



Mitigating Modality Collapse in Multimodal VAEs via Impartial Optimization



Adrián Javaloy



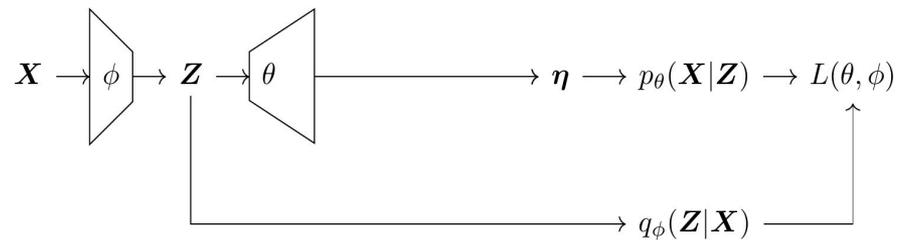
Maryam Meghdadi



Isabel Valera

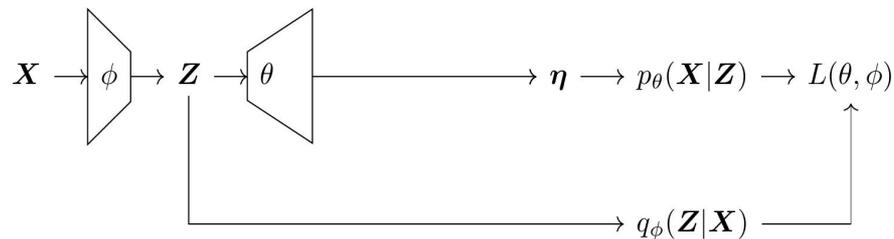
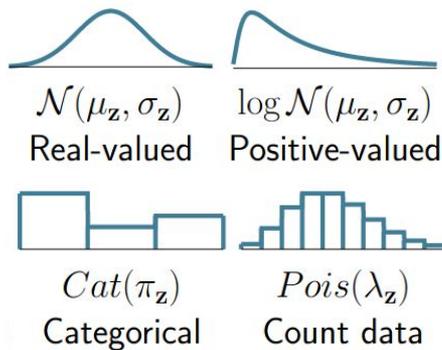
Problem motivation

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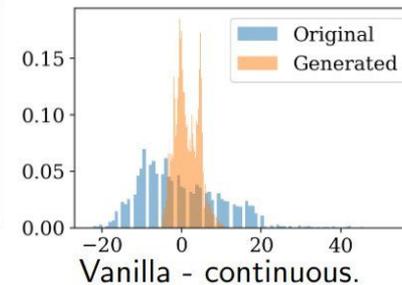
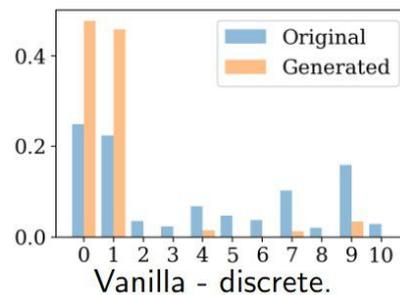
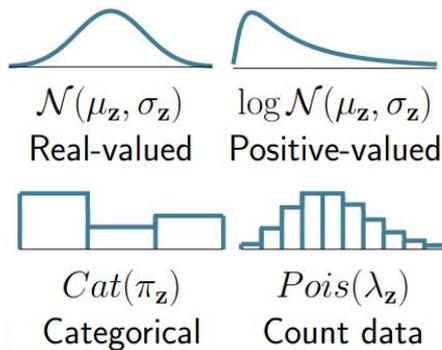
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Each modality is of a different type:



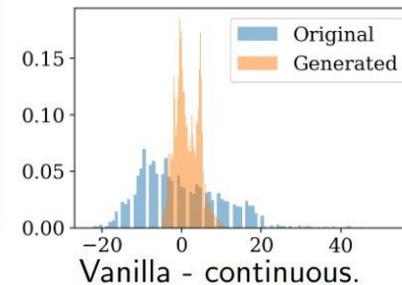
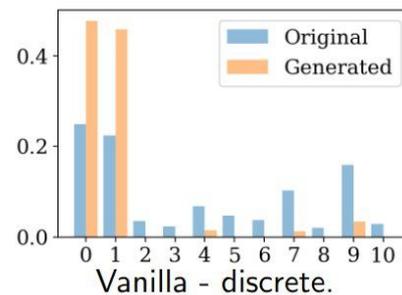
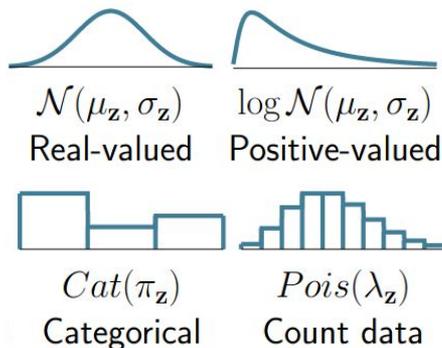
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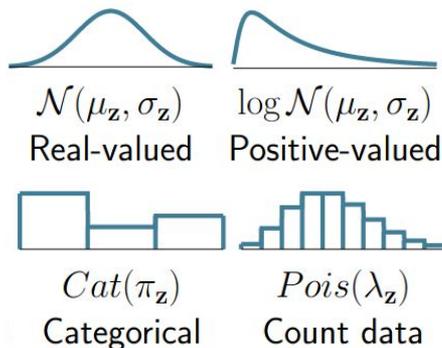


Likelihood impartiality

We aim for a learning process that does not prioritize learning any of the different likelihood modalities.

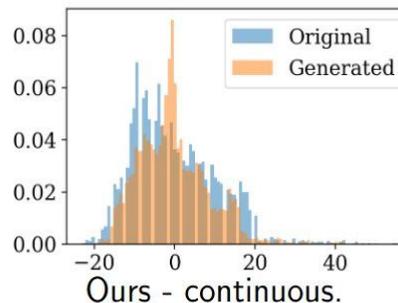
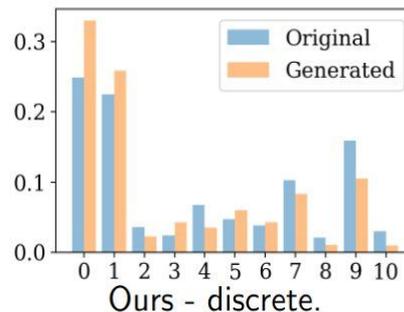
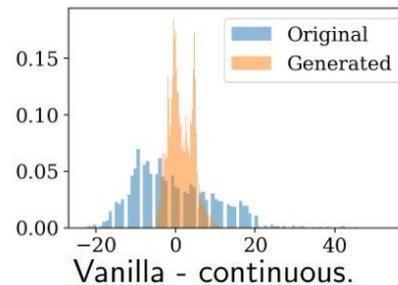
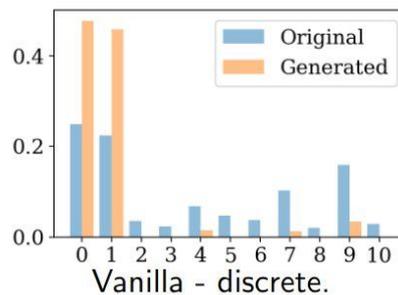
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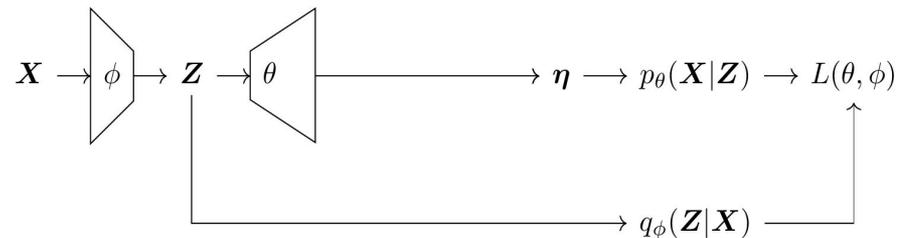
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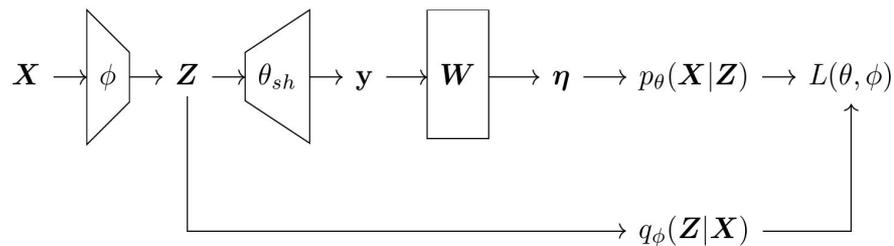


