

# Score-Guided Intermediate Layer Optimization: Fast Langevin Mixing for Inverse Problems

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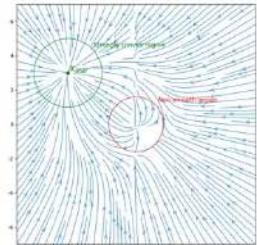
(\*): equal contribution

## Contributions of our work

- ▷ Solve inverse problems with extremely sparse measurements



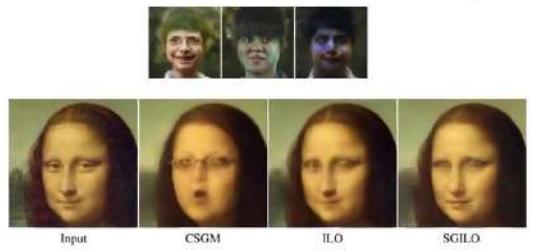
- ▷ Convergence of Langevin for Inverse Problems with generative models



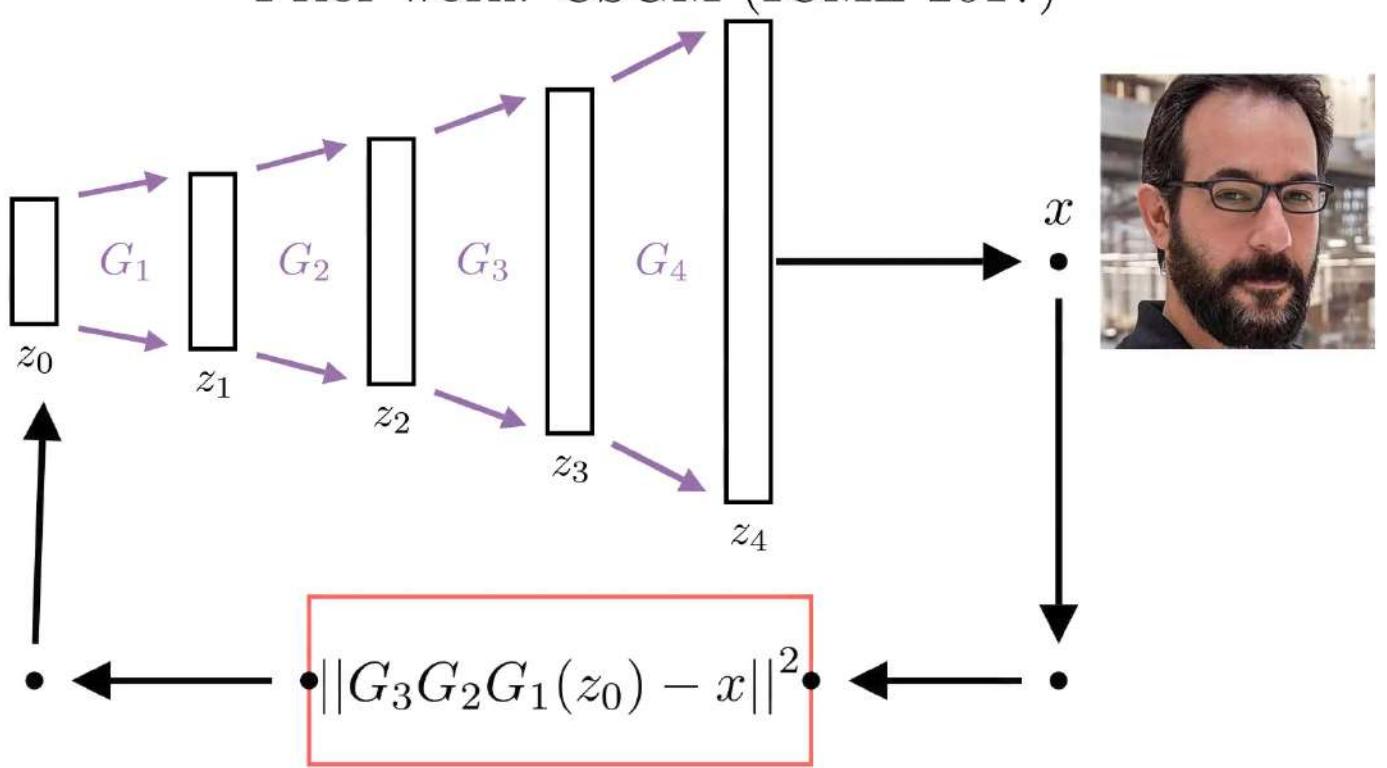
- ▷ Posterior sampling with GANs



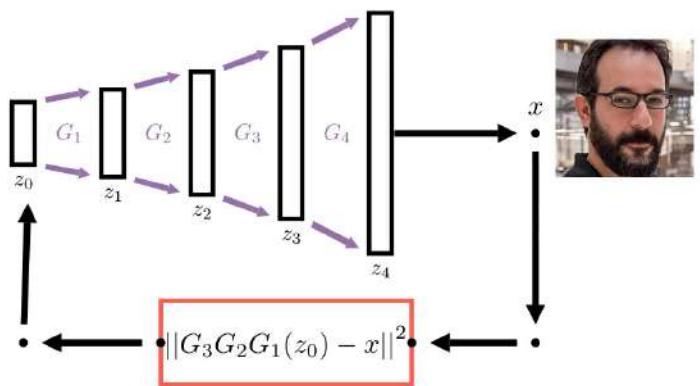
- ▷ GANs + Diffusion = ❤ for inverse problems



Prior work: CSGM (ICML 2017)

