

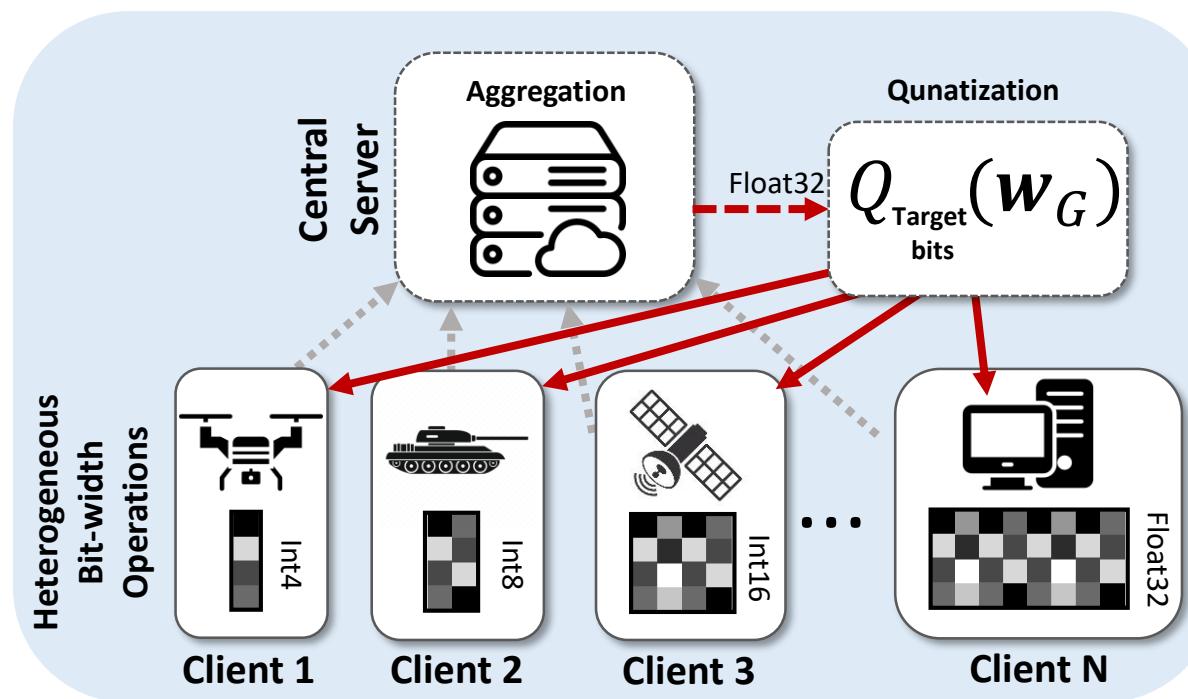
# Bitwidth Heterogeneous Federated Learning with Progressive Weight Dequantization

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(\*: equal contribution)

