slides available at:



# **Strategic ML:** How to Learn With Data That **'Behaves'**

## Nir Rosenfeld

Technion CS

tutorial @ ICML 2024





## this is machine learning:



### this is machine learning on images:



## this is machine learning on text:











what could possibly go wrong?

(or: how does human behavior change learning and its outcomes?)

- Builds on **conventional binary classification**
- Augments to account for human behavior
- Models humans as **inputs with agency**

- Allows (and requires!) to encode what humans:
- Basic elements of economic modeling
- Together, combine to determine how humans behave



homo-sapiens

modeling challenge: weave these into learning setup

- SC is great because it is:
  - simple enough to permit tractable analysis
  - > powerful enough to introduce novel challenges
  - > meaningful enough to have social implications
  - flexible enough to permit extensions, variations, and generalizations
- Start with **rigid assumptions** e.g., rationaity:



homo-sapiens

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homo-economicus

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  - flexible enough to permit extensions, variations, and generalizations
- Start with **rigid assumptions** e.g., rationaity
- Ultimate goal: capture realistic behavior "in the wild"



homor-simpsonus

# Outline

Introduction

#### • Three main sections:

#### I) ML aspects: (~40 min)

- strategic learning setup
- as learning vs. as a game
- optimization
- generalization (stats)
- modeling
- Challenges and opportunities
- Summary

#### II) Econ/GT aspects: (~60 min)

- incentives (=want)
- information (=know)
- actions (=do)
- limited resources
- social welfare

#### III) Beyond: (~20 min)

- causality
- dependencies
- over time

## Tutorial theme and goals

- Introduction to **emerging new field**
- Many open research questions
- Much potential for application
- Main theme: transitioning from theory → practice
- Focus on supervised batch setting (covers "half" of literature; other part being online)
- More **breadth** (less **depth**) → *see references*
- More modeling (less results)
- More questions (less answers)
- More **content** (less **time**) → *fast paced*!

an introduction

# standard classification:

learned model

train:





# standard classification:

learned model

train:

$$\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$$

$$input features$$

$$h(x) = \hat{v} \approx v$$

test:

$$h(x) = \hat{y} \approx y$$

prediction

ground truth



train:

test:

[BS'2011, HMPW'2016] learned model argmin  $\mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ h representation of human agent  $h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$ prediction ground truth





train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ 

test:

 $h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$ 





**1. want:**  $\hat{y} = 1$  (get the loan)

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ 

test:

 $h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$ 





**1. want:**  $\hat{y} = 1$  (get the loan)

**2. do:** modify features (at cost)

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ 

test:

 $h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$ 





**1. want:**  $\hat{y} = 1$  (get the loan)

- **2. do:** modify features (at cost)
- **3. know:** h (and cost function)

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ 

test:

$$h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$$

behavior

response:  $x \mapsto x^h \stackrel{\Delta}{=} \Delta_h(x)$ 





- **2. do:** modify features (at cost)
- **3. know:** h (and cost function)

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ 

test:

$$h(\mathbf{x}) = \hat{\mathbf{y}} \approx \mathbf{y}$$





 $rational \Rightarrow most \ cost-effective$ 

 $\Rightarrow$  move <u>on</u> decision boundary

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ test:  $h(\Delta_h(x)) = \hat{y} \not\approx y$  fresponse:  $\Delta_h(x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$ 



goal: learning that is robust to strategic "gaming" behavior

train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ test:  $h(\Delta_h(x)) = \hat{y} \not\approx y$  $\bigwedge_{h} (x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$ 

#### **Goodhart's law:**

"If a measure becomes the public's goal,

it is no longer a good measure."



train:  $\underset{h}{\operatorname{argmin}} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$ test:  $h(\Delta_h(x)) = \hat{y} \not\approx y$  $\bigwedge_{h} (x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$ 

#### > Common examples:













**Holy grail**: a realistically practical, well-understood, plug-n-play framework for strategic learning

SC is great, by frustrating

#### Culprit – lots (and <u>lots</u>) of assumptions:

- outcomes are binary
- users always want positive outcomes
- costs are fixed, uniform, and known to all
- classifier is made public
- modifying x does not affect y
- changes to x are real (no mis-reporting)
- user actions = modify features
- users are rational (best-respond)
- users respond independently
- input data are `clean' (=unmodified)
- playing order is fixed

....