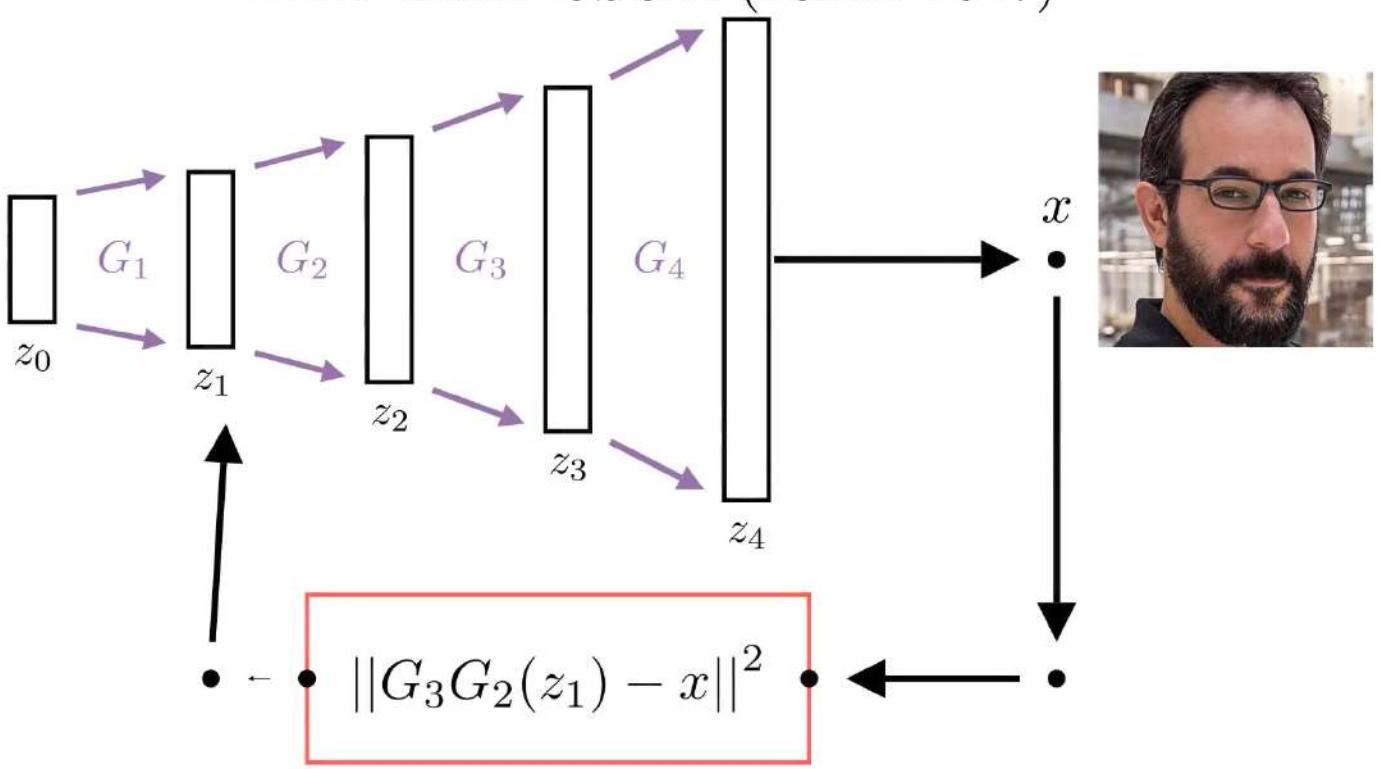


Prior work: CSGM (ICML 2017)

