

# Model-Based Minimum Bayes-Risk Decoding for Text Generation

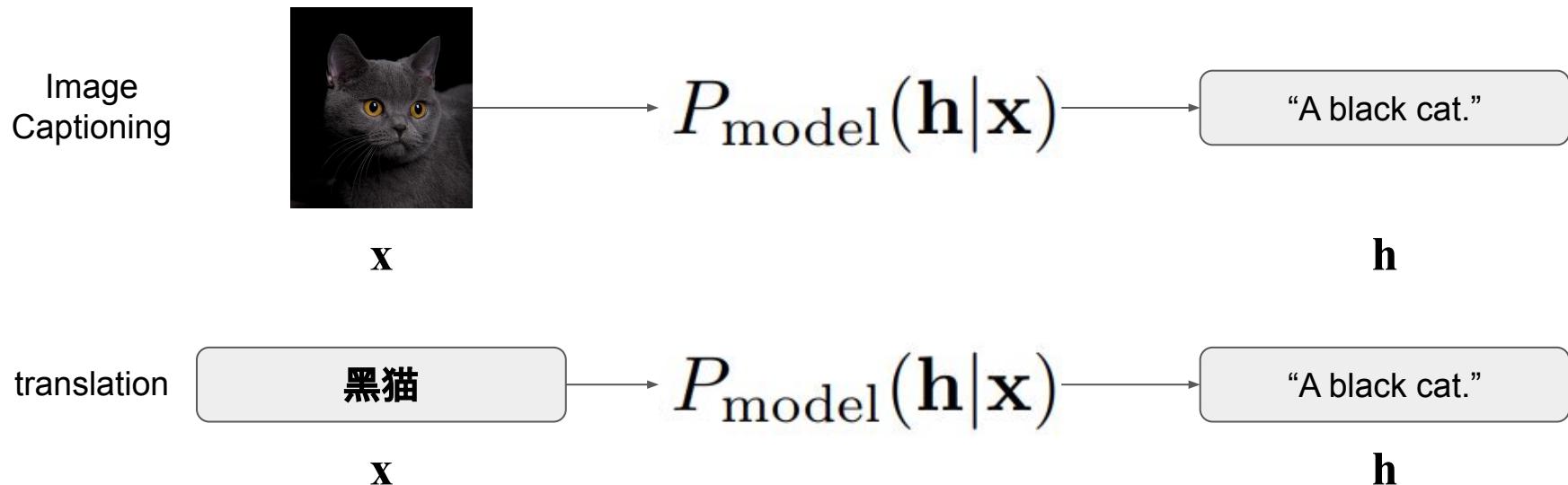
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Kaito Ariu, Kenshi Abe



CyberAgent AI Lab

## Text generation problem

Many NLP tasks involve text generation



## Beam search decoding

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Beam search selects the text that maximizes the model probability  
(Maximum a-posteriori estimate)

$$\mathbf{h}^{\text{MAP}} = \arg \max_{\mathbf{h} \in \mathcal{Y}} P_{\text{model}}(\mathbf{h} | \mathbf{x})$$

**$\mathbf{x}$**  Input  
 **$\mathcal{Y}$**  All possible outputs  
 **$\mathbf{h}$**  Candidate output

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However, **sequences with the highest model probability is often a bad sequence** (Ott+18, Stahlbert+19)

## Minimum Bayes Risk (MBR) Decoding (Kumar+ '04, Eikema+ '20)

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**The goal is to maximize the quality of the text**

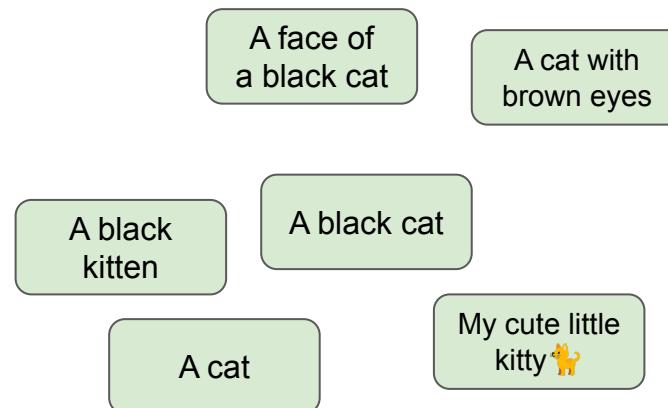
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Prompt: “What’s in picture?”