- only single playing round
- system cares only for accuracy
- ongoing community effort to relax, extend, scrutinize, and generalize

train:
$$\operatorname{argmin} \mathbb{E}[\mathbb{1}\{y \neq h(x)\}]$$
  
hh $discrepant$   
 $discrepant$ test: $h(\Delta_h(x)) = \hat{y} \approx y$ 

response: 
$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$$

### standard setup has

lots (and lots) of assumptions: (implicit/explicit)

- modifying x does not affect y
- outcomes are binary
- input data are `clean' (=unmodified)
- changes to x are real (no mis-reporting)
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train:argmin 
$$\mathbb{E}[\mathbb{1}\{y \neq h(\Delta_h(x))\}]$$
hconsistenttest: $h(\Delta_h(x)) = \hat{y} \approx y$ 

**response:** 
$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$$

#### key point:

**far from trivial!** minor change  $\Rightarrow$  major implications

## standard setup has lots (and lots) of assumptions: (in

- modifying x does not affect y
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ongoing community effort to relax, extend, scrutinize, and generalize

#### strategic

#### classification as a Stackelberg game: [HMPW'16]

Players: [1<sup>st</sup>] Learner [2<sup>nd</sup>] Users (dist.)

➤ Actions: classifier h modify  $x \mapsto x^h$ 

> Payoffs:  $\mathbb{E}[\mathbb{1}\{h(x^h) = y\}] \mathbb{E}[\mathbb{1}\{h(x^h) = 1\}]$ 

• Best response: 
$$x^h = \Delta_h(x) = \operatorname{argmax} h(x') - c(x, x')$$



- Solve equilibrium ⇔ solve learning
- Holds in idealized setting; trickier as becomes more realistic (finite data, partial information, weaker assumptions, ...)
- **Still**: SC = fundamental ML task + basic economic questions

play order is **crucial modeling choice** – choose with care! [NGTR'21, [ZMSJ'21]

#### strategic classification as an interface between machine learning and game theory:



revisit old questions + tackle new ones



# Learning aspects

of strategic classification
optimization generalization ML SC loss functions regularization model selection tobustness uncertainty *learning objective:* 

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\widetilde{\Delta}_{h}(x_{i})\right)\right)$$

s.t.  $\Delta_h(x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$ 

nasty nested min-argmax problem!

**ask**: how to optimize objective?



 $\underset{h}{\operatorname{argmin}} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_i, h\left(\widetilde{\Delta}_h(x_i)\right)\right)$ 

s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is *differentiable* 

ask: how to optimize objective?

optimization generalization Ioss functions regularization model selection robustness uncertainty

**ask**: how to optimize objective?

*learning objective:* 

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\widetilde{\Delta}_{h}(x_{i})\right)\right)$$

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#### LR ICML21

optimization generalization loss functions regularization model selection tobustness uncertainty

**ask**: how to optimize objective?

*learning objective:* 



s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is *differentiable* 



#### LR ICML21





s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is *differentiable* 

- For common case where:  $h(x) = w^{\top}x$  $c(x, x') = ||x' - x||_2$  (or squared, or PSD)
- Admits simple closed-form solution:

$$\Delta_{w}(x) = \begin{cases} x & w^{\mathsf{T}}x \ge 0 \text{ or } \operatorname{dist}(x;w) > 2\\ \operatorname{proj}^{+}(x;w) & \operatorname{o.w.} \\ & = x - \min\left\{0, \frac{w^{\mathsf{T}}x + b}{\|w\|_{2}^{2}}\right\} \text{ differentiable!}$$
  
Just replace hard-if with soft-if (e.g., sigmoid) 
$$\mathsf{LR} \mathsf{ICML22}$$





$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\widetilde{\Delta}_{h}(x_{i})\right)\right)$$

s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is *differentiable* 

- Otherwise, when: •  $h(x) = w^{T}\phi(x) + \psi(x)$ (for some non-linear  $\phi, \psi$ ) •  $\Delta$  applies to  $z = \phi(x)$ 
  - $\succ$  *c* is convex (in *z*)
- Then can use **plato:** [LR ICML21]

implements  $\Delta$  as concave optimization layer [AABBDK'19]

