

TACTiS

Transformer-Attentional Copula for Time Series



Alexandre Drouin



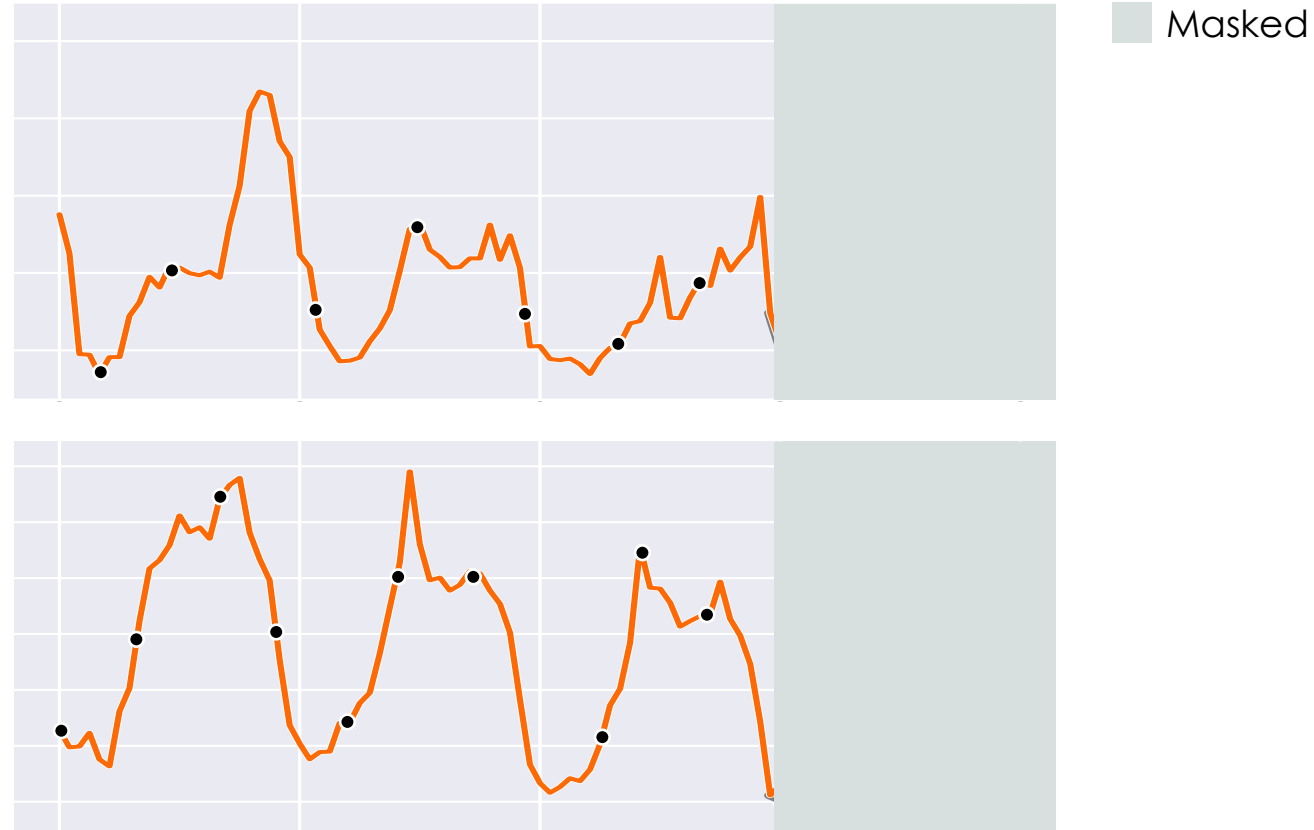
Étienne Marcotte



Nicolas Chapados

