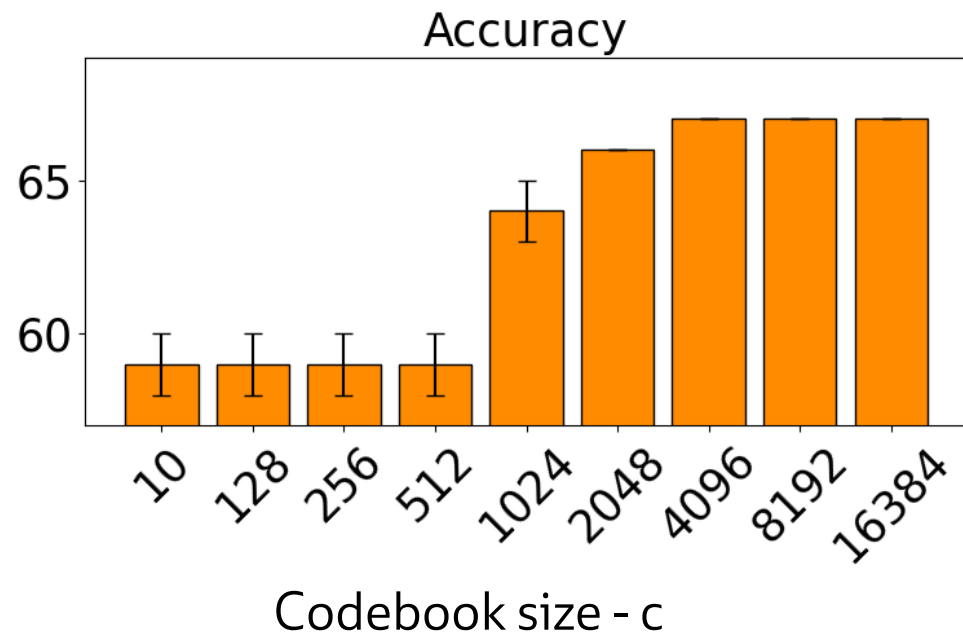
# Collapse-Proof



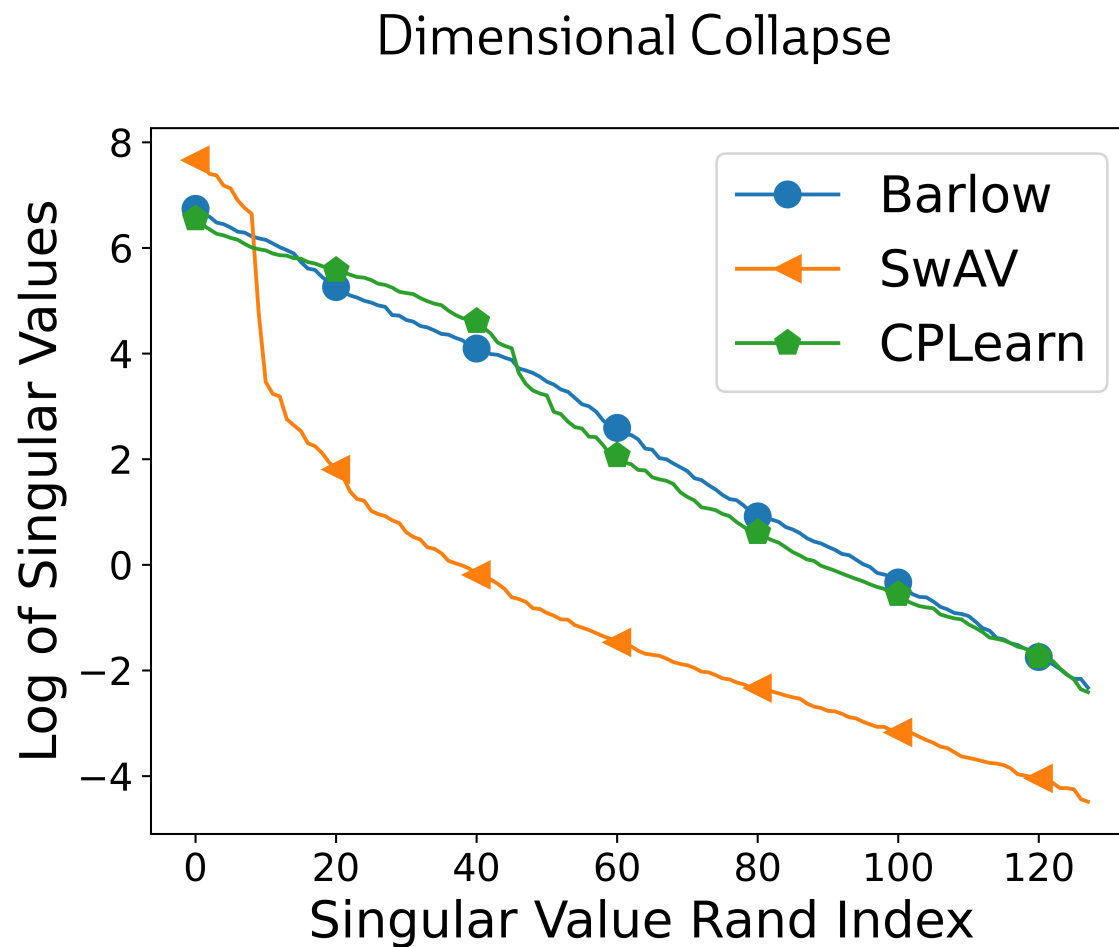
# Experiments on CIFAR-10 with ResNet



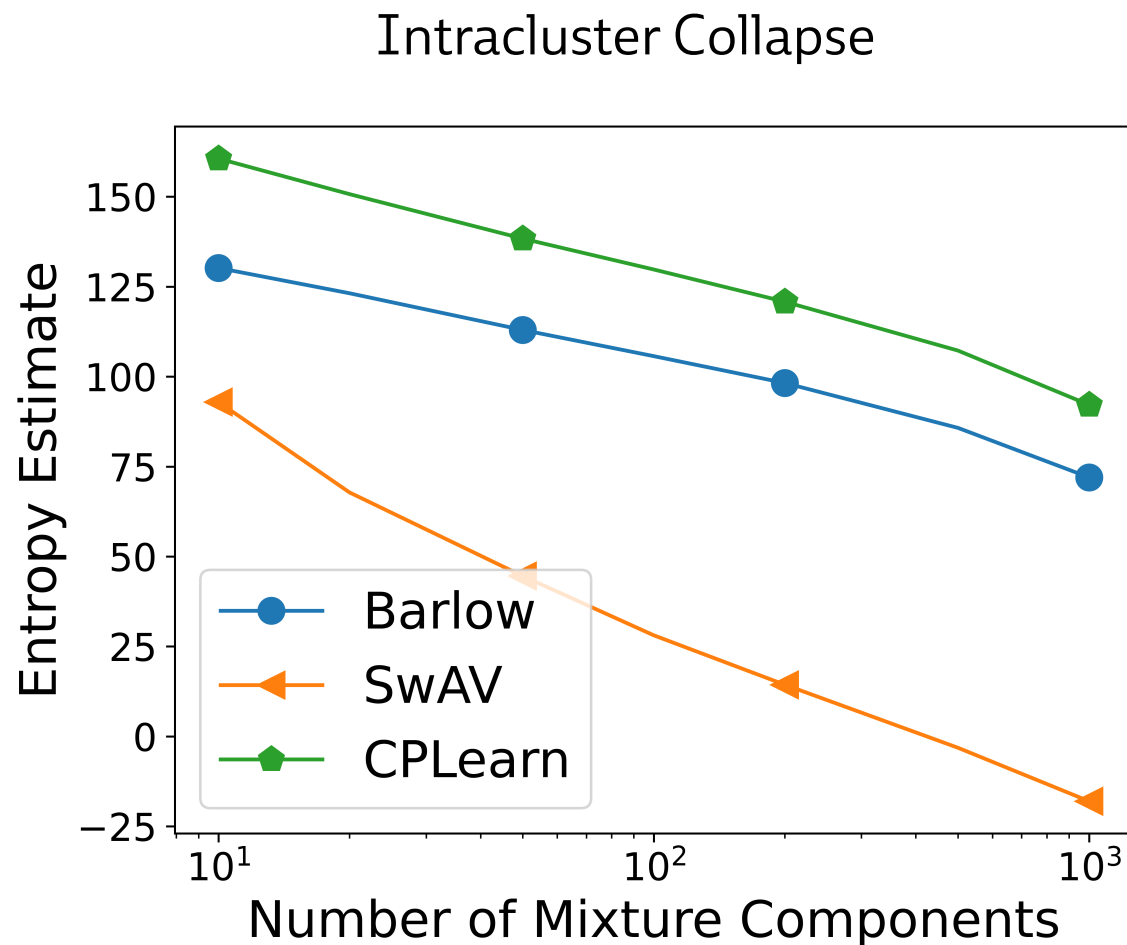
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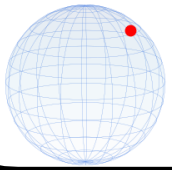
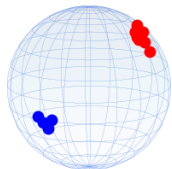
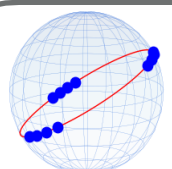
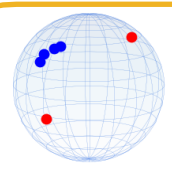
# Experiments on CIFAR-10 with ResNet





# Thank You !

 @skiera87

	Feature Decorrelation	Clustering	CPLearn
 Representation collapse	✓	✓	✓
 Cluster collapse	✗	✓	✓
 Dimensional collapse	✓	✗	✓
 Intracluster collapse	✗	✗	✓