Code: <u>https://plato.codes/</u>

#### e.g., if $\Delta$ is LP:







accuracy (concave in x, z) accuracy accuracy Benchmark SERM Blind

credit

varied costs:

Accuracy for various datasets and cost scales

fraud

spam

ö

fin. distress

s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is differentiable

- Otherwise, when:  $\succ$   $h(x) = w^{\top} \phi(x) + \psi(x)$ (for some non-linear  $\phi, \psi$ )
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• Code: <u>https://plato.codes/</u>



$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\widetilde{\Delta}_{h}(x_{i})\right)\right)$$

s.t.  $\widetilde{\Delta}_h(x) \approx \Delta_h(x)$  and is *differentiable* 

- Otherwise uncharted territory
- Idea: borrow methods from adversarial learning literature (e.g., FGSM [GSS'15] or PGD [MMSTV'18])
- Essentially, optimize objective by alternating between:
  - fixing features  $x^h$  and updating heta
  - fixing parameters  $\theta$  and updating  $x^h$
- Technically possible but hasn't been done yet in strategic learning
- $\blacktriangleright$  More on strategic  $\leftrightarrow$  adversarial connection to follow!



 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$ 



- **Q** will strategic behavior:
  - 1. increase overfitting?
  - *2. reduce* overfitting?
  - 3. make no difference?
- **Rephrase:** how does behavior affect sample complexity?

**ask**: how does behavior affect generalization?







Underfitting

Balanced

Overfitting

 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$ 



- SC = model-dependend distribution shift
- In typical distriubtion shift,  $p_{\rm test}$  is assumed to be "close" to  $p_{\rm train}$  (e.g., in ball)
- Contrarily, in strategic shift:
  - 1. only points in "band" before h move
  - 2. entire region moves <u>on</u> decision boundary
  - 3. moving region determined by choice of h





 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$ 



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 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$ 



- Generalization theory typically relies on discrepency measures  $d(p_{\text{train}}, p_{\text{test}})$  [MMR ICML09]
- ⇒ bounds are **shift** (and so **dsitribution**) **dependent**
- Interestingly, strategic shifts admit distribution-<u>in</u>dependent generalization bounds



 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$ 

# optimization generalization ML SC loss functions regularization model selection robustness uncertainty

- Induced class:  $H_{\Delta} = \{h(\Delta_h(x)) : h \in H\}$
- Strategic VC:  $SVC(H) = VC(H_{\Delta})$
- **Result**: for standard setting, recover non-strategic bounds (almost!)
- But **cost form matters!** [SVXY'23] show:
  - instance-invariant costs:
     c(x x') ⇒ SVC ≈ VC (for linear h)
     i.e., learning is not harder
  - instance-wise costs: =individualized
     c<sub>x</sub>(x') ⇒ unlearnable! (in the worst case)
     i.e., learning is impossible

#### instance-invariant:



#### instance-wise:



 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$ 



• Also: regret analys for online strategic classification



standard hinge:  $\max\{0, 1 - yw^{\mathsf{T}}x\}$ 





**ask**: can we just use conventional proxies?

# max-margin classifier

- selection criterion
- good generalization

LR ICML22

- tractable



#### max-margin classifier

- selection criterion
- good generalization



#### naive max-margin classifier

- vacous criterion
- unclear if generalizes



#### strategic max-margin classifier

- regain selection criterion
- comparable generalization

LR ICML22

- reasonably tractable



#### strategic max-margin classifier

# conclusion: strategic robustness requires rethinking fundamental learning concepts

- regain selection criterion
- comparable generalization

LR ICML22

- reasonably tractable





# Economic aspects

of strategic classification

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \ \frac{h(x')}{h(x')} - c(x, x')$$



$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \underbrace{u(x') - c(x, x')}_{= \begin{cases} +1 & \hat{y} = +1 \\ -1 & \hat{y} = -1 \end{cases}}$$