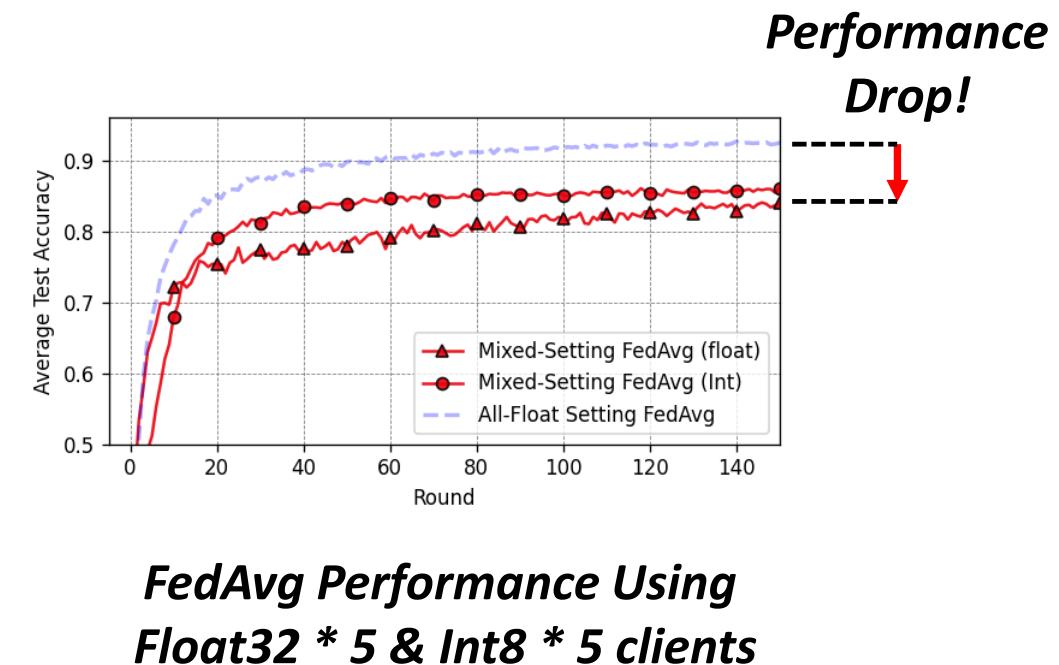
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# Bitwidth Heterogeneous Federated Learning

Embedded devices participating in federated learning may have to operate using **different bit-widths** for computation and storage during **training and inference**.



**Bitwidth Heterogeneous Federated Learning (BHFL)**



# Related Works

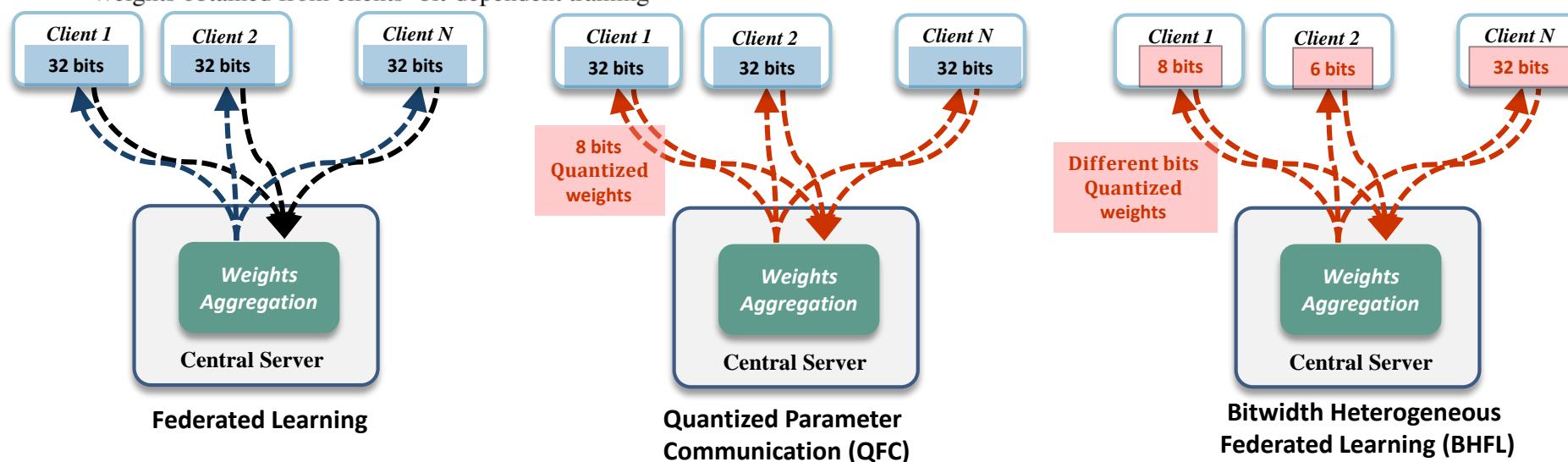
Embedded devices participating in federated learning may have to operate using **different bit-widths** for computation and storage during **training and inference**.