Analyzing modality collapse

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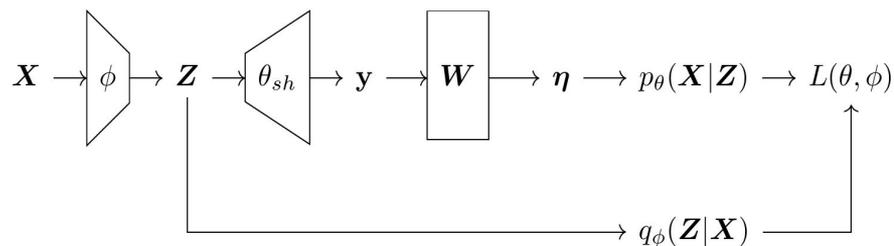
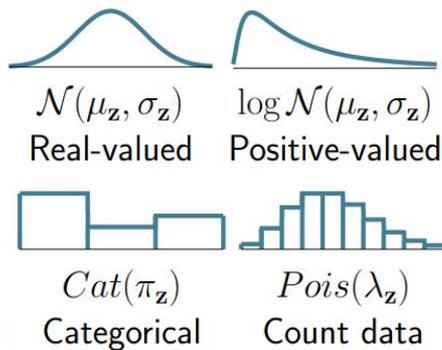


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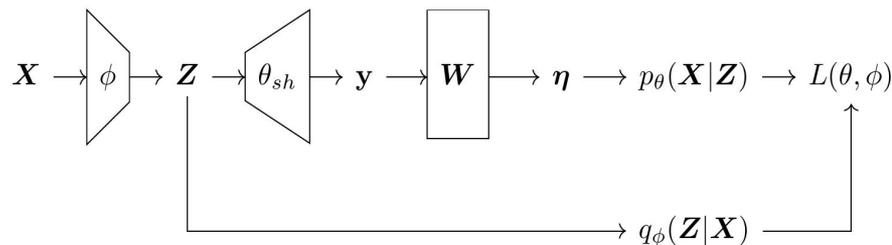
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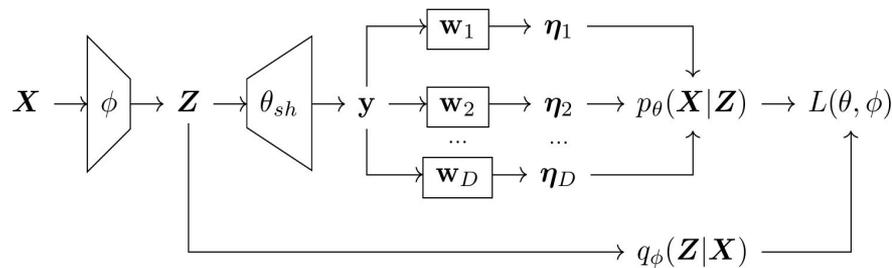
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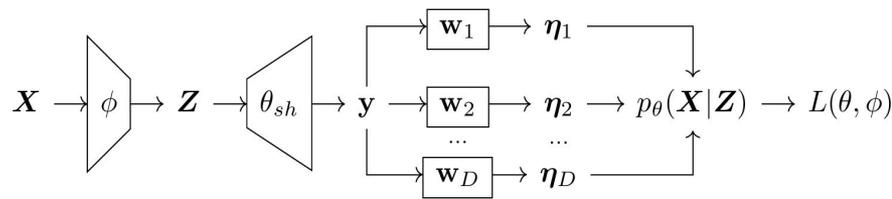
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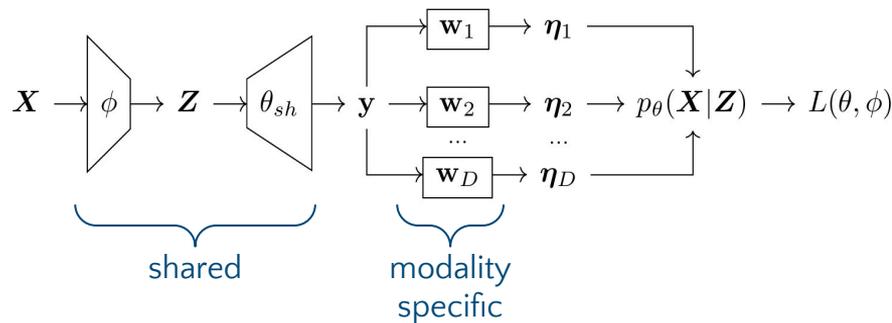
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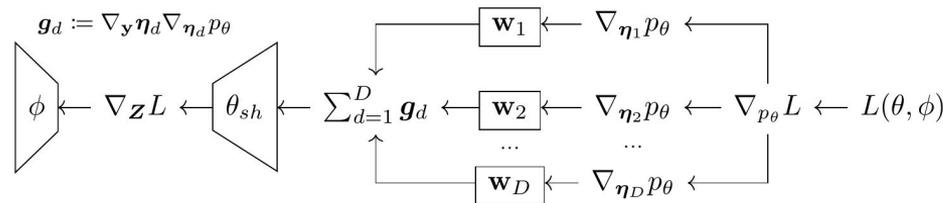
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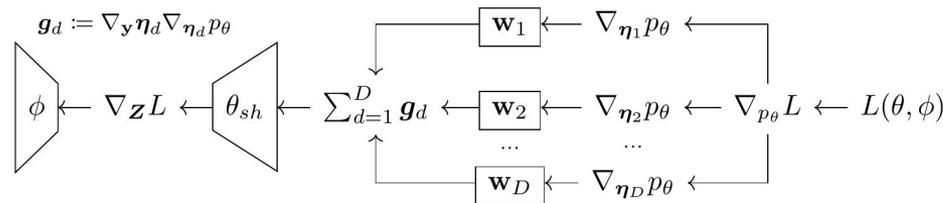
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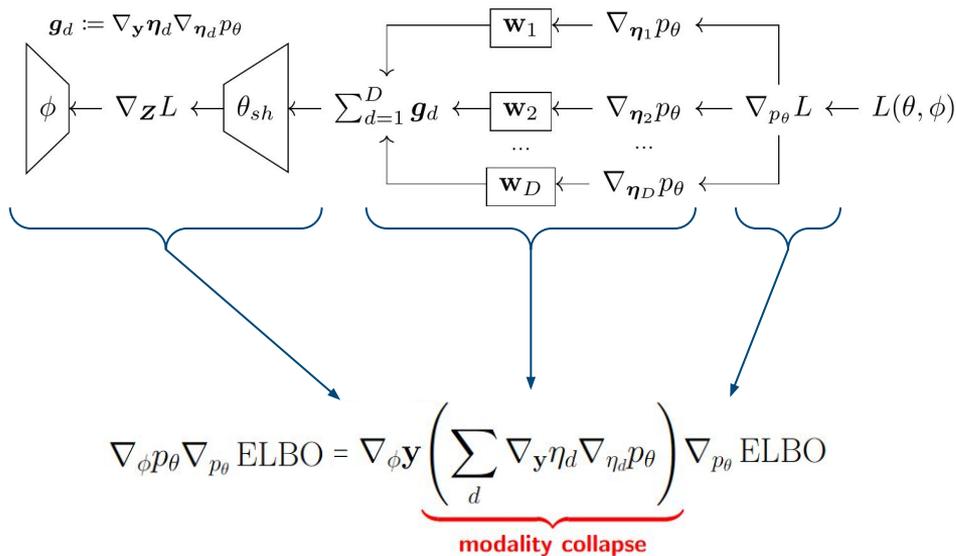