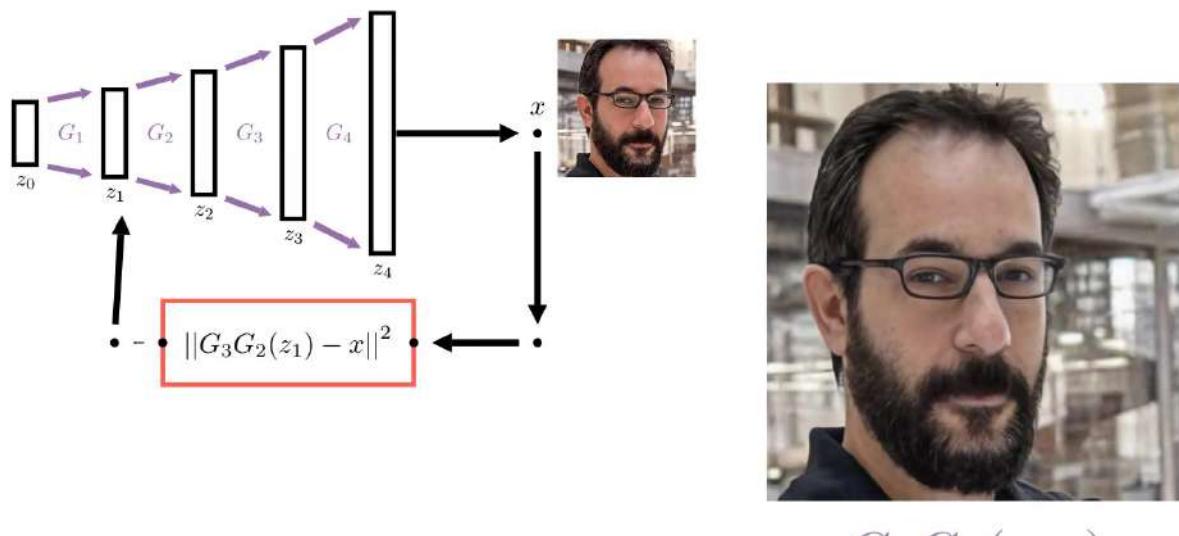


$$G(z_0*)$$

Prior work: CSGM (ICML 2017)