$$P_{\text{model}}(\mathbf{h}|\mathbf{x}) \longrightarrow$$



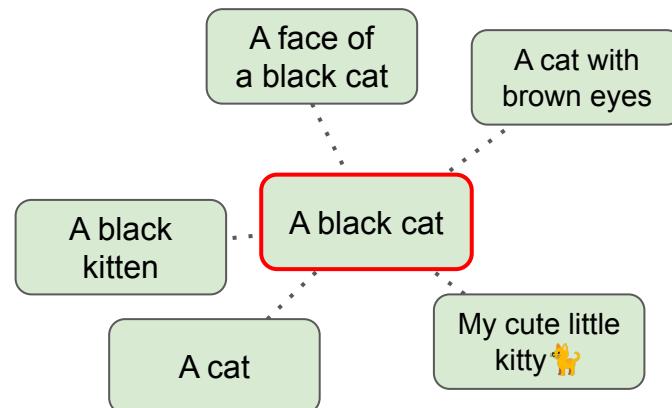
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Estimate the “similarity” between the samples with  $u(\mathbf{h}, \mathbf{y})$

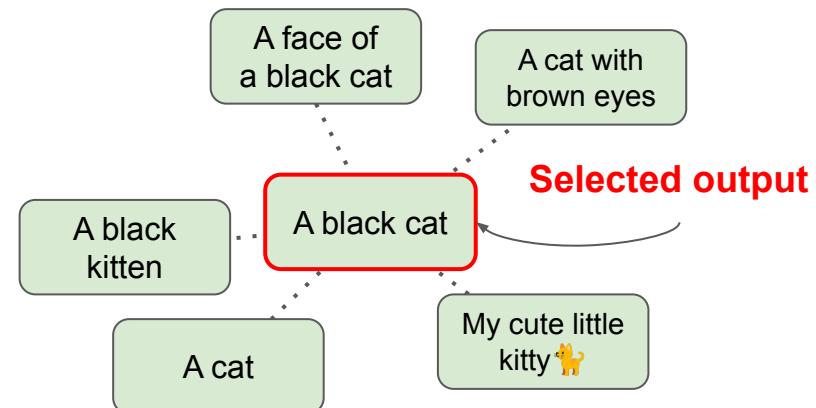
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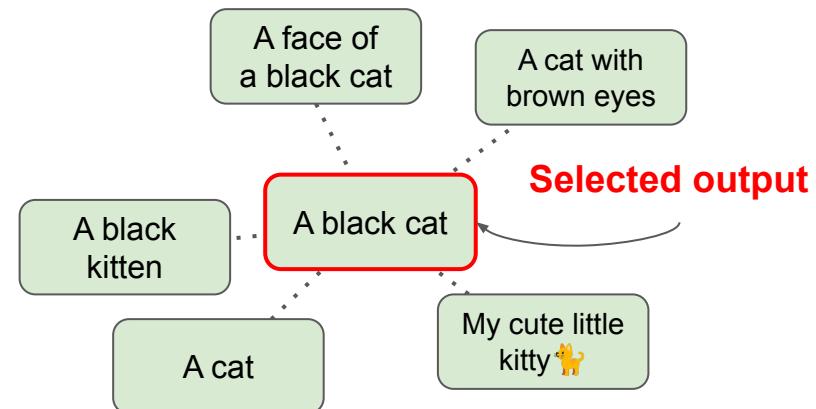
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## Problem: MBR needs a lot of samples

Selecting the center point accurately requires a lot of samples



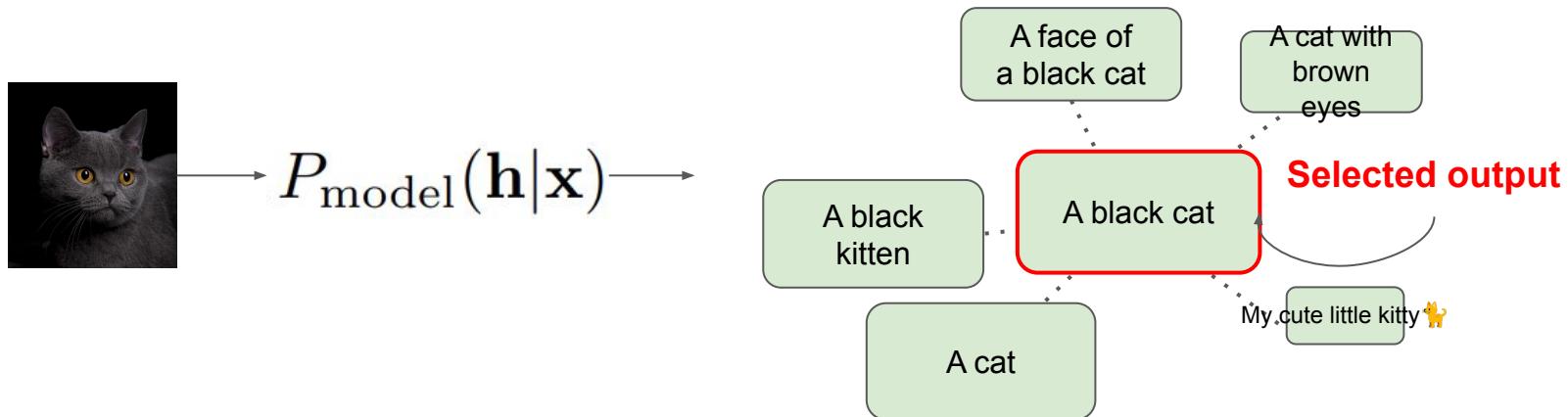
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## Problem: MBR needs a lot of samples