$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \begin{array}{c} u(x') - c(x, x') \\ & & \downarrow \end{array} = \begin{cases} +1 & \hat{y} = +1 \\ -1 & \hat{y} = -1 \end{cases}$$

#### generalized SC:

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \frac{u(x')}{u(x')} - c(x, x')$$

1. arbitrary **utility function** 



LR, ICML22

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \begin{array}{c} u(x') - c(x, x') \\ & \\ \end{array} = \begin{cases} +1 & \hat{y} = +1 \\ -1 & \hat{y} = -1 \end{cases}$$

#### generalized SC:

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \frac{u(x';z)}{u(x';z)} - c(x,x')$$

- 1. arbitrary **utility function**
- 2. can depend on **private information**



LR, ICML22

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \begin{array}{c} u(x') - c(x, x') \\ & \\ \end{array} \rightarrow = \begin{cases} +1 & \hat{y} = +1 \\ -1 & \hat{y} = -1 \end{cases}$$

#### generalized SC:

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \frac{\tilde{u}(x';z)}{\tilde{u}(x';z)} - c(x,x')$$

- 1. arbitrary utility function
- 2. can depend on **private information**
- 3. act on **perceived utility** (*≠* true utility)



LR, ICML22

#### generalized SC:

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \ \tilde{u}(x';z) - c(x,x')$$

- **Q**: how to learn?
- A: generalize strategic margins and hinge!

## standard hinge:

 $\max\{0, 1 - yw^{\mathsf{T}}x\}$ =  $\max\{0, 1 - \operatorname{sign}(yw^{\mathsf{T}}x)|w^{\mathsf{T}}x|\}$ correctness distance

➤ naïve hinge:

 $\max\{0,1-\operatorname{sign}(yw^{\mathsf{T}}\Delta_{h}(x,z))|w^{\mathsf{T}}\Delta_{h}(x,z)|\}$ 

generalized strategic hinge: (gs-hinge)

 $\max\{0, 1 - \operatorname{sign}(yw^{\mathsf{T}}\Delta_h(x, z))d_{\Delta}(x, z; w)\}$ 



#### generalized SC:

$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \ \tilde{u}(x';z) - c(x,x')$$

## reinterpretation of "margin":



 admits convenient tractable form for several known special cases

> generalized strategic hinge: (gs-hinge)  $\max\{0, 1 - \operatorname{sign}(yw^{\mathsf{T}}\Delta_{h}(x, z))d_{\Delta}(x, z; w)\}$ 



L**R**, ICML22

#### classification *about* humans



system wants: correct predictions
users want: positive predictions



#### incentive-aligned:



**ask**: can learning (implicitly) coordinate cooperation?

#### classification *for* humans (as a *service*)



system wants: correct predictions
users want: correct predictions

#### incentive-aligned:

#### classification *for* humans (as a *service*)



system wants: correct predictions users want: correct predictions



#### incentive-aligned:

#### classification *for* humans (as a *service*)



system wants: correct predictions users want: correct predictions



actions

strategically linearly separable
#### incentive-aligned:

#### classification *for* humans (as a *service*)



system wants: correct predictions users want: correct predictions





# classification *against* humans (?)



system wants: correct predictions
users want: wrong predictions



**ask**: can strategic modeling help make adversarial training *less conservative*?







#### A note on strategic vs. adversarial learning:

- From SC perspective, adversarial is "special case"
- But only in a narrow sense many distinctions in practice
- E.g., in adversarial learning (vs. strategic learning):
  - attack proxy loss (e.g. log-loss) vs. 0-1
  - focus on non-linear models
  - focus on complex modalities (e.g. images) -
  - $\Rightarrow$  best-responses are approximate
  - vulnerabilities mostly in latent space
  - maximize utility under budget constraints
  - $\Rightarrow$  features always modified and to the max
  - $\Rightarrow$  optimize minimax objective

much potential for synergy! will return to this



- vs. modify minimally and only if needed
- vs. nested min-argmax

















#### GNETR ICML21

# **SCHUFA**













- Price of OPacity: (POP)
  - $err(h, \hat{h}) err(h, h)$
- Main result: can be arbitrarily bad
   ⇒ transparency is often in best interest of system!