$$\nabla_{\phi} p_{\theta} \nabla_{p_{\theta}} \text{ELBO}$$

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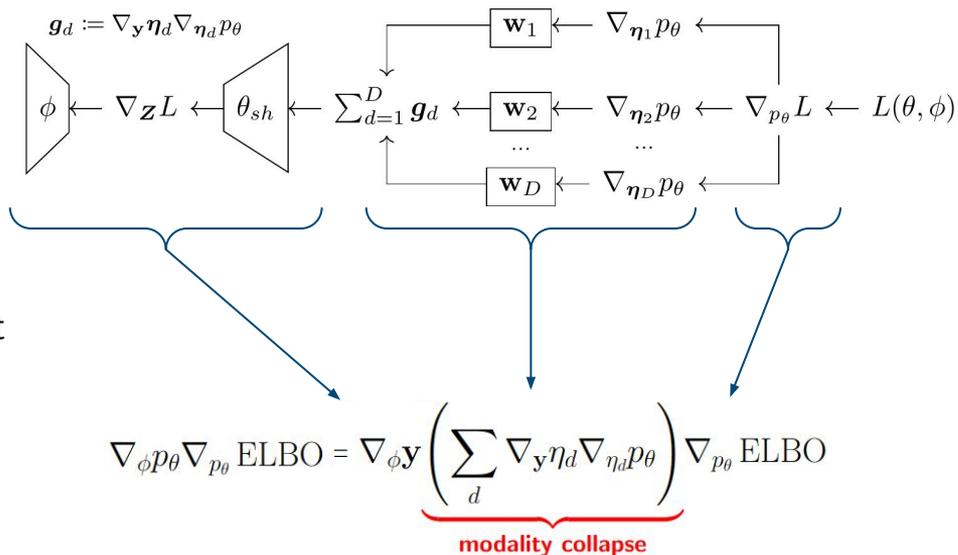
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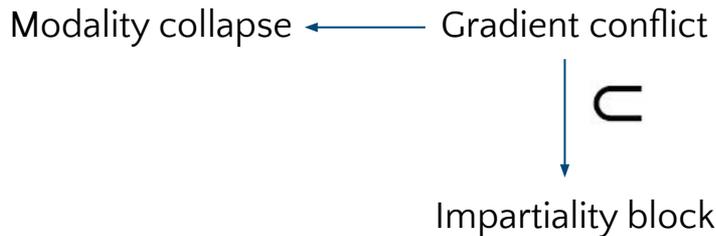
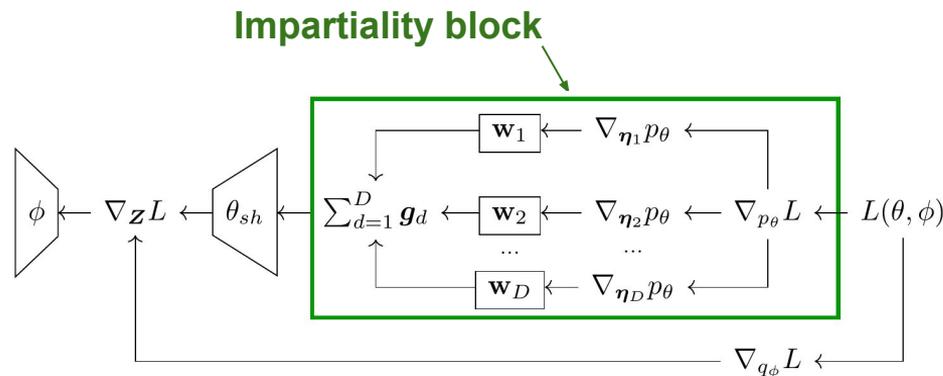


Modality collapse ← Gradient conflict

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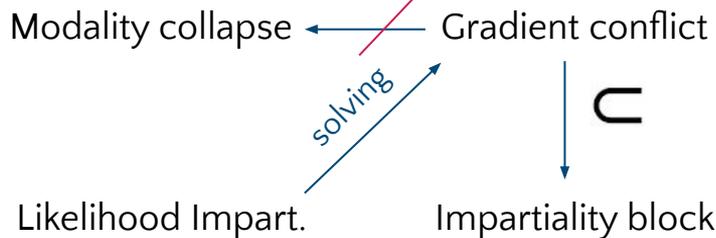
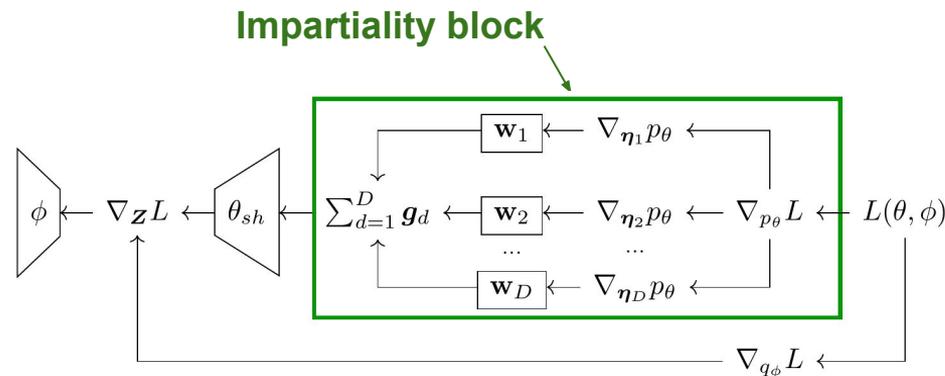
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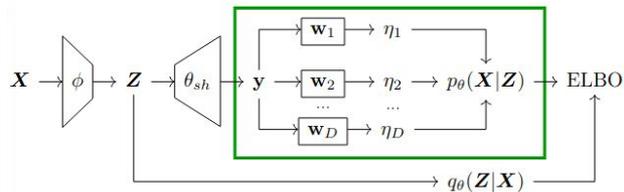
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Multimodal VAEs



Want: Model all modalities equally well.

Problem: Modality collapse.

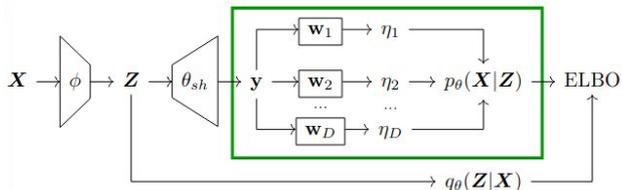
Shared params: ϕ and θ_{sh} .

Excl. params: w_1, w_2, \dots, w_K .