Prior work: CSGM (ICML 2017)



$$G_3G_2(z_1*)$$

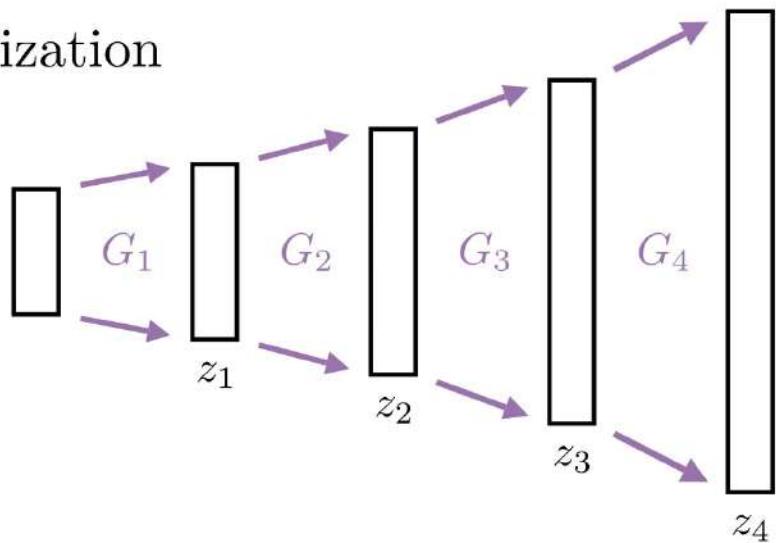
## The need of regularization



Input image

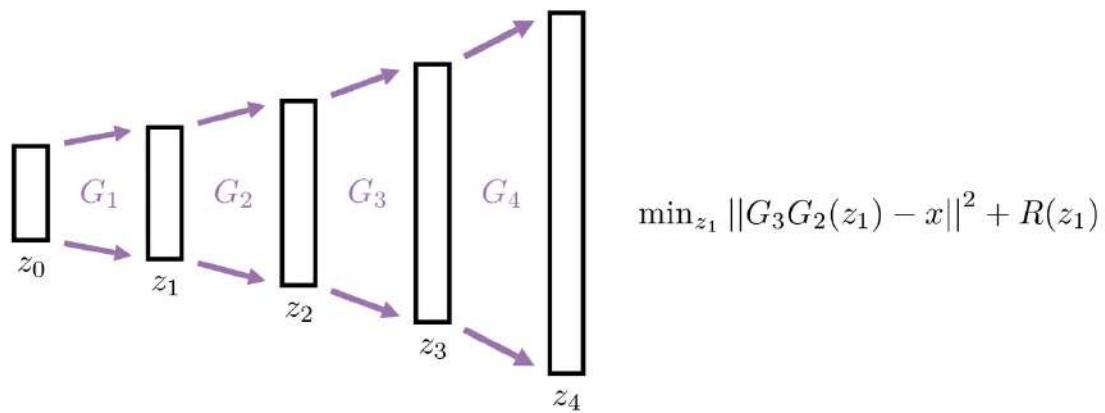
Intermediate Layer Optimization

## The need of regularization



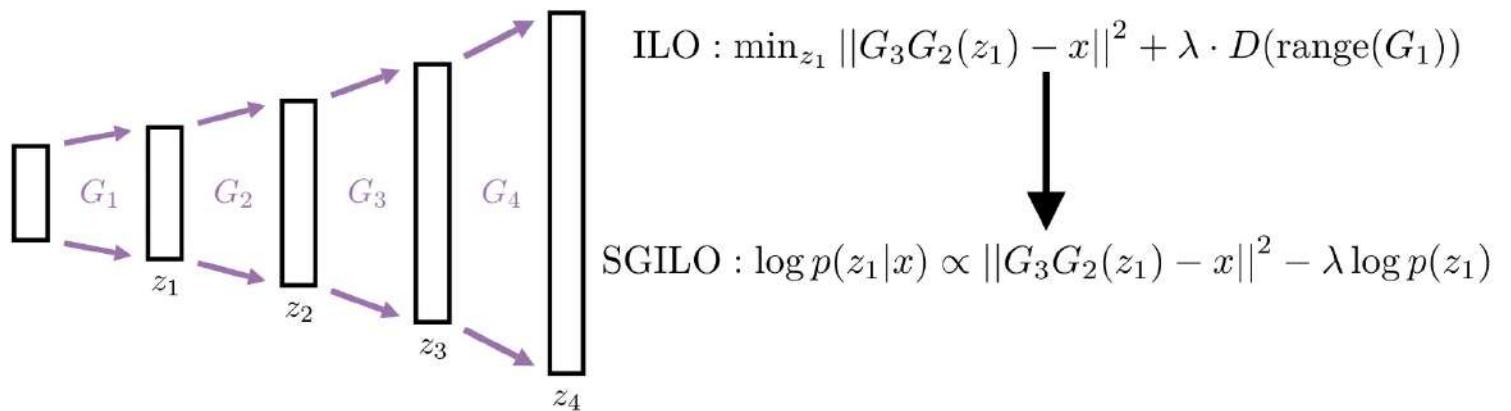
$$\min_{z_1} \|G_3 G_2(z_1) - x\|^2 + \underbrace{R(z_1)}_{\text{regularization}}$$