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  - $err(h, \hat{h}) err(h, h)$
- Main result: can be arbitrarily bad
   ⇒ transparency is often in best interest of system!









$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$$

$$uncertainty$$

$$unknown user response:$$

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{?}(x_{i})\right)\right)$$



# ask: how can learning contend

with uncertain user behavior?

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$$
  
uncertainty  
$$\operatorname{unknown} \operatorname{user} \operatorname{response:}_{h} \int_{m}^{m} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{?}(x_{i}))\right)$$

1) infer  $\Delta$  over time (more on this later)



**ask**: how can learning contend with uncertain user behavior?

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$$
*uncertainty unknown user response:*

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{i}(x_{i})\right)\right)$$

### 1) infer $\Delta$ over time (more on this later)







**ask**: how can learning contend with uncertain user behavior?

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$$
*uncertainty unknown user response:*

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{i}(x_{i})\right)\right)$$

### 1) infer $\Delta$ over time (more on this later)







**ask**: how can learning contend with uncertain user behavior?

 $\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{l} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$ 

unknown user response:

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{?}(x_{i})\right)\right)$$

(public) policy problems:



1) infer  $\Delta$  over time (more on this later)

2) *robust learning* – *unkonwn costs:* 

$$\underset{h}{\operatorname{argmin}} \max_{c \in C} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}^{c}(x_{i})\right)\right)$$
$$\underbrace{uncertainty set}$$

- "One shot" can deploy only once
- **Goal**: learn to be doubly-robust:
  - vs. strategic behavior
  - vs. worst-case cost  $c \in C$
- Hardness: not knowing *c* can be catastrophic
- Convexification: updated ad-hoc s-hinge
- Algorithm: effective, converge to opt. min-max







- Robustness via penalizing deserving sub-population
- Main result is negative: increased accuracy ⇒ increased social burden
- However, results apply to certain monotone setting
- In more general settings, there is reason for optimism!

**ask**: when and how can we reduce social harm?



= "social burden" [MMDH'19]

$$\operatorname{burden}(h) = \mathbb{E}[\min_{x':h(x')=1} c(x, x') \mid y = 1]$$



#### LR ICML21

- **Conjecture**: many good models, vary in burden
- Learning objective underspecified can exploit!
- Regularize for **generalization**:







- **Conjecture**: many good models, vary in induced burden
- Learning objective underspecified **can exploit!**
- Regularize for **sparsity**:





- **Conjecture**: many good models, vary in induced burden
- Learning objective underspecified **can exploit!**
- Regularize for... **social good?**







- **Conjecture**: many good models, vary in induced burden
- Learning objective underspecified can exploit!
- Regularize for... social good?





LR ICML21

- **Conjecture**: many good models, vary in induced burden
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- **Conjecture**: many good models, vary in induced burden
- Learning objective underspecified **can exploit!**
- Regularize for... **social good!**





**\_R** ICML21

- Applies to other social good metrics (utility, recourse, ...)
- Similarly underspecified similar pareto fronts!







$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} \begin{array}{l} h(x') - c(x, x') \\ utility \end{array} \quad cost$$

## ask: where do costs come from?

(ask first: what are features?)







Market Stall



Market Stall








**ask**: can learning anticipate and account for the markets it induces?

#### strategic *modification*:

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h(\Delta_{h}(x_{i}))\right)$$

s.t. 
$$\Delta_h(x) = \underset{x'}{\operatorname{argmax}} h(x') - c(x, x')$$





ask: what other actions can users take?

#### strategic *modification*:

$$\operatorname{argmin}_{h} \frac{1}{m} \sum_{i=1}^{m} \ell\left(y_{i}, h\left(\Delta_{h}(x_{i})\right)\right)$$

#### strategic *participation*:



s.t. 
$$a_h(x) = 1$$
{worthwhile to apply}







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HSKR ICML24

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s.t.  $a_h(x) = \mathbb{1}$ {worthwhile to apply}







ask: what other actions can users take?

HSKR ICML24

#### strategic participation:



test

y = 1y = 0

(interview, trial period, ...)



#### strategic participation:







#### **ask**: how does learning affect applications?



• **Observation:** learning rule determines **self-selection** 





main result: learning has capacity
to fully determine applications!