METHODS	FL Type	Bits <sub>Server</sub>	Bits <sub>Clients</sub>	Bits <sub>Uplink</sub>	Bits <sub>Downlink</sub>	Communication
FEDAVG (McMahan et al., 2017)	FL	Float32	Float32	Float32	Float32	Weights
FEDPROX (Li et al., 2018)	FL	Float32	Float32	Float32	Float32	Weights
FEDPAQ (Reisizadeh et al., 2020)	QPC <sup>1</sup>	Float32	Float32	Target bits	Float32	$Q_{\text{Target\_bits}}(\text{Diffs})$ <sup>2</sup>
FEDCOM (Haddadpour et al., 2021)	QPC	Float32	Float32	Target bits	Float32	$Q_{\text{Target\_bits}}(\text{Diffs})$
FEDCOMGATE (Haddadpour et al., 2021)	QPC	Float32	Float32	Target bits	Float32	$Q_{\text{Target\_bits}}(\text{Diffs})$
PROWD (OURS)	BHFL	Float32	Client-specific	Client-specific	Float32 × 2	$W_Q$ <sup>3</sup>

<sup>1</sup> Quantized Parameter Communication (QPC)

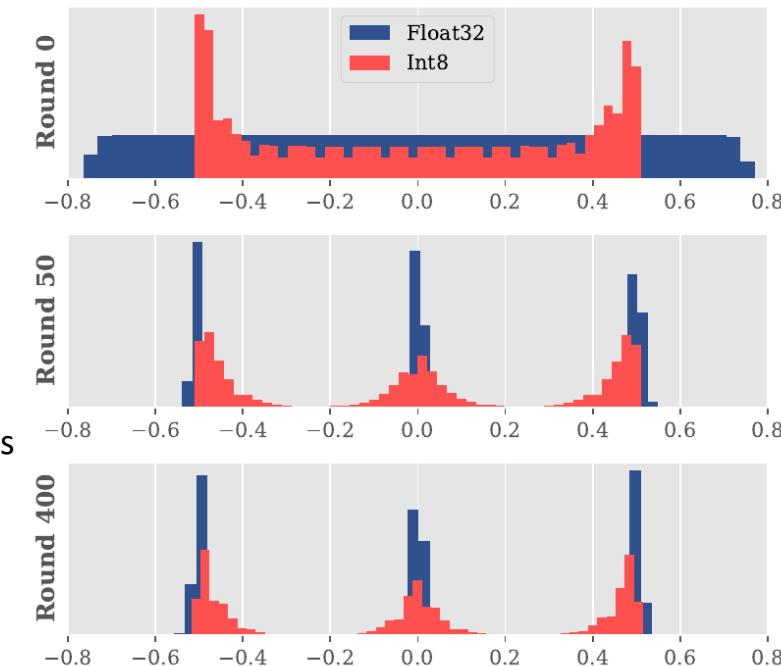
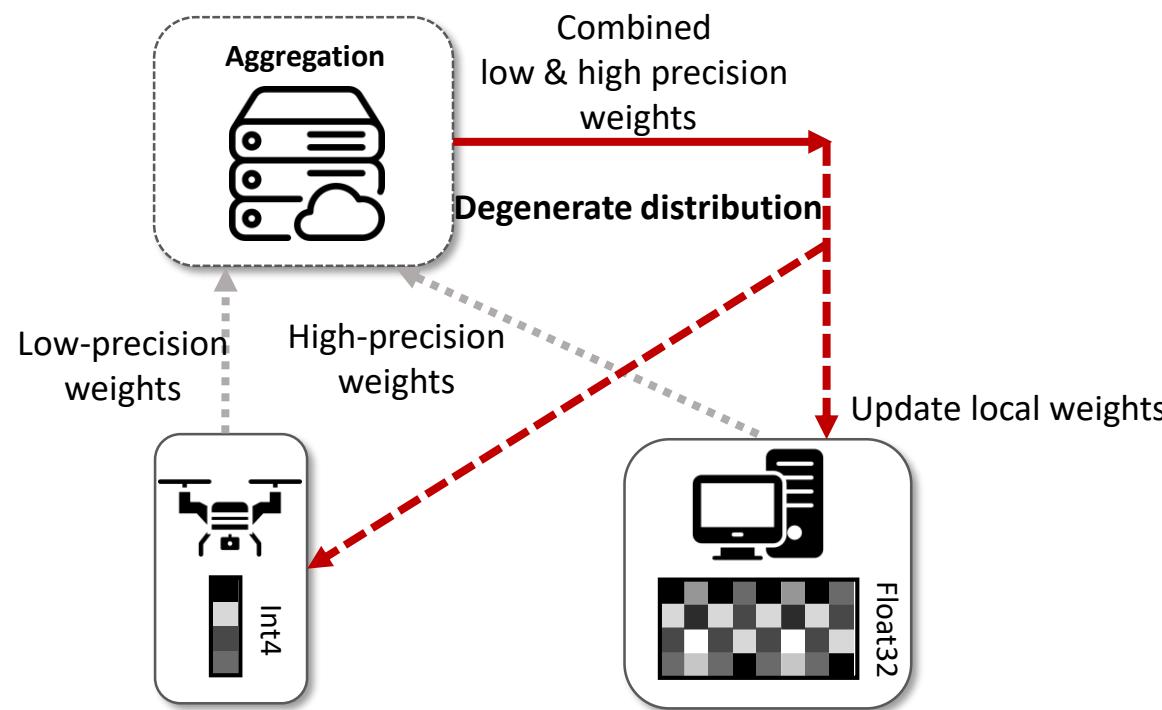
<sup>3</sup> Weights obtained from clients' bit-dependent training