Updating ϕ :

$$\begin{aligned}\nabla_{\phi} p_{\theta} \nabla_{p_{\theta}} \text{ELBO} &= \\ &= \nabla_{\phi} y \underbrace{\left(\sum_d \nabla_y \eta_d \nabla_{\eta_d} p_{\theta} \right)}_{\text{modality collapse}} \nabla_{p_{\theta}} \text{ELBO}\end{aligned}$$

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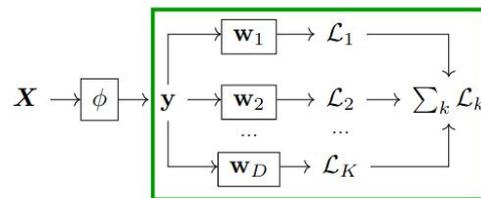
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Multitask Learning



Want: Learn all tasks equally well.

Problem: Negative transfer.

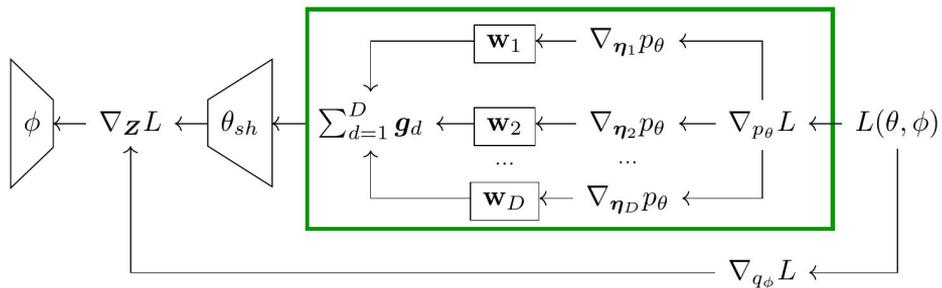
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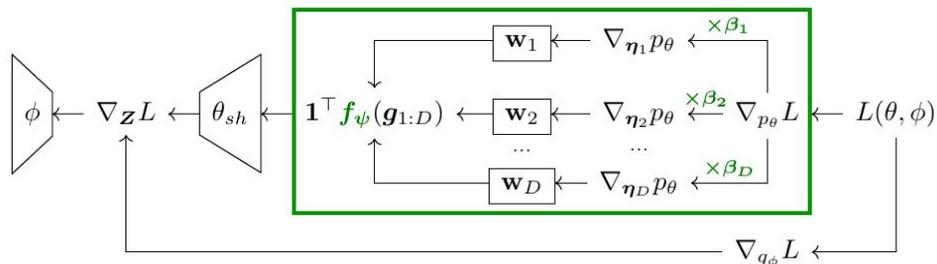
Updating ϕ :

$$\nabla_{\phi} \mathcal{L} = \nabla_{\phi} \mathbf{y} \underbrace{\left(\sum_k \nabla_{\mathbf{y}} \mathcal{L}_k \right)}_{\text{negative transfer}}$$

How to achieve impartiality



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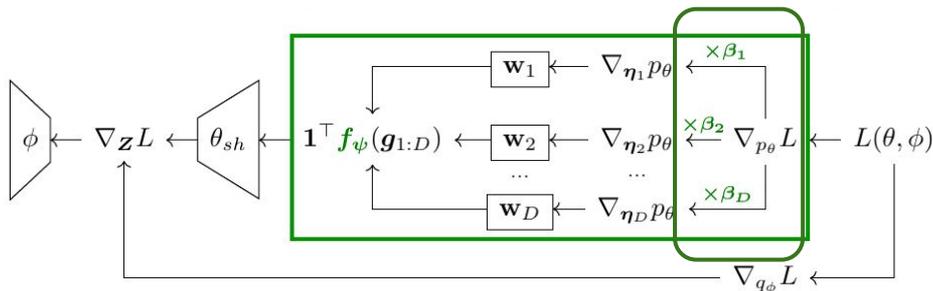


Two-step solution:

Algorithm 1 Backward pass within the impartiality block.

- 1: **Input:** Output gradient, $\nabla_{p_\theta} L$.
- 2: **for** $d = 1$ **to** D **do**
- 3: $\mathbf{h}_d \leftarrow \beta_d \nabla_{\eta_d p_\theta} \nabla_{p_\theta} L$
- 4: $\nabla_{\omega_d} L \leftarrow \nabla_{\omega_d} \eta_d \cdot \mathbf{h}_d$
- 5: $\mathbf{g}_d \leftarrow \nabla_{\mathbf{y}} \eta_d \cdot \mathbf{h}_d$
- 6: **end for**
- 7: $\tilde{\mathbf{g}}_{1:D} \leftarrow \mathbf{f}_\psi(\mathbf{g}_{1:D})$
- 8: **return** $\sum_d \tilde{\mathbf{g}}_d$

How to achieve impartiality



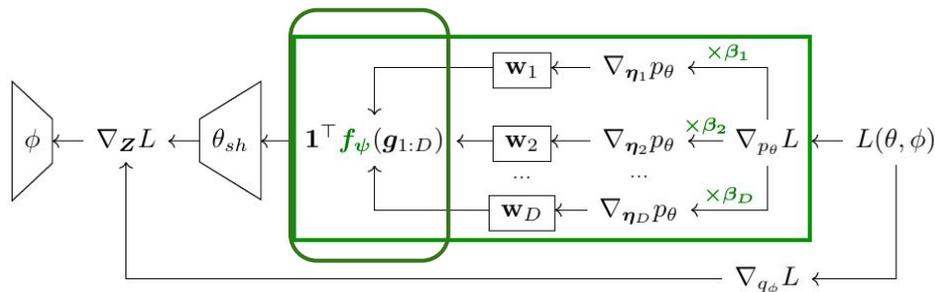
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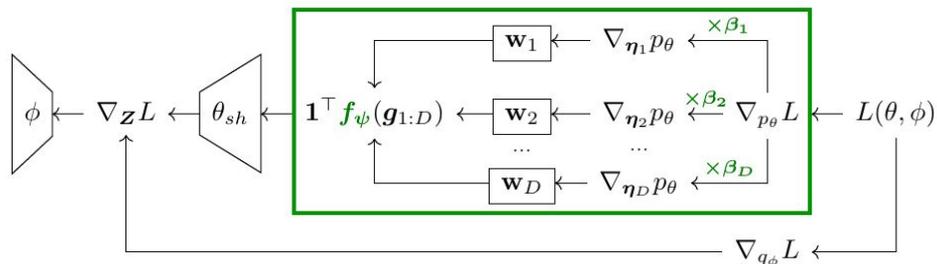
Local step, β : re-scale gradients to make them comparable.

Global step, f : apply an MTL algorithm to alleviate gradient conflict.

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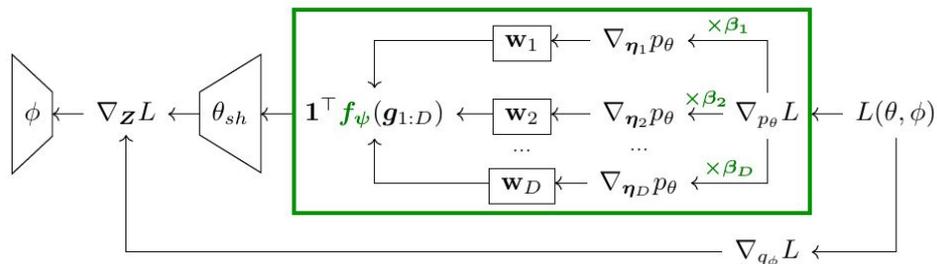