#### strategic participation:



- **Observation:** learning rule determines **self-selection**
- Implications: can create *false appearance* of fairness,

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# **† †**



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ask: how does learning affect applications?

# Beyond

the standard setup





revisit old fronts + tackle new ones!



revisit old fronts + tackle new ones!

# 1) Causality

vanilla SC

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	credit card <b>\$7,289</b>	LAST T ▲ \$20	RANSACTIONS 0.00 ▼-\$428.56	>

superficial changes  $\Rightarrow$  gaming









# 1) Causality

- **Standard SC:** changing *x* does <u>not</u> affect *y* (=gaming)
- More realistic: changing x can also change y
- Assume exists underlying *causal graph* [Pearl 2009]:

**ask**: can we learn in causal strategic settings?



(taken from Miller et al. 2020)

#### • Lots of challenges:

- graph not necessarily known
- key variables not necessarily observed (e.g., confounders)
- > structure determines interactions (i.e., what affects what)
- Causal SC is inherently difficult as hard as causal inference [MMH ICML20]

## Causal SC as distribution shift

- **Q1**: How does causality affect learning?
- Simplifying assumption: causal vs. correlative features
- A1: Entails different types of distribution shift:
  - correlative  $\rightarrow$  *strategic* shift  $\rightarrow$  gaming
  - only causal  $\rightarrow$  *covariate* shift  $\rightarrow$  missinformation
  - both  $\rightarrow$  *mixture* shift  $\rightarrow$  interactions
- Corollary: choose your battles!



h



 $x_{\rm corr}$ 

### Incentivizing improvement

- Q1: How does causality affect learning?
- Q2: How does causality affect social outcomes?
- A2: Causal SC has potential for improvement:

### $\mathbb{E}_{x}\left[\mathbb{E}[p(y \mid do(\Delta)) - p(y) \mid x]\right]$

- Goal: learn h that (also) promotes improvement
- Has long and rich history in economics (e.g., see [KR 19])
- Also considered in (online) SC (e.g., [SEA'20, BLWZ'21, CWL'21, HNSHW'22, MDW'22])



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- But changing x can also **impair** outcomes!
- Solution: learn safe models by "looking ahead"

causal effect:



#### uncertainty:



RHRP NeurIPS20

- Standard SC: responses are <u>independent</u> ( $\Delta_f(x)$  depends only on x) find
- More realistic: responses are interdependent
- Reason #1: limited resources
  - Actually, all common examples have limit on # of  $\hat{y} = 1$
  - This means that users **compete**



limited teaching capacity



limited qualified personell



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- More realistic: responses are interdependent
- Reason #1: limited resources
  - Actually, all common examples have limit on # of  $\hat{y} = 1$
  - This means that users compete
  - Reasonable approach:

learn to rank, then set  $\hat{y} = 1$  only for top-k

- Turns out to be *exceedingly hard* [LGB ICML22]
- Still major goal!



- Standard SC: responses are independent
- More realistic: responses are interdependent
- Reason #1: limited resources
- **Reason #2:** model-induced dependencies





graph-dep. embedding

social network



GNN

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- More realistic: responses are interdependent
- **Reason #1:** limited resources
- **Reason #2:** model-induced dependencies
- **Reason #3:** economic graph structure





strategic content creators

main result: can use graph to incentiveize diversity

### 3) Learning over time

- **Standard SC:** batch setting: train → deploy → test
- Assumes access to clean data (otherwise, chicken & egg!)
- More realistic: data is dirty (i.e., result of some behavior)
- **One solution:** iterated deployments over time: train  $\rightarrow$  deploy  $\rightarrow$  train  $\rightarrow$  deploy  $\rightarrow$  train  $\rightarrow$  ...
- Three main aproaches:  $\rightarrow$  lots of research; will present here only in brief
  - online learning (e.g., bandits) (e.g., [DRSWW NeurIPS17, CSSVZ ICML23, HPW NeurIPS23, SBM NeurIPS23, ABBN EC21, ...])
  - 2. performative prediction (retraining revisited) [PZMH ICML20]
  - 3. dynamical systems

