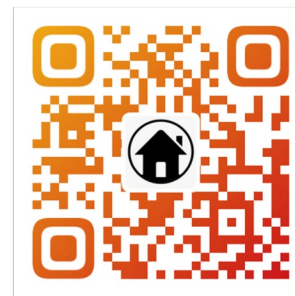


ProGCL: Rethinking Hard Negative Mining in Graph Contrastive Learning

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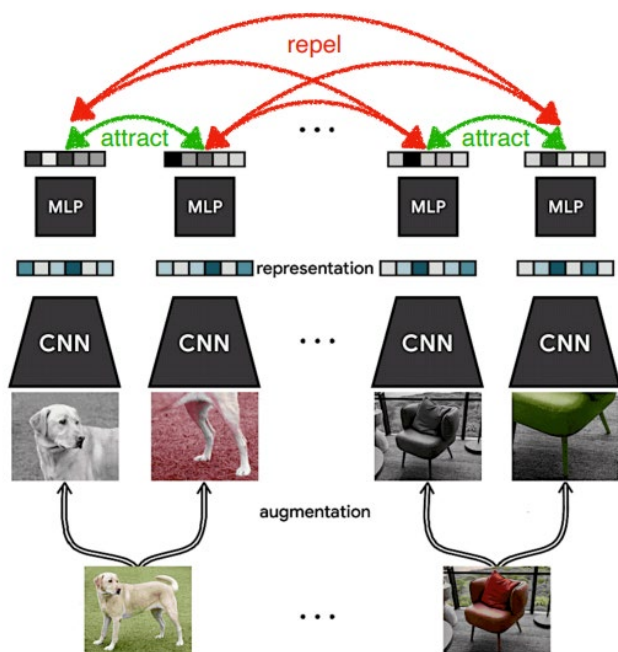


Outline

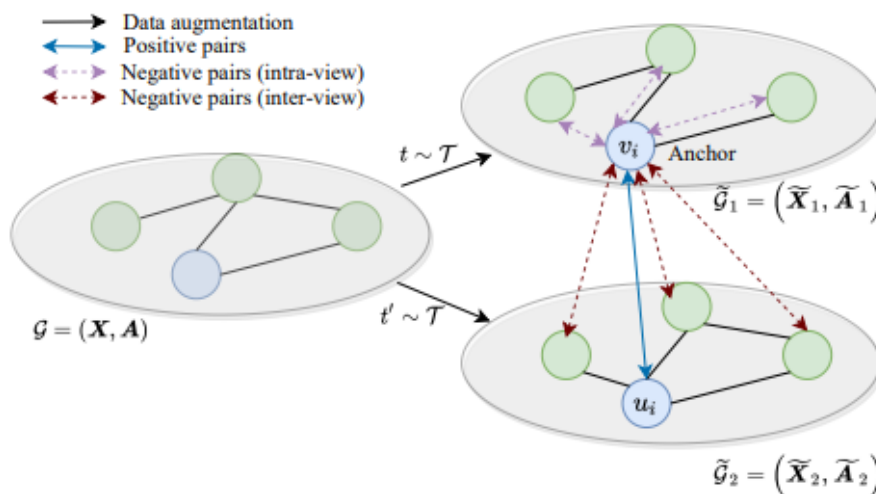
- Preamble
- Analysis
- ProGCL
- Experiments
- Concluding Remarks

Preamble

- Contrastive Learning (CL) & Graph Contrastive Learning (GCL)