Objective

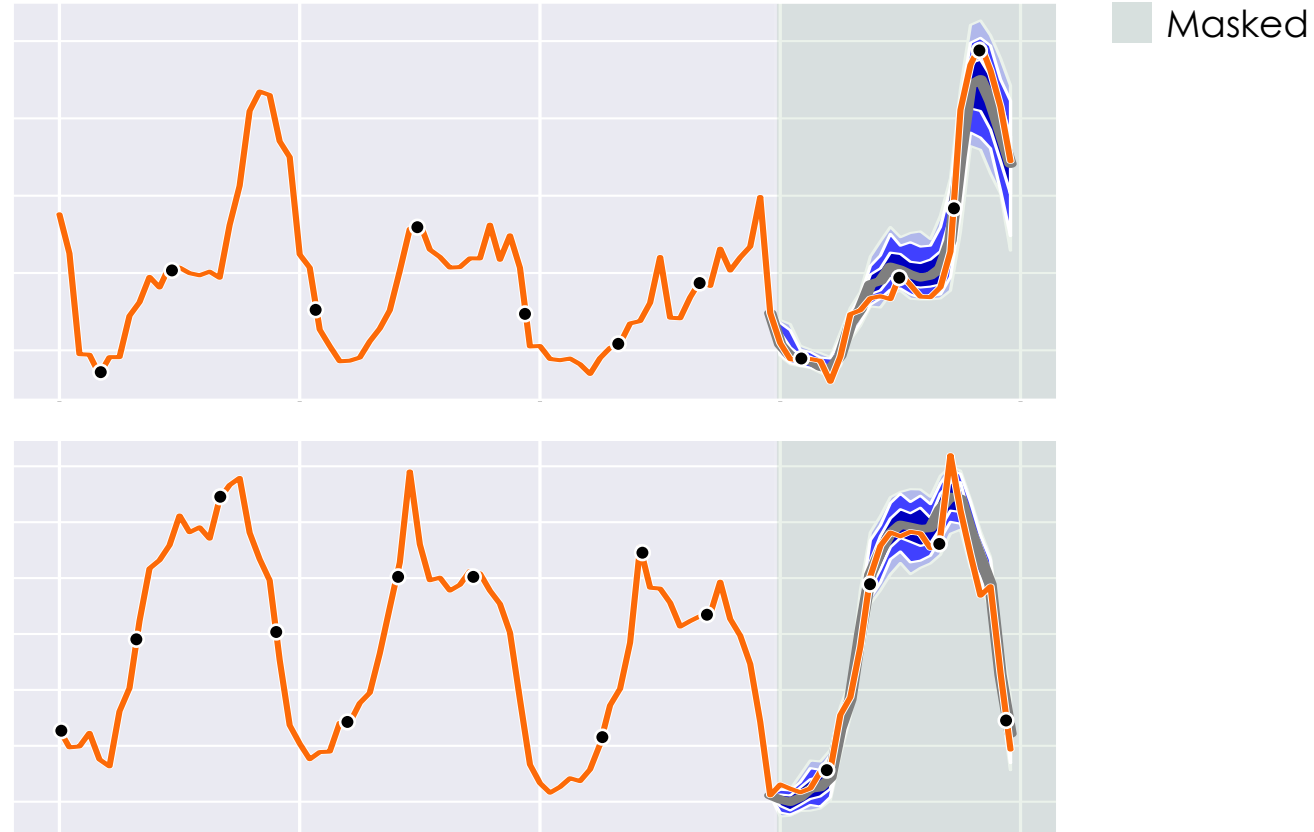
Goal: Infer the joint distribution of masked time points, given the observed time points