**Selecting the center point accurately requires a lot of samples**

→ Weight the samples according to its generation probability

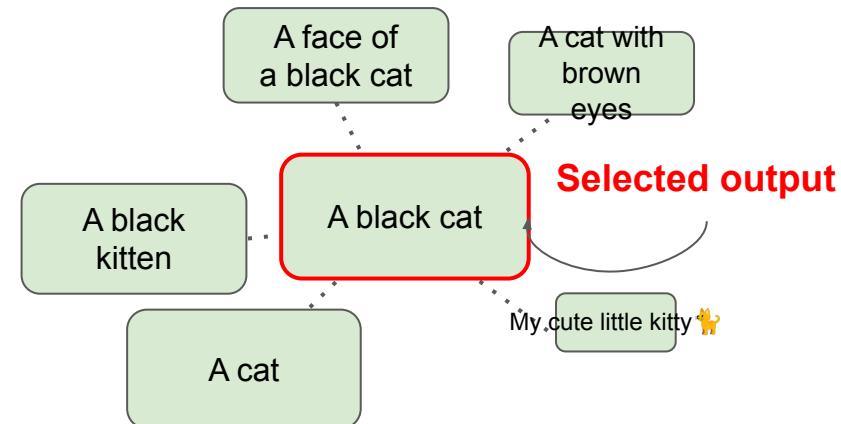


Estimate the “similarity” between the samples with  $u(\mathbf{h}, \mathbf{y})$

## Q. Wouldn't it increase the estimation error?

**No!** We can weight the samples without increasing the estimation error in expectation

1. Remove duplicated samples
2. Weight samples by  $P_{\text{model}}(\mathbf{h}|\mathbf{x})$



# Model-Based Minimum Bayes Risk (MBMBR) Decoding

## MBR Decoding (prior work)

$$\mathbf{h}^{\text{MC}} = \arg \max_{\mathbf{h} \in \mathcal{H}_{\text{cand}}} \sum_{\mathbf{y} \in \mathcal{H}_{\text{ref}}} u(\mathbf{h}, \mathbf{y}) \cdot \hat{P}_{\text{model}}(\mathbf{y})$$

Monte-Carlo estimate

## MBMBR Decoding (new!)

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Model-based estimate

## Example of MBMBR

Sampled Texts		Target	Monte Carlo Estimate	Model-Based Estimate
Text	#Occurrences	$P$	$\hat{P}$	$\hat{P}_{\text{MB}}$
<i>But telling the truth is not a crime.</i>	2	0.3	0.4	0.6
<i>However, telling the truth is not a crime.</i>	2	0.1	0.4	0.2
<i>But to tell the truth is not a crime.</i>	1	0.1	0.2	0.2
(All others)	0	0.5	0	0
$D_{\text{KL}}(\cdot    P)$		0	0.808	<b>0.693</b>

### Monte Carlo estimate (prior work)

$$\mathbf{h}^{\text{MC}} = \arg \max_{\mathbf{h} \in \mathcal{H}_{\text{cand}}} \sum_{\mathbf{y} \in \mathcal{H}_{\text{ref}}} u(\mathbf{h}, \mathbf{y}) \cdot \hat{P}_{\text{model}}(\mathbf{y})$$

### Model-based estimate (new!)

$$\mathbf{h}^{\text{MB}} = \arg \max_{\mathbf{h} \in \mathcal{H}_{\text{cand}}} \sum_{\mathbf{y} \in \mathcal{H}_{\text{ref}}} u(\mathbf{h}, \mathbf{y}) \cdot P_{\text{model}}(\mathbf{y})$$

# Error(Model-based estimate) $\leq$ Error(Monte Carlo estimate)

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## Theorem (informal)

**Model-based estimate is guaranteed to be closer to the true model probability than Monte Carlo estimate measured by KL-divergence.**