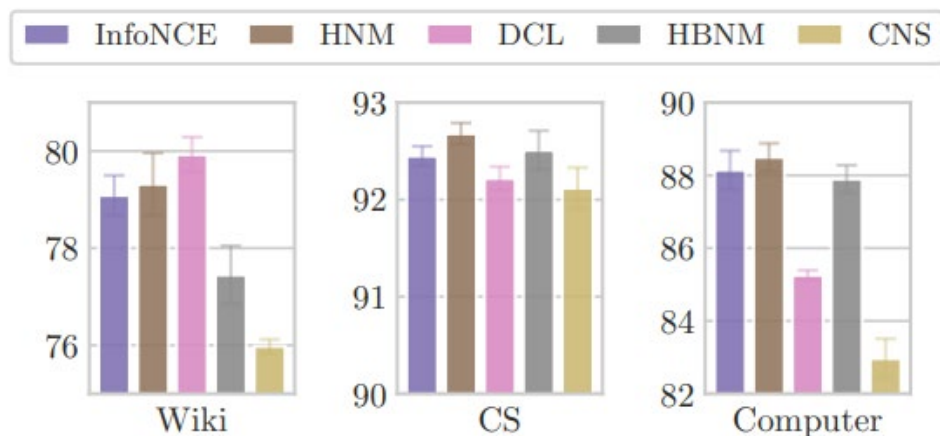
Ref 1. SimCLR, ICML'20



Ref 2. GCA, WWW'21

Analysis

- Hard Negative Mining Methods Fail in Graph Contrastive Learning



Ref 3. NeurIPS' 21 (Benchmarks Track)

Methods/Datasets	Amazon-Photo	Amazon-Computers	Coauthor-CS
GCA	92.55	87.82	92.40
+DCL	91.02 (↓ 1.53)	86.58 (↓ 1.24)	92.36 (↓ 0.04)
+HCL	91.48 (↓ 1.07)	87.21 (↓ 0.61)	93.06 (↑ 0.66)
+MoCHi	92.36 (↓ 0.19)	87.68 (↑ 0.14)	92.58 (↑ 0.18)
+Ring	91.33 (↓ 1.22)	84.18 (↓ 3.64)	92.48 (↓ 0.08)
+ProGCL-mix	93.64 (↑ 1.09)	89.55 (↑ 1.73)	93.67 (↑ 1.27)

Table 1. Our Results

Analysis

- Why above phenomena would occur ?

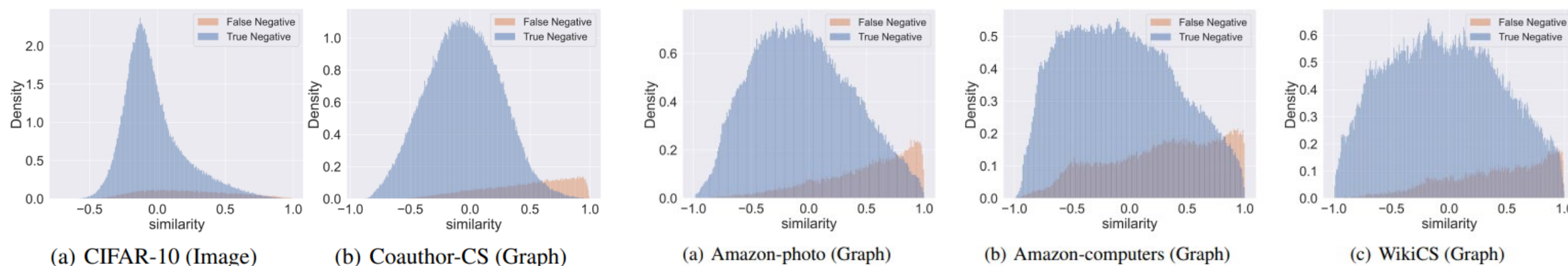


Fig 2. Similarity histograms of negatives.

Unlike CL, most negatives with larger similarities to the anchor are false ones in GCL.