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- One solution: iterated deployments over time: train  $\rightarrow$  deploy  $\rightarrow$  train  $\rightarrow$  deploy  $\rightarrow$  train  $\rightarrow$  ...
- **Pros**: less restrictive
  - (1) does <u>not</u> require clean data
  - (2) does not assume known  $\Delta_h$  (or even best-response)
  - (3) permits causal  $\Delta_h$  (under additional assumptions)
- Cons: each deployment is social "experiment"
  - in some cases, exploration is reasonable
  - in other cases it is very much <u>not</u>

# Opportunities & challenges

open questions

- Strategic learning is exiting new field with much potential for growth
- But it is also young so that many challenges still lie ahead:
- **1. Learning aspects**:



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- But it is also young so that many challenges still lie ahead:
- **1. Learning aspects**:
  - labels beyond binary
    - regression
    - multiclass
    - multilabel
    - sequences
    - structured (e.g., graphs)





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### **1. Learning aspects**:

- labels beyond binary
- inputs beyond vectors
  - images
  - text
  - graphs
  - ...



- Strategic learning is exiting new field with much potential for growth
- But it is also young so that many challenges still lie ahead:

### **1. Learning aspects**:

- labels beyond binary
- inputs beyond vectors
- models beyond linear
  - neural nets (behavior in latent space)
  - tree-based
  - text-based (prompts)
  - ...



- Strategic learning is exiting new field with much potential for growth
- But it is also young so that many challenges still lie ahead:

### **1. Learning aspects**:

- labels beyond binary
- inputs beyond vectors
- models beyond linear
- settings beyond classification
  - unsupervised and semi-supervised
  - generative
  - RL and MARL

- ...



- Strategic learning is exiting new field with much potential for growth
- But it is also young so that many challenges still lie ahead:
- **1. Learning aspects**
- 2. Econ/GT aspects:
  - information
    - power
    - control
    - selective release/withold
    - ...


### Open questions

- Strategic learning is exiting new field with much potential for growth
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- **1. Learning aspects**
- 2. Econ/GT aspects:
  - information

- ...

- other economic settings
  - markets, auctions, contracts, ...
  - competition (between classifiers)
  - cooperation (between users)
  - monopolistic behavior



### Open questions

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1.	Learning aspects			cor	firmatio	n bias
2.	<ul> <li>Econ/GT aspects:</li> <li>information</li> <li>other economic settings</li> <li>behavior <ul> <li>Bayesian</li> <li>non-rational "behavioral" (=biase</li> <li></li> </ul> </li> </ul>	future discounting		decoy e	causal fallacy coy effect primacy/recency g endowment effect oice overload availability bias	
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### Open questions

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- But it is also young so that many challenges still lie ahead:
- **1. Learning aspects**
- 2. Econ/GT aspects
- 3. "In the wild":
  - evaluation [BBK 20, HHP 23, CIALRM 23]
  - measuring utility/welfare
  - estimating costs
  - monitoring and regulation

### Why supervised learning?

- Most human-centric tasks are policy problems (vs. prediction problems)
- So supervised learning is clearly the wrong tool to use
- But it is also by far the most prevelant, accessible, and easy to use
- Vision for the future:

- Goal: make integrating human agency as seemless as possible
- Not so easy! And requires much caution and deliberation (c.f. fairness)

# Summary

### Summary

- SC captures natural tension between learning systems and their users
- Appealing interface between ML and GT many open question!
- Original setup is clean and simple, but likely to narrow
- Nonetheless, flexible and modular: easy to extend, relax, and generalize

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- SC captures natural tension between learning systems and their users
- Appealing interface between ML and GT many open question!
- Original setup is clean and simple, but likely to narrow
- Nonetheless, flexible and modular: easy to extend, relax, and generalize
- > A call to rethink the design of learning algorithms for social settings
- > An opportunity to revise foundations using economic and behavioral modeling
- High potential for real impact much more work needed!



• "users game system"



- "users game system"
- "system exploits users"





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- "system exploits users unintentionally"





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#### Recommended for you:





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. . .

**Robert J. Shiller** Winne - of the Nobe leconomics **How Stories Go** Viral & Drive Major Economic Events