## Prior work: Intermediate Layer Optimization (ICML 2021)



$R(z_1)$ : close to the range of the previous layer.

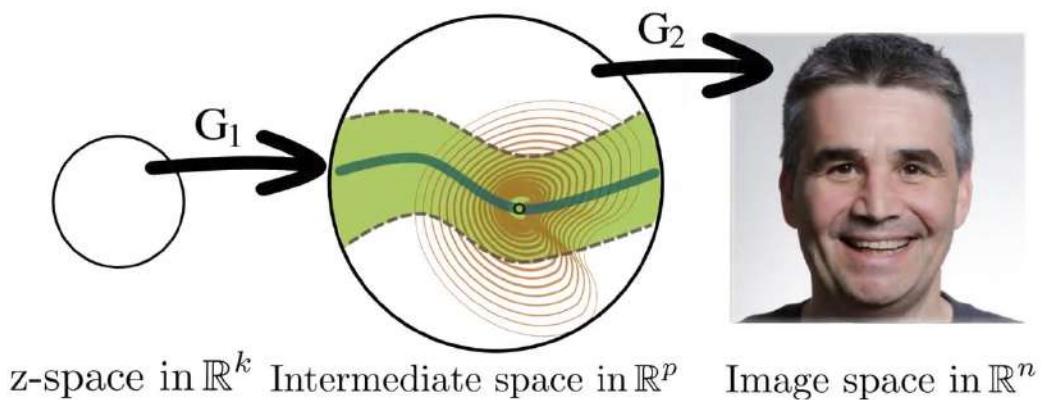
## Score-Guided Intermediate Layer Optimization (SGILO)



Changes:

- 1) From optimization to posterior sampling
- 2) Learned prior on latent space

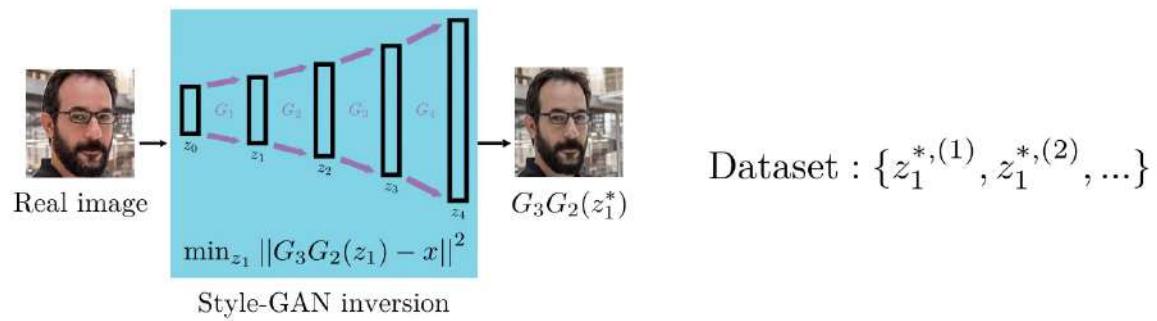
## Score-Guided Intermediate Layer Optimization (SGILO)



