# Robust Subtask Learning for Compositional Generalization

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# Motivating Example

- Three subtasks: LEFT, RIGHT and UP
- > Each exit leads to a new room
- Example task: LEFT -> RIGHT-> UP-> RIGHT



### Subtask

- Subtask  $\sigma = (R, F, T)$
- $\succ \text{ Reward function } R: S \times A \times S \rightarrow \mathbb{R}$
- $\succ$  Final states  $F \subseteq S$
- → Jump transition  $T: S \times F \rightarrow [0,1]$

T(s'|s) is the probability of jumping to s' upon reaching final state s.



## Subtask

- Subtask  $\sigma = (R, F, T)$
- $\succ$  F<sub>left</sub> = Blue region

$$R_{\sigma}(s, a, s') = -\|s' - c_{\sigma}\|_{2} + B \cdot \mathbb{1}(s' \in F_{\sigma})$$



#### Task

- > Task  $\tau = \sigma_0 \sigma_1$  ... is an infinite sequence of subtasks
- $\succ$  Upon completion of subtask  $\sigma_i$  system switches to next subtask  $\sigma_{i+1}$
- → Want to learn policies  $\Pi = {\pi_{\sigma} \mid \sigma \in \Sigma}$  to maximize

$$J(\Pi) = \inf_{\tau \in \mathcal{T}} \mathbb{E}_{\rho \sim \mathcal{D}_{\tau}^{\Pi}} \Big[ \sum_{t=0}^{\infty} \gamma^{t} R_{\tau[i_{t}]}(s_{t}, \pi_{\tau[i_{t}]}(s_{t})) \Big]$$
  
Min-max objective: Worst case performance over tasks



- One copy of S for each subtask
- Player 1 chooses actions from A in
- Player 2 chooses subtask from Σ in space of chosen subtask

states – leads to normal system transitions

states – leads to a jump transition into state

# Solving the game

- > Two value iteration algorithms to compute V\* in the known model case
- > A Q-learning algorithm that **converges in the limit** for finite states
- > An SAC based algorithm for infinite state/action spaces
- > An asynchronous algorithm for **learning options in parallel**

# Experiments





(a) F1/10th Car

Right Left Straight Sharp Left Sharp Right An example track

(b) Segment Types

Rooms environment

F1/10th environment

## Experiments



Figure 3: Plots for the Rooms environment. x-axis denotes the number of sample steps and y-axis denotes the either the average number of subtasks completed or the probability of completing 5 subtasks. Results are averaged over 10 runs. Error bars indicate  $\pm$  standard deviation.





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