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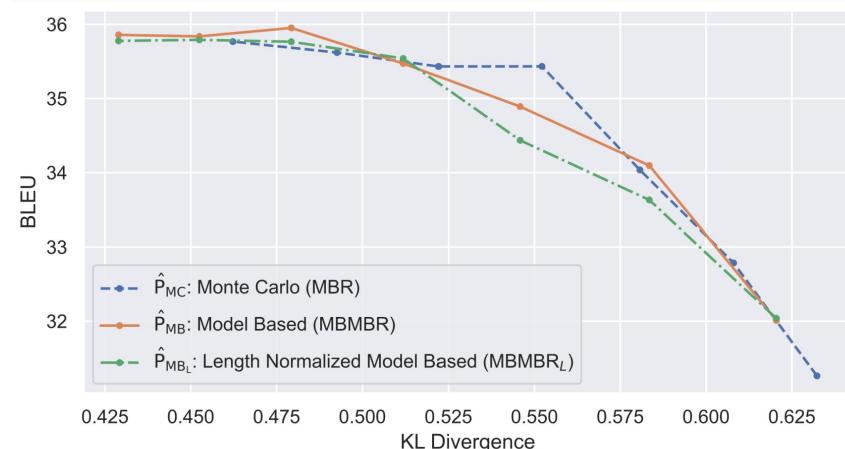
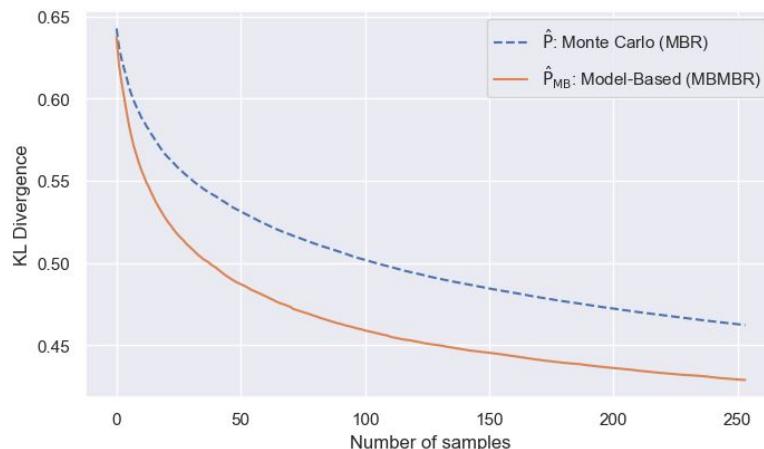
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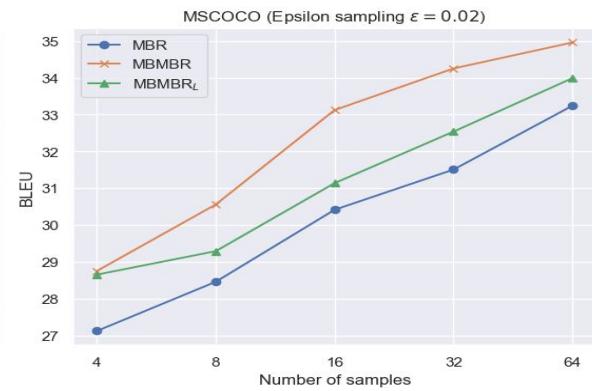
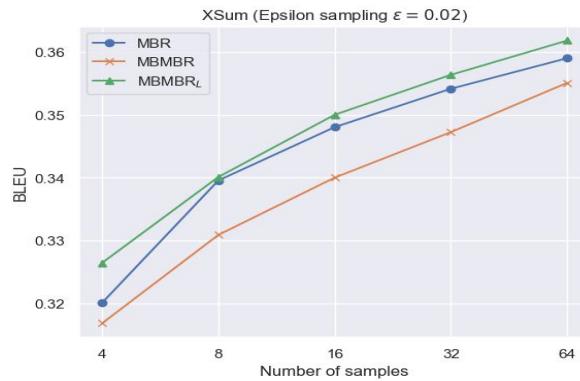
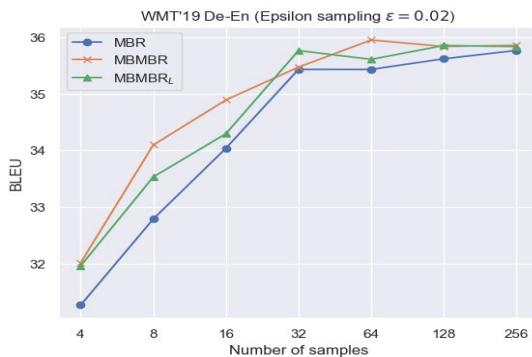
**Model-based estimate is guaranteed to be closer to the true model probability than Monte Carlo estimate measured by KL-divergence.**

## Accuracy of the probability estimate matters

Divergence from the model probability **correlates with the text quality**



# Experimental Evaluation



Machine  
translation  
(WMT19 De-En)

Text  
summarization  
(XSum)

Image  
captioning  
(MS COCO)

## Summary

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- MBMBR uses the model probability instead of Monte Carlo estimate
- MBMBR improves the estimation of the model probability which leads to improved text quality
- Experiments show that MBMBR is effective in machine translation, text summarization, and image captioning
- Implemented in mbrs (Deguchi, 2024) (pip install mbrs)

### Monte Carlo estimate (prior work)

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