Analysis

- Experimental & Theoretical Analysis

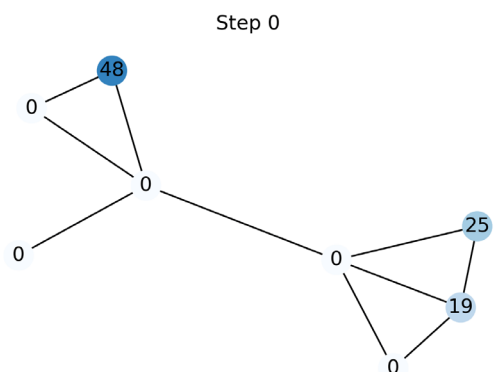


Fig 3. Semantic Diagram of Messaging-Passing.

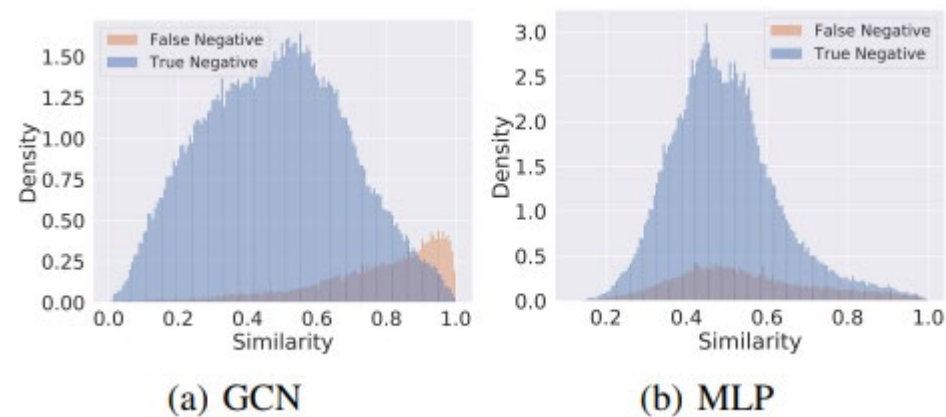
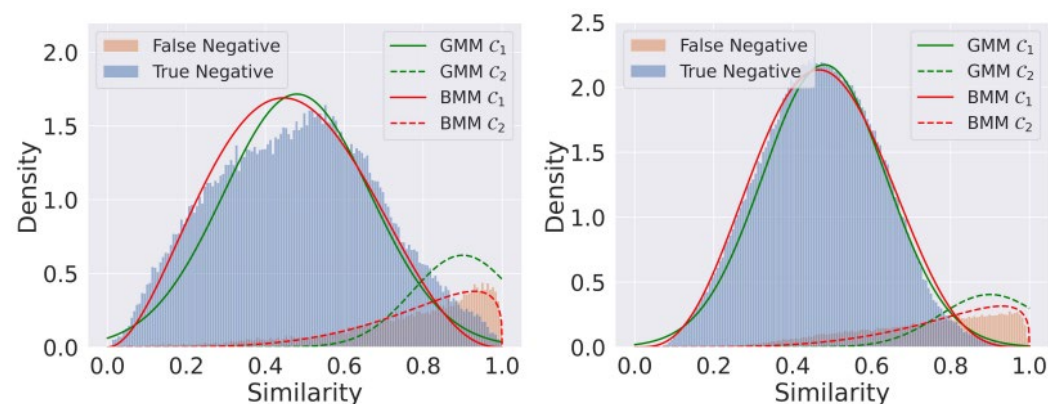


Fig 4. GCN (with MP) vs. MLP (w/o MP).

Delving into the Role of Message-Passing in GCL

- How to eliminate the bias?

- a. Fit the negatives' distribution with Beta Mixture Model (BMM)



(a) Amazon-Photo

(b) Coauthor-CS

Fig 5. Empirical distribution v.s. estimated distribution.