Very general: forecasting, interpolation, or arbitrary patterns

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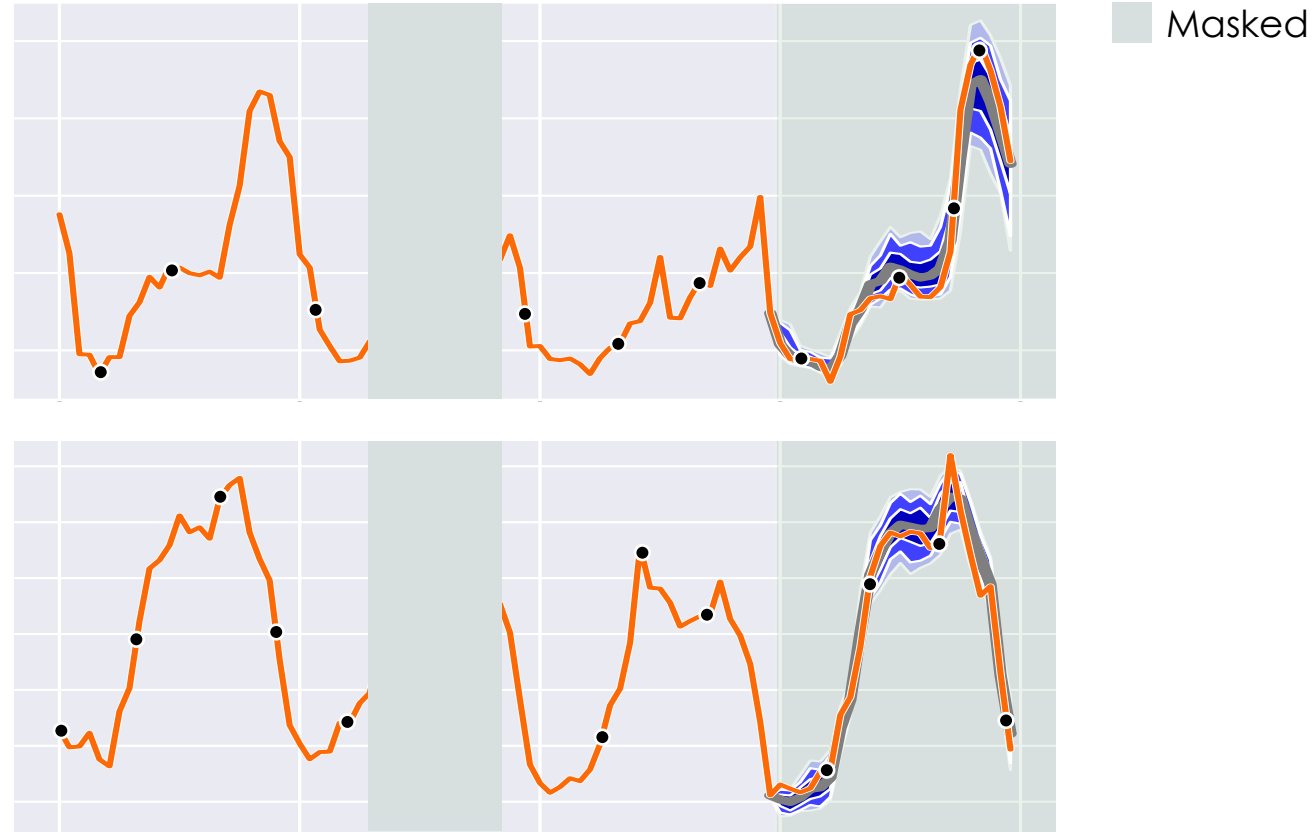
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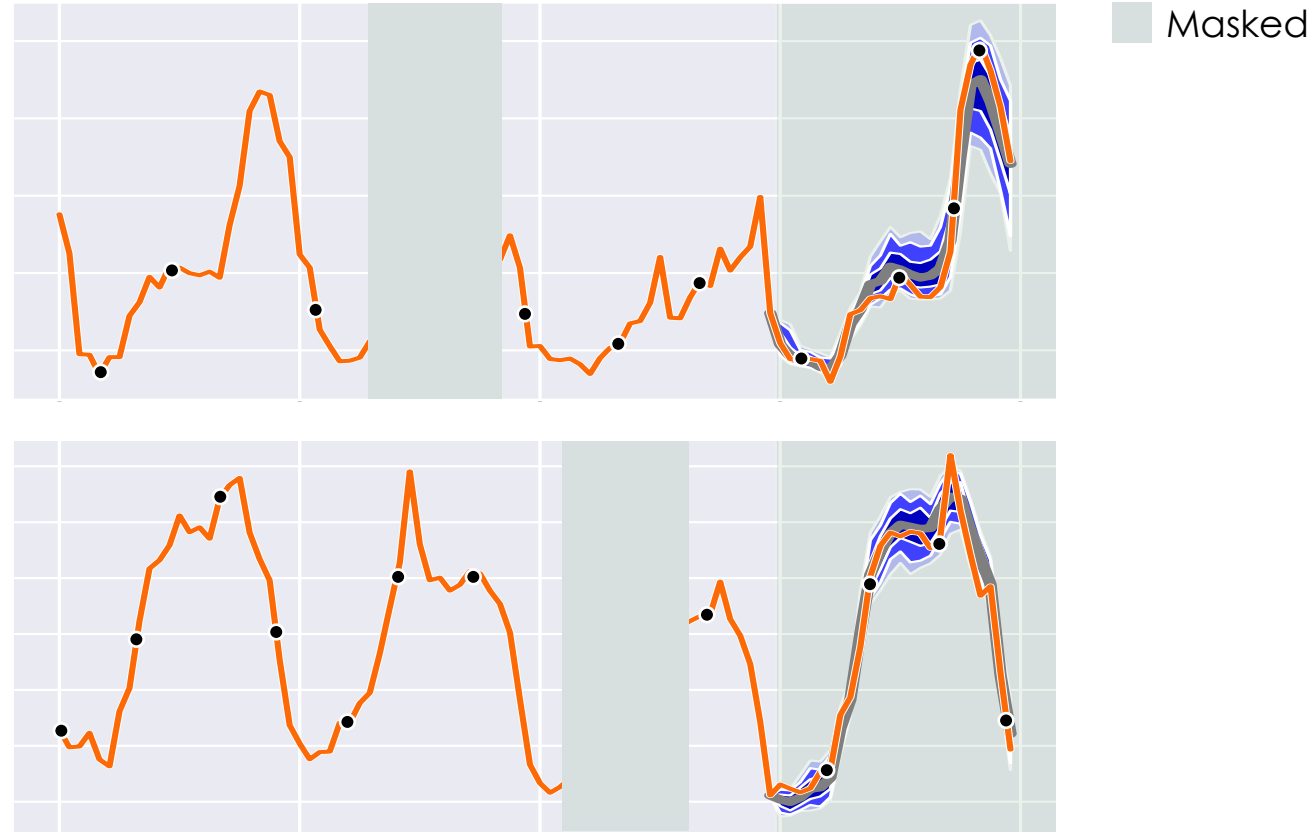