<sup>2</sup>  $Q_{\text{Target\_bits}}(w)$ : A function quantizes input  $w$  to the target bitwidth



# Challenges

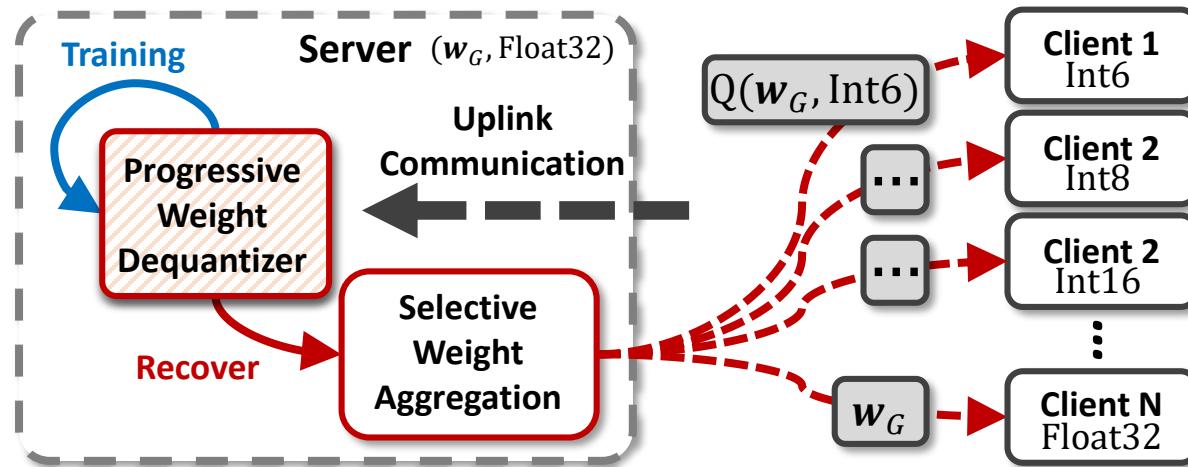
We observed that the weights from low-bitwidth clients **cannot easily be combined** with high-bitwidth weights due to **distributional incompatibility**.