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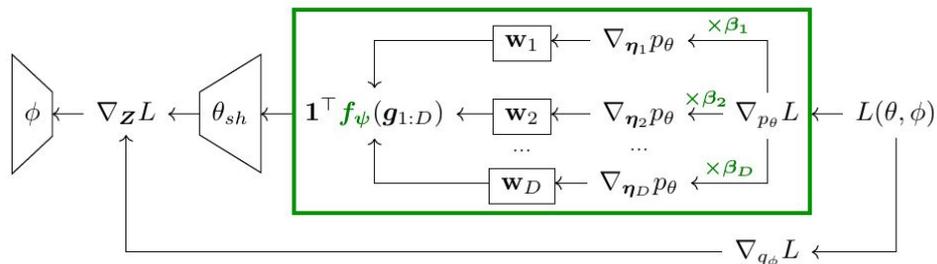
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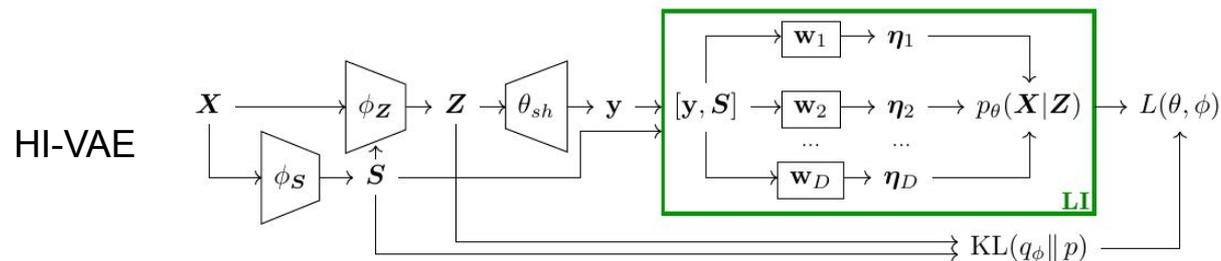
It can appear more than once.

Algorithm 1 Backward pass within the impartiality block.

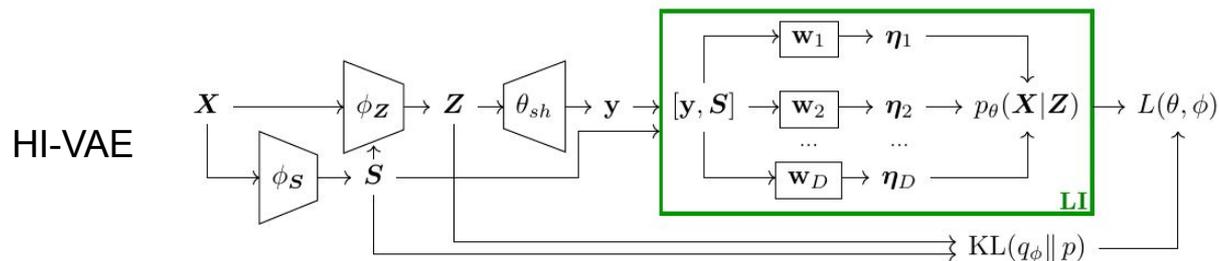
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VAE extensions

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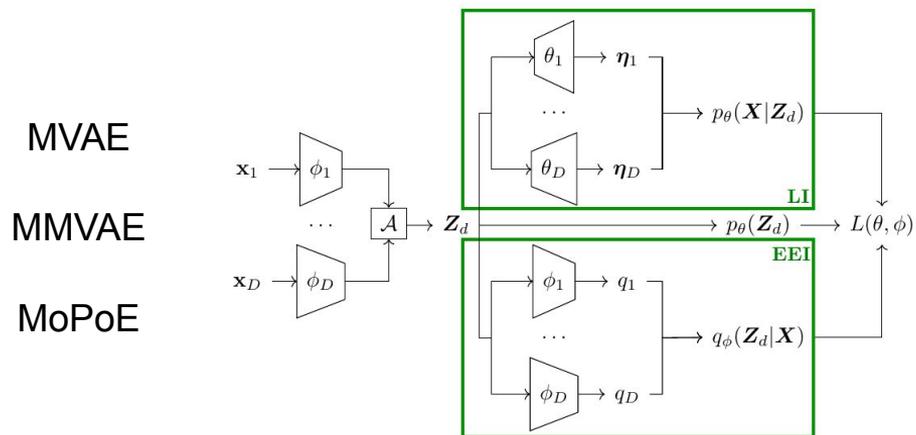
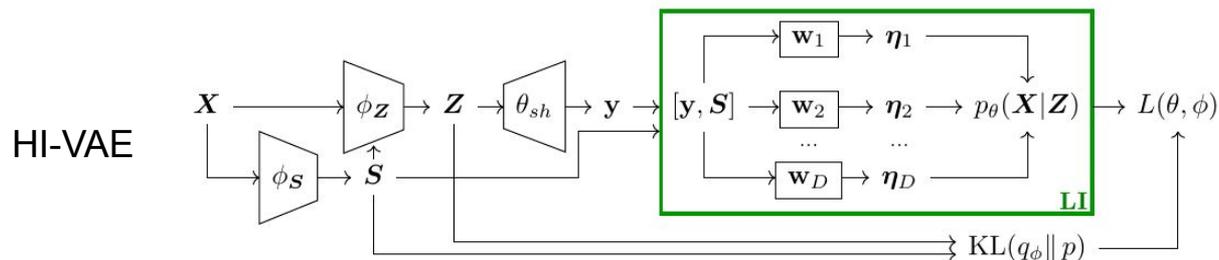


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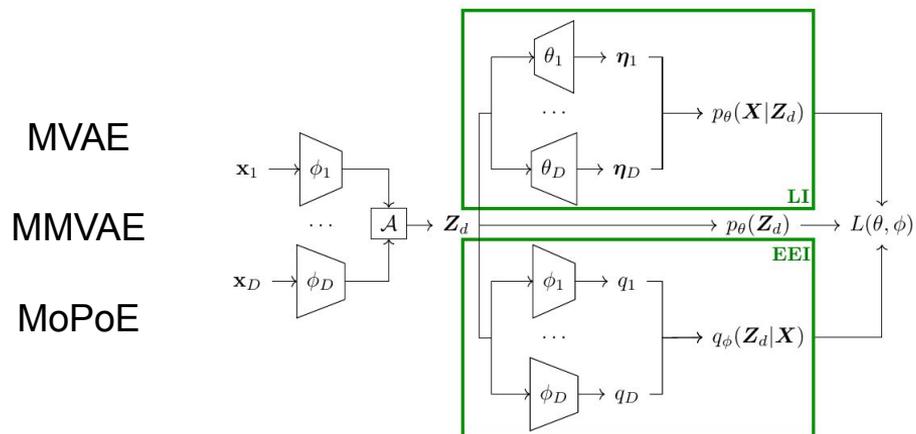
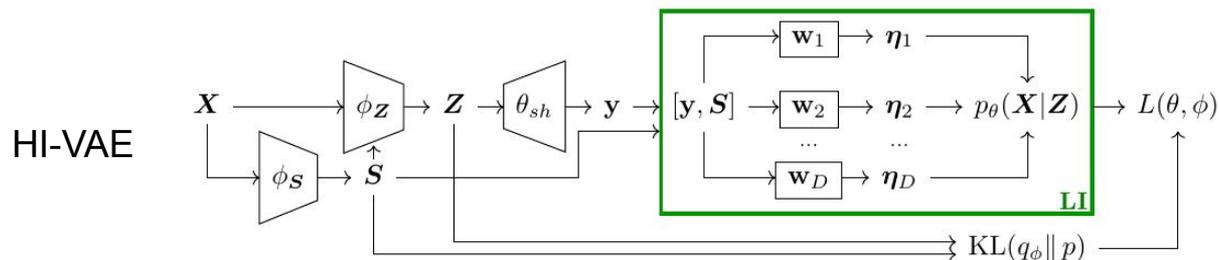