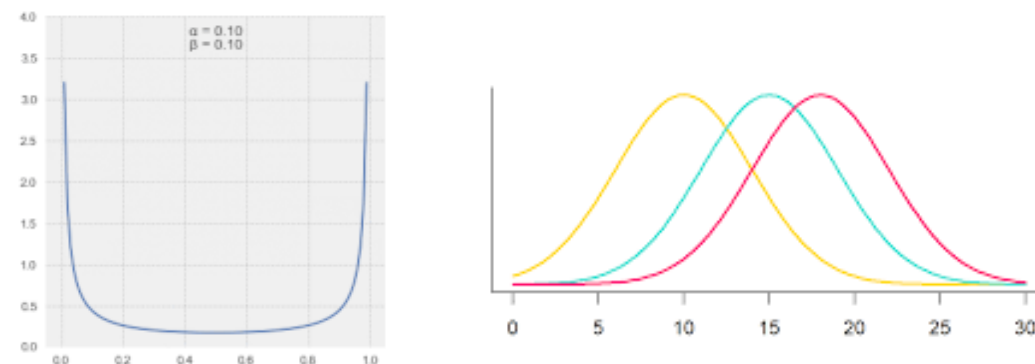


Fig 6. Beta distribution v.s. Normal distribution.

Beta distribution
$$p(s | \alpha, \beta) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} s^{\alpha-1} (1-s)^{\beta-1}$$

Normal distribution
$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

- Expectation-Maximization for Beta Mixture Distribution

- a. E-Step

$$p(s) = \sum_{c=1}^C \lambda_c p(s | \alpha_c, \beta_c). \quad p(c | s) = \frac{\lambda_c p(s | \alpha_c, \beta_c)}{\sum_{j=1}^C \lambda_j p(s | \alpha_j, \beta_j)} \quad \bar{s}_c = \frac{\sum_{i=1}^M p(c | s_i) s_i}{\sum_{i=1}^M p(c | s_i)}, \quad v_c^2 = \frac{\sum_{i=1}^M p(c | s_i) (s_i - \bar{s}_c)^2}{\sum_{i=1}^M p(c | s_i)}$$

- b. M-Step

$$\alpha_c = \bar{s}_c \left(\frac{\bar{s}_c (1 - \bar{s}_c)}{v_c^2} - 1 \right), \quad \beta_c = \frac{\alpha_c (1 - \bar{s}_c)}{\bar{s}_c} \quad \lambda_c = \frac{1}{M} \sum_{i=1}^M p(c | s_i) \quad p(c | s) = \frac{p(c) p(s | \alpha_c, \beta_c)}{p(s)}$$

- Scheme 1: ProGCL-weight

New Measure:
$$w(i, k) = \frac{p(c_t | s_{ik}) s_{ik}}{\frac{1}{N-1} \sum_{j \neq i} [p(c_t | s_{ij}) s_{ij}]}$$

$$\ell_w(\mathbf{u}_i, \mathbf{v}_i) = \log \frac{e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_i)}{\tau}}}{\underbrace{e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_i)}{\tau}}}_{\text{positive pair}} + \underbrace{\sum_{k \neq i} w(i, k) e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_k)}{\tau}}}_{\text{inter-view negative pairs}} + \underbrace{\sum_{k \neq i} w(i, k) e^{\frac{\theta(\mathbf{u}_i, \mathbf{u}_k)}{\tau}}}_{\text{intra-view negative pairs}}}$$

$$\mathcal{J}_w = -\frac{1}{2N} \sum_{i=1}^N [\ell_w(\mathbf{u}_i, \mathbf{v}_i) + \ell_w(\mathbf{v}_i, \mathbf{u}_i)]$$