*Degeneration of high-precision weights over naïve BHFL rounds*

# Methodology Overview

The server **dequantizes** the received mixed-bitwidth models into float32, before aggregating them and broadcasting to each client.

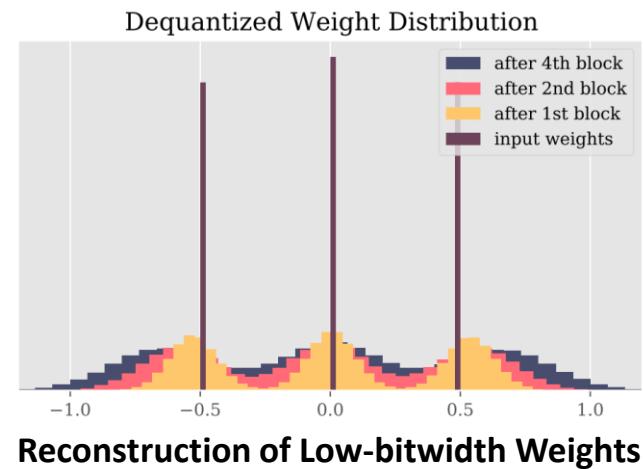
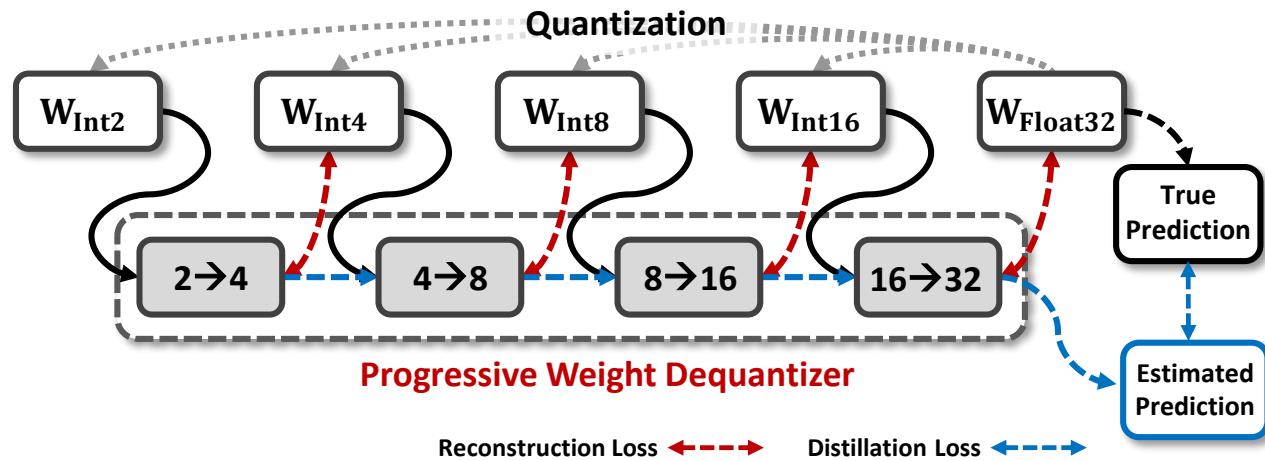


*Illustration of our ProWD framework*

The **Progressive Weight Dequantizer** and **Selective Weight Aggregation** can alleviate the distribution disparity problem.

# Progressive Dequantizer

Each block in our dequantizer **progressively converts** a set of weights into a higher bitwidth.



$$L_{recon} = \sum_{j=0}^{K-1} ||q_{\pi_{j+1}} - \phi^{\pi_j \rightarrow \pi_{j+1}}(q_{\pi_j}; \theta_j)||_1, \quad L_{distill} = -SIM(f(\mathbf{u}; \mathbf{w}), f(\mathbf{u}; \phi^{0 \rightarrow k}(q_{\pi_0}; \theta)))$$

**ProWD Objective**

$$\mathcal{L} = \mathcal{L}_{recon} + \lambda \mathcal{L}_{distill}$$

Reconstruction error	Distillation loss
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The dequantizer is **fine-tuned periodically** during the BHFL process using the weights sent from the clients, and a tiny server-side data buffer.