Two impartiality blocks:
One for y
One for S

VAE extensions



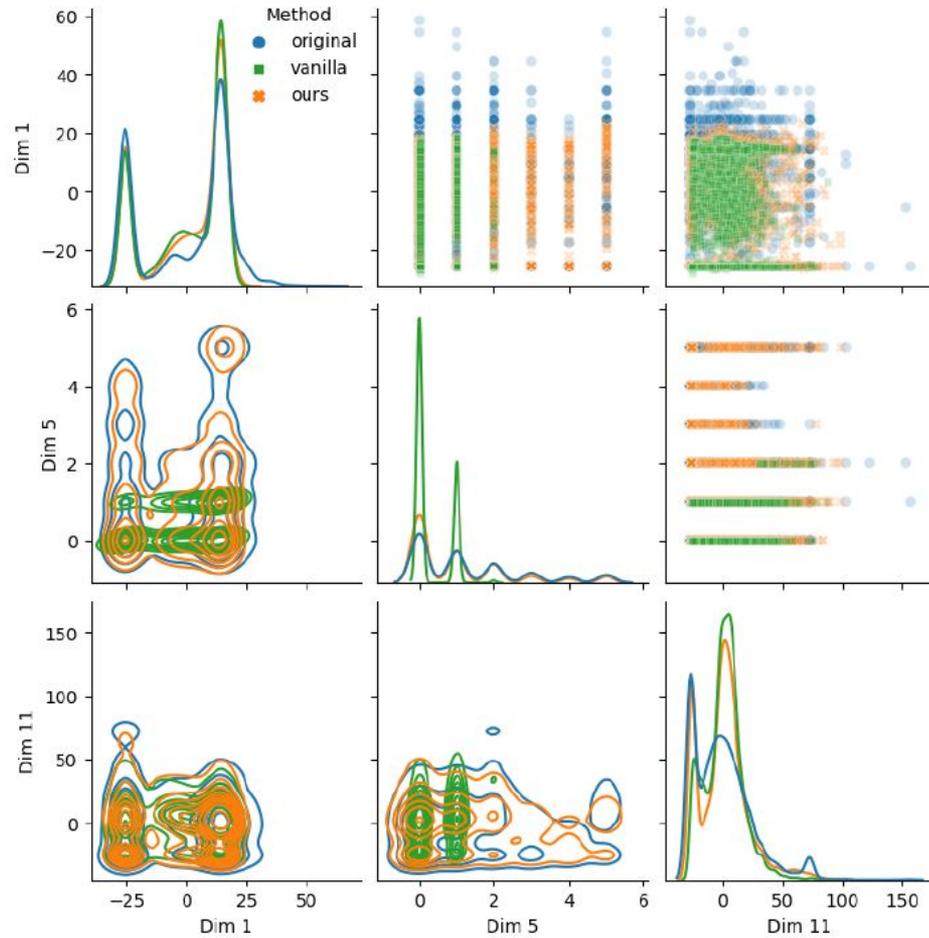
VAE extensions



Results – heterogeneous data

Table 1. Test reconstruction errors (median over five seeds) for different datasets and VAE models. Statistically different values according to a corrected paired t-test ($\alpha = 0.1$) are shown in bold. Models trained with our approach outperforms the baseline in most cases.

		Heterogeneous									Homogeneous			
		<i>Adult</i>	<i>Credit</i>	<i>Wine</i>	<i>Diam.</i>	<i>Bank</i>	<i>IMDB</i>	<i>HI</i>	<i>rwm5yr</i>	<i>labour</i>	<i>El Nino</i>	<i>Magic</i>	<i>BooNE</i>	
Standard VAE	ELBO	vanilla	0.213	0.128	0.086	0.187	0.203	0.082	0.170	0.105	0.109	0.109	0.064	0.042
		ours	0.104	0.041	0.071	0.139	0.043	0.032	0.041	0.026	0.063	0.068	0.058	0.039
	IWAE	vanilla	0.226	0.134	0.075	0.185	0.199	0.090	0.155	0.094	0.098	0.086	0.053	0.037
		ours	0.129	0.051	0.066	0.125	0.076	0.035	0.042	0.032	0.066	0.061	0.048	0.035
	DReG	vanilla	0.234	0.132	0.077	0.176	0.191	0.088	0.153	0.094	0.096	0.085	0.050	0.037
		ours	0.168	0.075	0.065	0.139	0.103	0.055	0.042	0.026	0.076	0.069	0.046	0.036
	HI-VAE	vanilla	0.127	0.107	0.126	0.114	0.141	0.079	0.105	0.044	0.100	0.098	0.062	0.039
		ours	0.081	0.060	0.117	0.011	0.095	0.049	0.109	0.024	0.069	0.015	0.033	0.038



Results – multimodal data

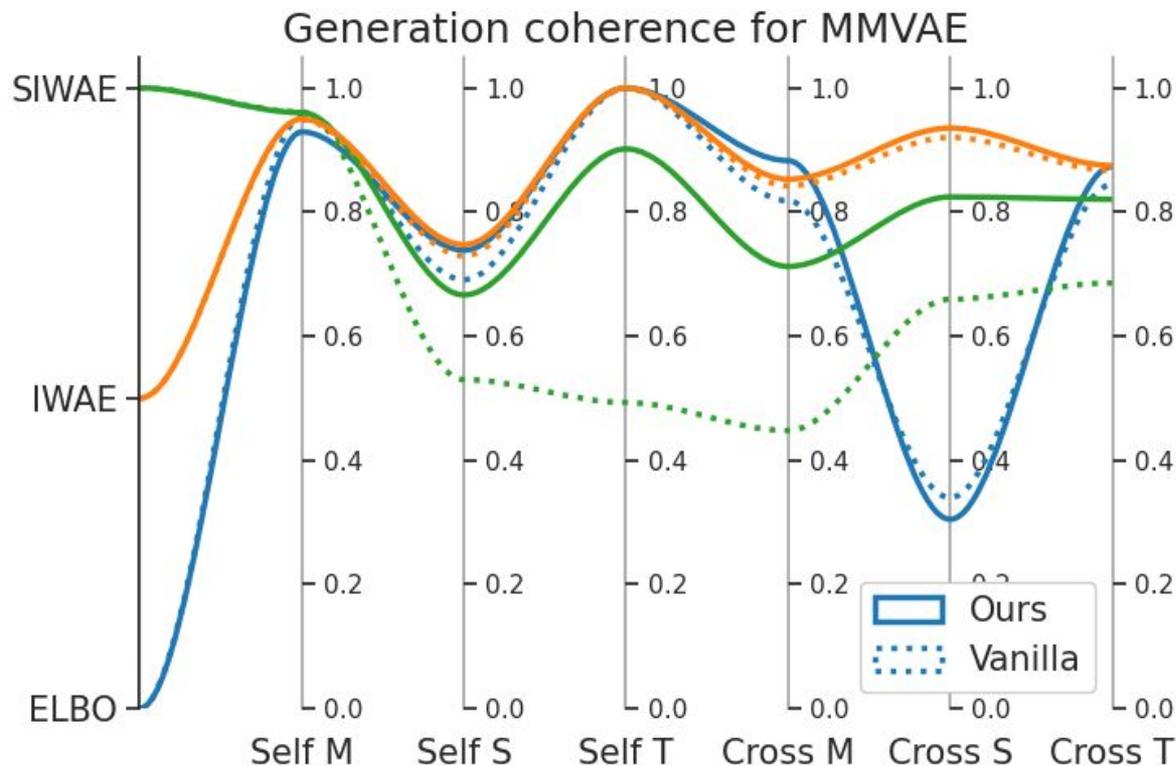
Table 5. Self and cross latent classification accuracy (%) for different models and losses on MNIST-SVHN-Text.