ProGCL

• Scheme 2: ProGCL-mix

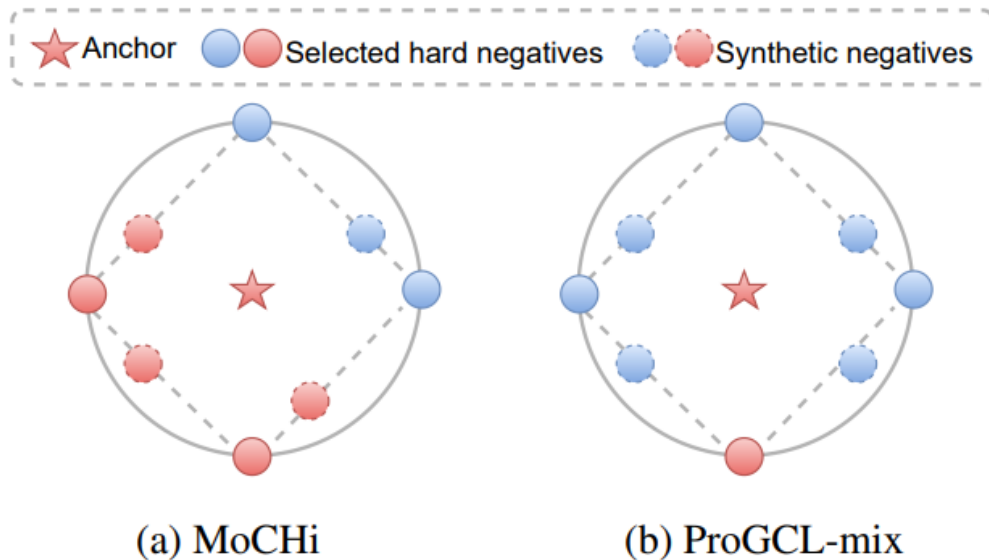


Fig 7. MoChi (NeurIPS' 21) v.s. ProGCL-mix.

$$\tilde{\mathbf{u}}_k = \alpha_k \mathbf{v}_p + (1 - \alpha_k) \mathbf{v}_q,$$

$$\alpha_k = \frac{p(c_t | s_{ip})}{p(c_t | s_{ip}) + p(c_t | s_{iq})}$$

$$\ell_m(\mathbf{u}_i, \mathbf{v}_i) =$$

$$\log \frac{e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_i)}{\tau}}}{\underbrace{e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_i)}{\tau}}}_{\text{positive pair}} + \underbrace{\sum_{k \neq i} e^{\frac{\theta(\mathbf{u}_i, \mathbf{v}_k)}{\tau}}}_{\text{inter-view negative pairs}} + \underbrace{\sum_{k \neq i} e^{\frac{\theta(\mathbf{u}_i, \mathbf{u}_k)}{\tau}}}_{\text{intra-view negative pairs}} + \underbrace{\sum_{k=1}^m e^{\frac{\theta(\mathbf{u}_i, \tilde{\mathbf{u}}_k)}{\tau}}}_{\text{synthetic negative pairs}}}$$

$$\mathcal{J}_m = -\frac{1}{2N} \sum_{i=1}^N [\ell_m(\mathbf{u}_i, \mathbf{v}_i) + \ell_m(\mathbf{v}_i, \mathbf{u}_i)]$$