# Selective Weight Aggregation

In order to improve the stability of the training process, before aggregating, we **impose a mask** on the clients' weights based on the **relevancy** among the weights.

$$\mathbf{c}^* = \operatorname{argmax}_{\mathbf{c}} \frac{(\mathbf{c} \odot \Delta \bar{\mathbf{w}}_{\text{Low}})^\top \Delta \bar{\mathbf{w}}_{\text{High}}}{\|\mathbf{c} \odot \Delta \bar{\mathbf{w}}_{\text{Low}}\| \|\Delta \bar{\mathbf{w}}_{\text{High}}\|}, \text{ s.t. } |\mathbf{c}^*| \leq \tau$$

*Mask Computation*

$$\mathbf{w}_G \leftarrow \frac{1}{N} \sum_{n=1}^N \mathbf{c}_n \odot \mathbf{w}_n$$

*Selective weight aggregation*

# Experiments

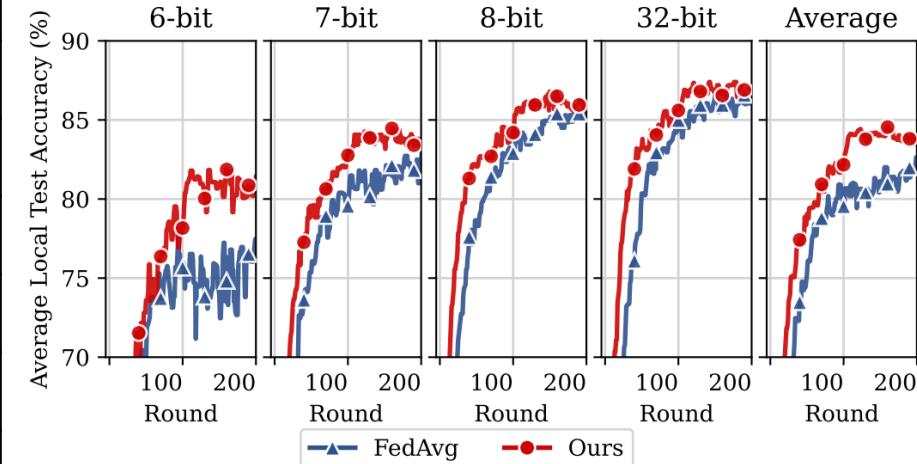
ProWD consistently **outperforms** strong baselines such as FedAvg, FedProx, FedCOM, and FedGroupedAvg.

Int8 50%    Float32 50%

	8bits Accuracy	32bits Accuracy	Averaged accuracy
Local Training	69.59	75.82	72.71
FedAvg	<b>76.88</b>	76.23	<b>76.56</b>
FedProx	71.16	69.28	70.22
FedCOM	75.37	77.69	76.53
GroupedAvg	61.85	<b>85.08</b>	73.46
<b>ProWD (Ours)</b>	<b>82.87</b>	<b>85.99</b>	<b>84.43</b>

Int8 80%    Float32 20%

	8bits Accuracy	32bits Accuracy	Averaged accuracy
Local Training	69.39	76.41	70.79
FedAvg	<b>77.43</b>	74.64	<b>76.87</b>
FedProx	69.60	66.28	68.94
FedCOM	73.60	<b>80.73</b>	75.03
GroupedAvg	71.76	78.07	73.02
<b>ProWD (Ours)</b>	<b>79.23</b>	<b>81.26</b>	<b>79.63</b>



# Conclusion

- We propose a **novel yet practical scenario** for FL where the participating devices operate using different bit-widths, called BHFL.
- We propose a novel framework, *ProWD*, for bit-heterogeneous FL, which can tackle these issues based on progressive weight dequantization and selective weight aggregation.
- We evaluate ProWD on realistic BHFL scenarios and show the effectiveness of our framework.

# Thank you

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