Changes:

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- 2) Learned prior on latent space

## Method: Training Phase



We train a diffusion model to learn the distribution of StyleGAN-2 intermediate latents

## Method: Sampling Phase

We want to:

- 1) match the measurements
- 2) Find a realistic latent
- 3) Be stochastic



Real image:  $x$

Input image:  $Ax$

$$z_1(t+1) = z_1(t) - \eta \left( \nabla_{z_1(t)} \|AG_3G_2(z_1(t)) - Ax\|^2 - \lambda s_\theta(z_1(t)) \right) + \sqrt{2\eta\beta^{-1}} u$$

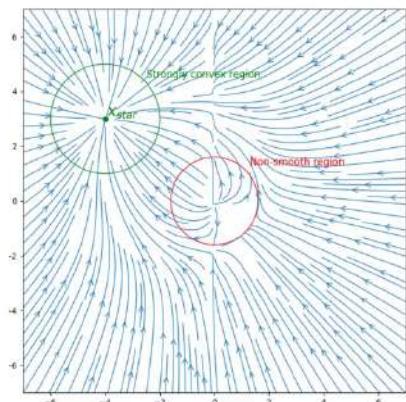
As  $t \rightarrow \infty$ , we will be sampling from  
 $\exp(-\beta \left( \|AG_3G_2(z_1(t)) - Ax\|^2 - \lambda \log p_\theta(z_1) \right))$

## Convergence of Langevin Dynamics for random generators

- ▷ Hand and Voroniski (2018): GD (wht no prior) converges fast to the optimum **point** for solving inverse problems with random generators
- ▷ SGLD (with no prior) converges fast to the stationary **distribution** for solving inverse problems with random generators

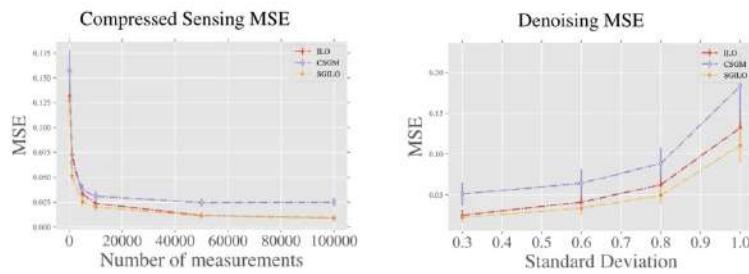
# Overview of the proof

- ▷ 0) Loss concentration.
- ▷ 1) Closed expression for expected loss.
- ▷ 2) Analyze vector field of expected loss.
- ▷ 3) W.h.p. we avoid the bad region and we enter the strongly convex region.
- ▷ 4) W.h.p. we don't escape the strongly convex region.
- ▷ 5) Discrete and continuous dynamics are close for strongly convex functions.

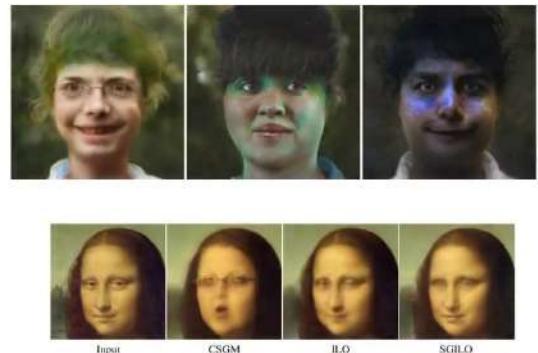


# Results

▷ Superior performance to inverse problems, compared to ILO and CSGM



▷ Fast and flexible image prior



▷ Diverse reconstructions using posterior sampling