Experiments

- Results in Transductive Setting

Method	Available Data	Amazon-Photo	Amazon-Computers	Coauthor-CS	Wiki-CS
Raw features	X	78.53 ± 0.00	73.81 ± 0.00	90.37 ± 0.00	71.98 ± 0.00
node2vec	A	89.67 ± 0.12	84.39 ± 0.08	85.08 ± 0.03	71.79 ± 0.05
DeepWalk	A	89.44 ± 0.11	85.68 ± 0.06	84.61 ± 0.22	74.35 ± 0.06
DeepWalk + features	X, A	90.05 ± 0.08	86.28 ± 0.07	87.70 ± 0.04	77.21 ± 0.03
GAE	X, A	91.62 ± 0.13	85.27 ± 0.19	90.01 ± 0.17	70.15 ± 0.01
VGAE	X, A	92.20 ± 0.11	86.37 ± 0.21	92.11 ± 0.09	75.35 ± 0.14
DGI	X, A	91.61 ± 0.22	83.95 ± 0.47	92.15 ± 0.63	75.35 ± 0.14
GMI	X, A	90.68 ± 0.17	82.21 ± 0.31	OOM	74.85 ± 0.08
MVGRL*	X, A	92.08 ± 0.01	87.45 ± 0.21	92.18 ± 0.15	77.43 ± 0.17
BGRL*	X, A	92.95 ± 0.07	87.89 ± 0.10	92.72 ± 0.03	78.41 ± 0.09
MERIT*	X, A	92.53 ± 0.15	88.01 ± 0.12	92.51 ± 0.14	78.35 ± 0.05
GCA*	X, A	92.55 ± 0.03	87.82 ± 0.11	92.40 ± 0.07	78.26 ± 0.06
ProGCL-weight	X, A	93.30 ± 0.09	89.28 ± 0.15	93.51 ± 0.06	78.68 ± 0.12
ProGCL-mix	X, A	93.64 ± 0.13	89.55 ± 0.16	93.67 ± 0.12	78.45 ± 0.04
Supervised GCN	X, A, Y	92.42 ± 0.22	86.51 ± 0.54	<u>93.03 ± 0.31</u>	77.19 ± 0.12
Supervised GAT	X, A, Y	<u>92.56 ± 0.35</u>	<u>86.93 ± 0.29</u>	92.31 ± 0.24	<u>77.65 ± 0.11</u>