		ELBO	IWAE	SIWAE
		Self latent classification		
MVAE	vanilla	69.68	69.14	68.58
	ours	69.95	69.06	69.75
MMVAE	vanilla	71.81	87.55	71.30
	ours	87.83	90.78	85.55
MoPoE	vanilla	89.85	87.23	67.58
	ours	91.47	90.74	69.26
		Cross latent classification		
MVAE	vanilla	33.60	39.15	38.36
	ours	35.25	49.73	46.23
MMVAE	vanilla	44.25	76.81	40.60
	ours	71.42	84.80	60.50
MoPoE	vanilla	66.14	83.71	40.36
	ours	84.52	90.48	53.24

Table 9. Reconstruction coherence ($A = \{M, S, T\}$) for each modality, model, and dataset.

		ELBO			IWAE			SIWAE		
x_d		M	S	T	M	S	T	M	S	T
MVAE	vanilla	97.53	88.26	99.30	97.27	87.19	98.76	97.37	87.47	98.83
	ours	97.85	89.65	99.64	98.28	89.01	99.93	97.42	87.63	99.20
MMVAE	vanilla	86.01	45.59	89.17	85.25	84.03	88.66	58.95	61.27	63.27
	ours	89.42	45.83	91.54	87.55	86.87	90.93	74.85	73.89	81.09
MoPoE	vanilla	95.72	85.86	98.01	95.82	87.55	97.93	75.10	67.16	76.61
	ours	96.50	93.60	99.14	97.29	92.93	99.00	96.91	89.01	99.28

Results – multimodal data



Make sure to follow us!



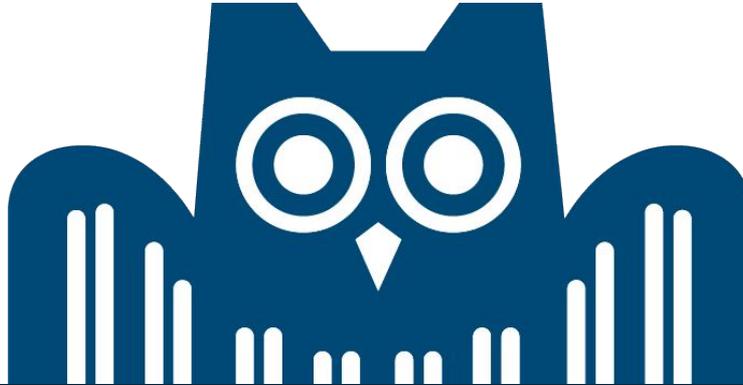
@javaloyML



@maryam_meghdadi



@IValeraM



Gradient conflict in multimodal VAEs

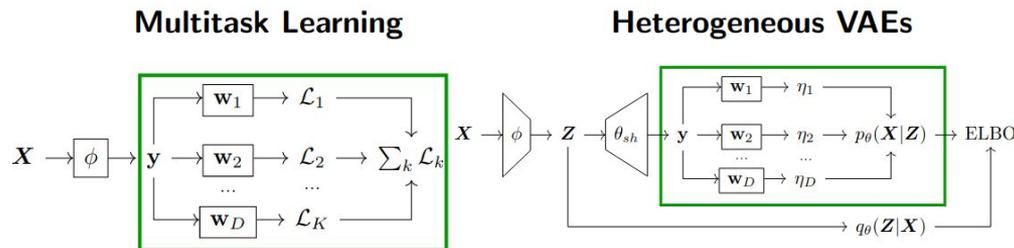


Table 3. Reconstruction coherence ($A = \{M, S, T\}$) for each modality and model, trained using SIWAE.

	x_d	M	S	T
MVAE	vanilla	97.37	87.47	98.83
	ours	97.42	87.63	99.20
MMVAE	vanilla	58.95	61.27	63.27
	ours	74.16	68.93	78.17
MoPoE	vanilla	75.10	67.16	76.61
	ours	96.91	89.01	99.28

Want: Learn all tasks equally well. **Want:** Model all features equally well.

Problem: Negative transfer.

Problem: Feature overlooking.

Shared params: ϕ .

Shared params: ϕ and θ_{sh} .

Excl. params: w_1, w_2, \dots, w_K .

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Updating ϕ :

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$$\nabla_{\phi} \mathcal{L} = \nabla_{\phi} \mathbf{y} \left(\underbrace{\sum_k \nabla_{\mathbf{y}} \mathcal{L}_k}_{\text{negative transfer}} \right)$$

$$\begin{aligned} \nabla_{\phi} p_{\theta} \nabla_{p_{\theta}} \text{ELBO} &= \\ &= \nabla_{\phi} \mathbf{y} \left(\underbrace{\sum_d \nabla_{\mathbf{y}} \eta_d \nabla_{\eta_d} p_{\theta}}_{\text{feature overlooking}} \right) \nabla_{p_{\theta}} \text{ELBO} \end{aligned}$$

		<i>Adult Credit Wine</i>			
Standard VAE	ELBO	vanilla	0.213	0.128	0.086
	ours		0.104	0.041	0.071
IWAE	vanilla	0.226	0.134	0.075	
	ours		0.129	0.051	0.066
DReG	vanilla	0.234	0.132	0.077	
	ours		0.168	0.075	0.065
HI-VAE	vanilla	0.127	0.107	0.126	
	ours		0.081	0.060	0.117

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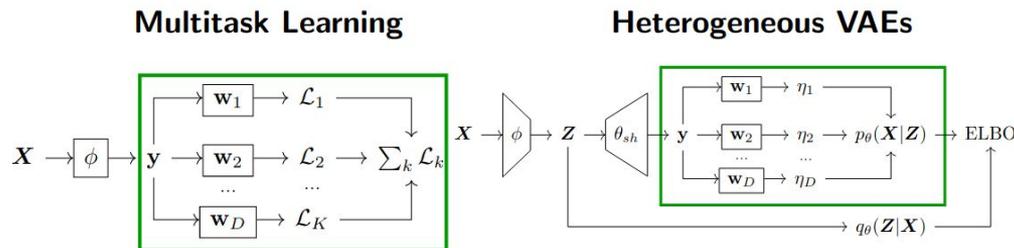


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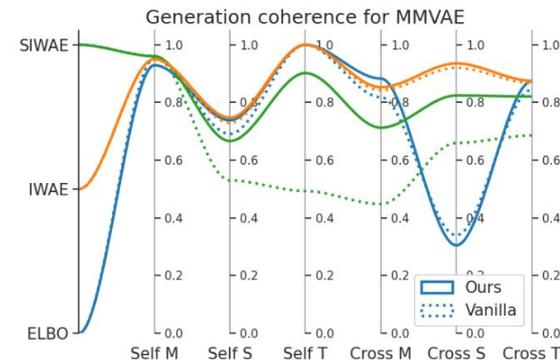
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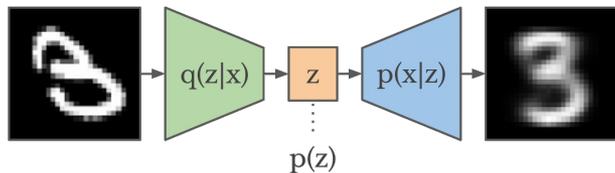
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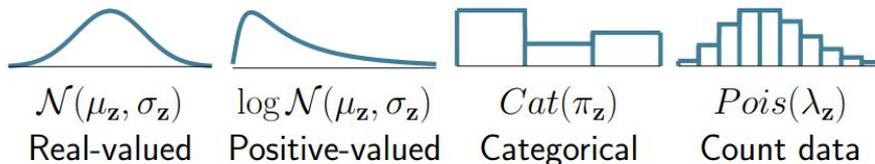
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$$\text{maximize}_{\theta, \phi} \mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})} [\log p_{\theta}(\mathbf{x}|\mathbf{z})] - \text{KL}(q_{\phi}(\mathbf{z}|\mathbf{x}) \| p(\mathbf{z}))$$

- **Heterogeneous data.** Each feature \mathbf{x}_d is of a different type:



Thus, a heterogeneous likelihood is of the form

$$p_{\theta}(\mathbf{X}|\mathbf{z}) = \prod_{d=1}^D p_d(\mathbf{x}_d|\mathbf{z}).$$

Likelihood impartiality

All dimensions are equally important. We want a learning process impartial to the likelihood of each of the dimensions.