Experiments

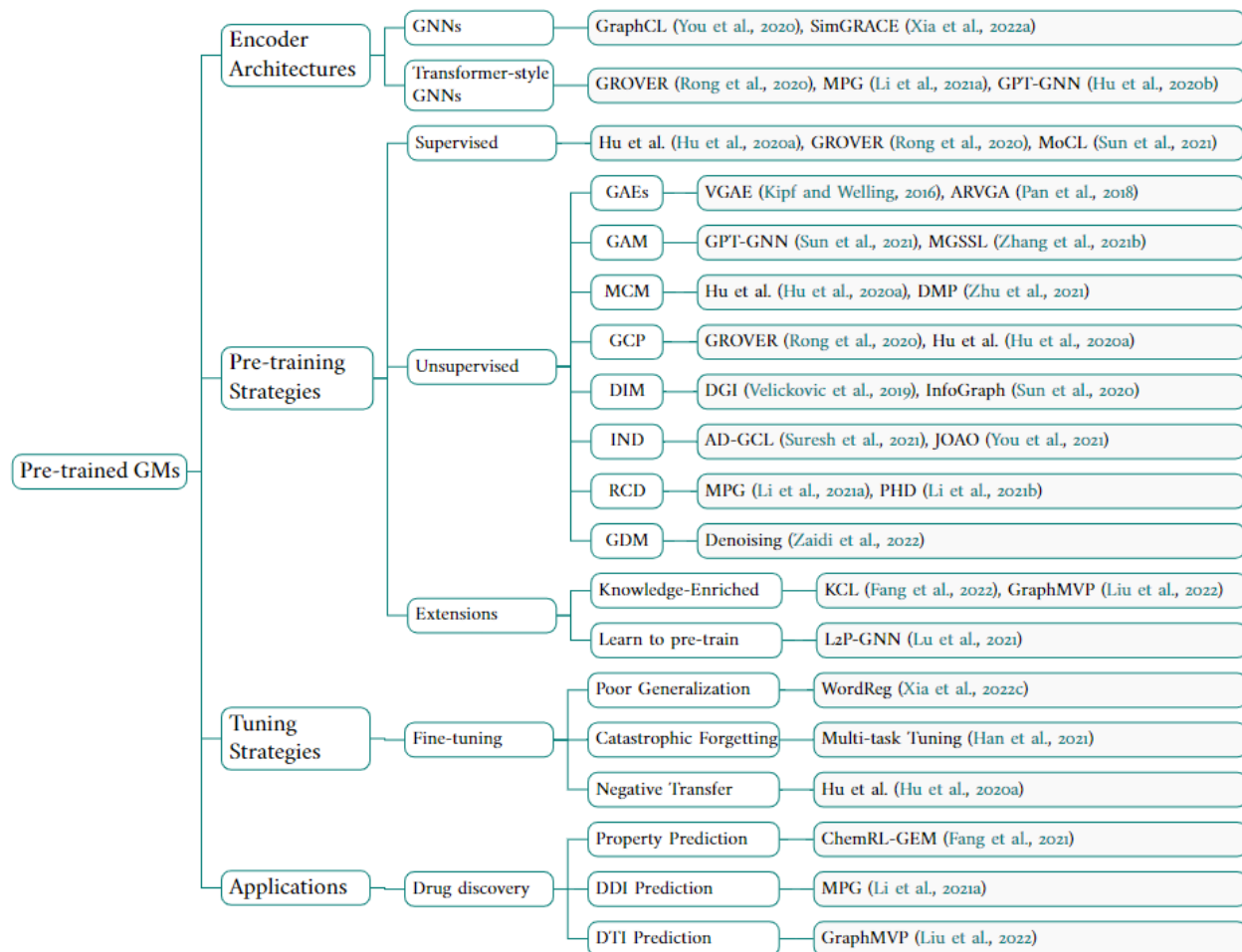
- Results in Inductive Setting

Method	Available Data	Flickr	Reddit
Raw features	X	20.3	58.5
DeepWalk	A	27.9	32.4
GraphSAGE	X, A	36.5	90.8
DGI	X, A	42.9 ± 0.1	94.0 ± 0.1
GMI	X, A	44.5 ± 0.2	94.8 ± 0.0
COLES-S ² GC	X, A	46.8 ± 0.5	95.2 ± 0.3
GRACE	X, A	48.0 ± 0.1	94.2 ± 0.0
ProGCL-weight	X, A	49.2 ± 0.6	95.1 ± 0.2
ProGCL-mix	X, A	50.0 ± 0.3	95.6 ± 0.1
Supervised FastGCN	X, A, Y	48.1 ± 0.5	89.5 ± 1.2
Supervised GraphSAGE	X, A, Y	<u>50.1 ± 1.3</u>	<u>92.1 ± 1.1</u>

	Validation	Test
MLP	57.65 ± 0.12	55.50 ± 0.23
node2vec	71.29 ± 0.13	70.07 ± 0.13
Random-Init	69.90 ± 0.11	68.94 ± 0.15
DGI	71.26 ± 0.11	70.34 ± 0.16
GRACE-Subsampling	72.61 ± 0.15	71.51 ± 0.11
BGRL	72.53 ± 0.09	71.64 ± 0.12
COLES-S ² GC	—	72.48 ± 0.25
ProGCL-weight	72.45 ± 0.21	72.18 ± 0.09
ProGCL-mix	72.82 ± 0.08	72.56 ± 0.20
Supervised GCN	73.00 ± 0.17	71.74 ± 0.29

Concluding Remarks

• Pretrained Graph Models for Molecular Representations: Retrospect and Prospect



Concluding Remarks

- Useful Resources

- a. The first comprehensive survey of pre-training on molecular graphs.

- ✓ https://bit.ly/PGMs_survey

- ✓ Journal version is under review.



- b. A curated list of must-read papers, open-source pre-trained models and pre-training datasets.

- ✓ https://bit.ly/PGM_resources



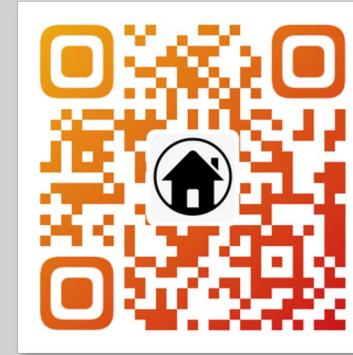
Thank you!



Code



Paper



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