We noticed

Each modality is of a different type:

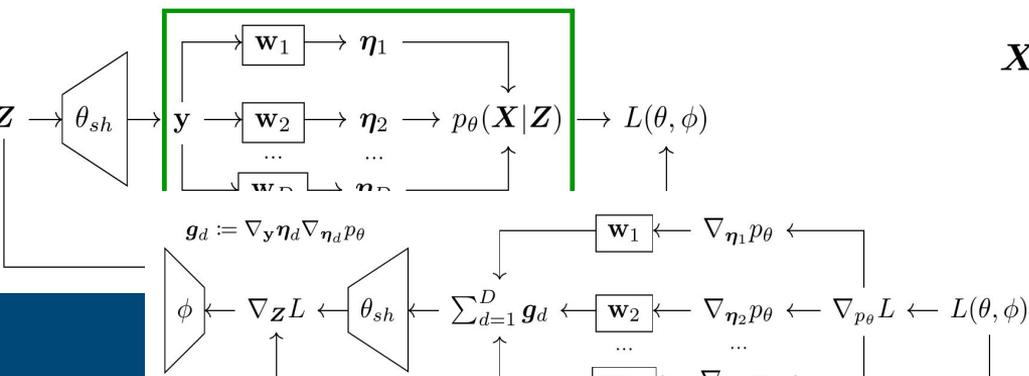
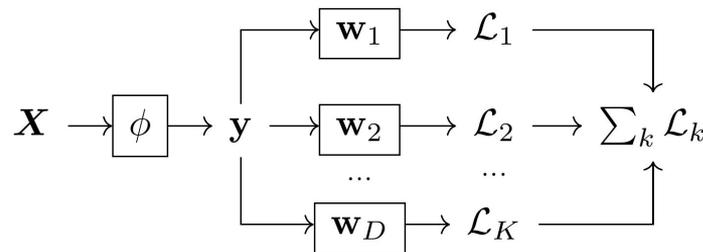
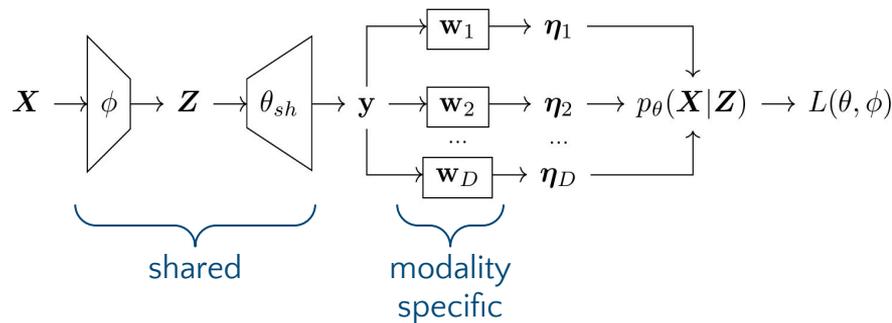
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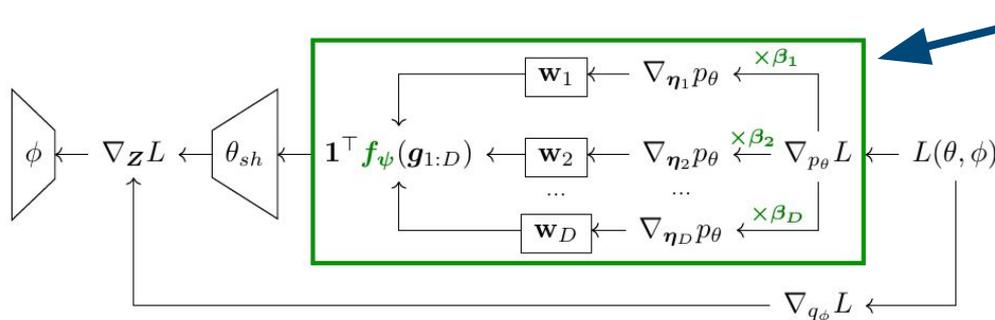
Real-valued Positive-valued




$Cat(\pi_{\mathbf{z}})$ $Pois(\lambda_{\mathbf{z}})$

Categorical Count data





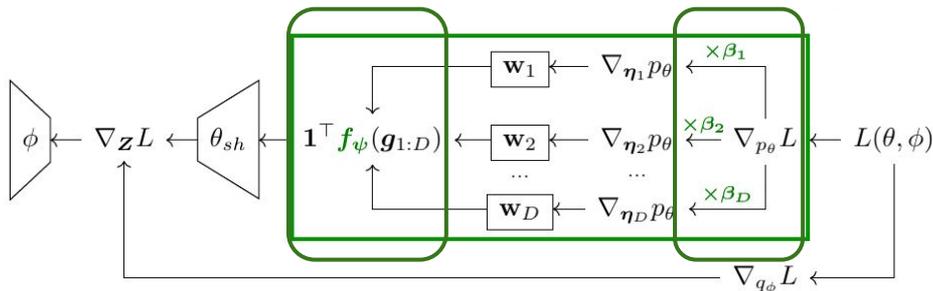
Impartiality block

- Input: shared
- Split-and-merge structure
- Suffers gradient conflict
- Two-step solution:
 - Local step, β : re-scale grads to make them comparable.
 - Global step, f : apply an MTL algorithm to alleviate gradient conflict.
- *Local* character
 - Anywhere
 - More than once

Algorithm 1 Backward pass within the impartiality block.

- 1: **Input:** Output gradient, $\nabla_{p\theta} L$.
- 2: **for** $d = 1$ **to** D **do**
- 3: $h_d \leftarrow \beta_d \nabla_{\eta_d p \theta} \nabla_{p\theta} L$
- 4: $\nabla_{\omega_d} L \leftarrow \nabla_{\omega_d} \eta_d \cdot h_d$
- 5: $g_d \leftarrow \nabla_y \eta_d \cdot h_d$
- 6: **end for**
- 7: $\tilde{g}_{1:D} \leftarrow f_\psi(g_{1:D})$
- 8: **return** $\sum_d \tilde{g}_d$

How to achieve impartiality



The impartiality block is local!

Local/steps in solving the gradients to make the solution as good as possible

Does not depend on the different algorithms to alleviate gradient conflict.

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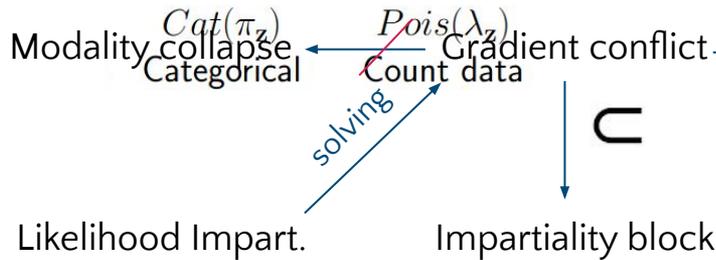
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Analyzing modality collapse

Each modality is of a different type:

$$p_{\theta}(\mathbf{X}|\mathbf{z}) = \prod_{d=1}^D p_d(\mathbf{x}_d|\mathbf{z})$$

Real-valued Positive-valued



Impartiality block