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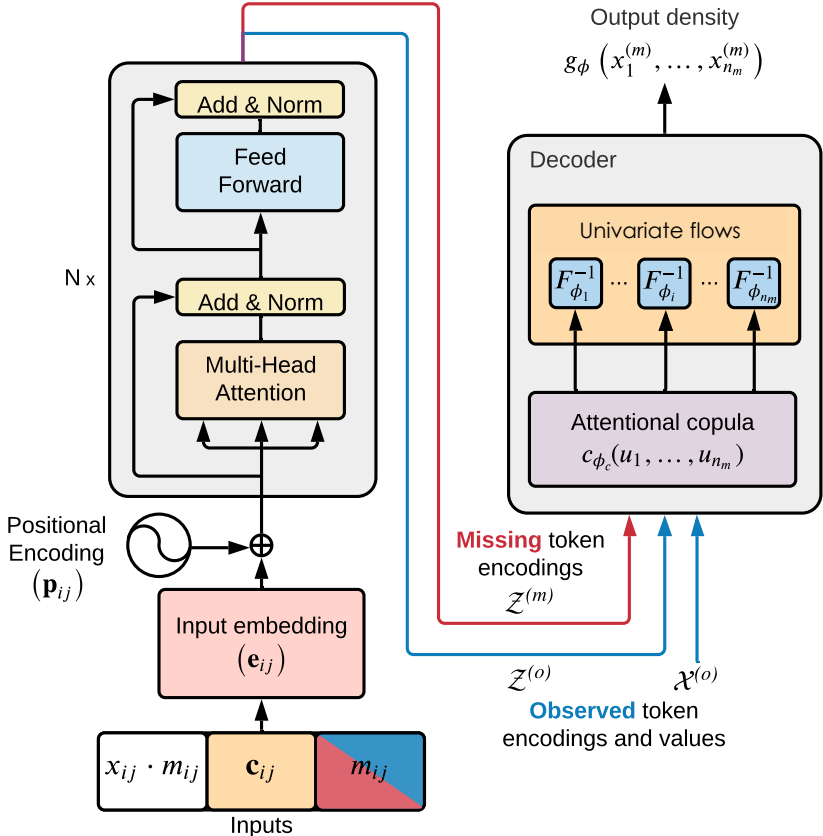
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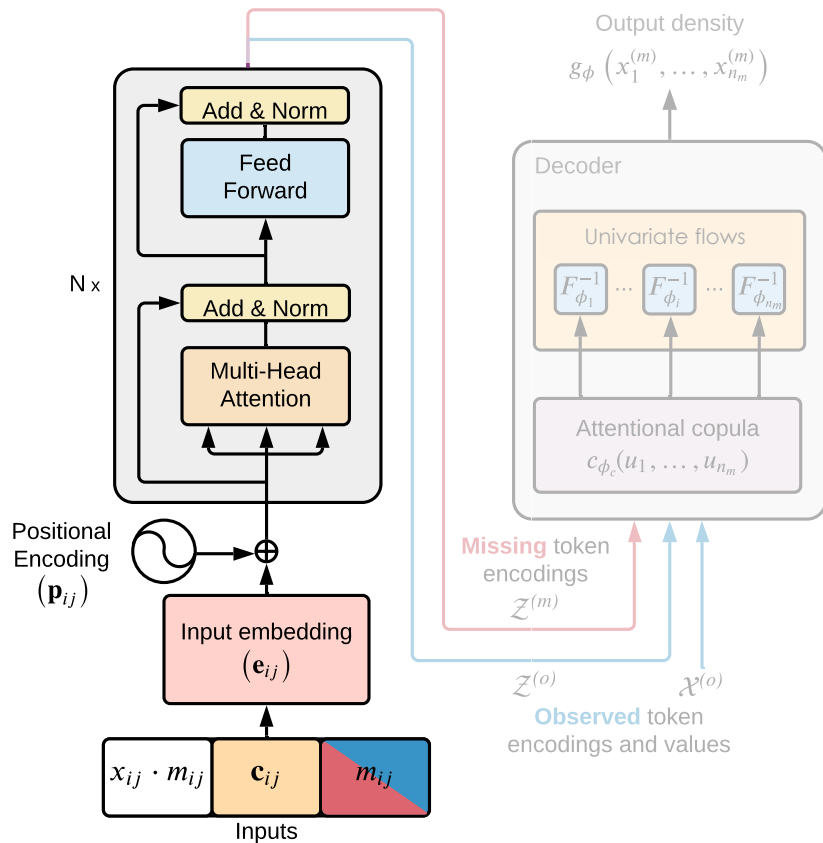
Overview of the model

TACTiS is an encoder-decoder model, similar to standard transformers.

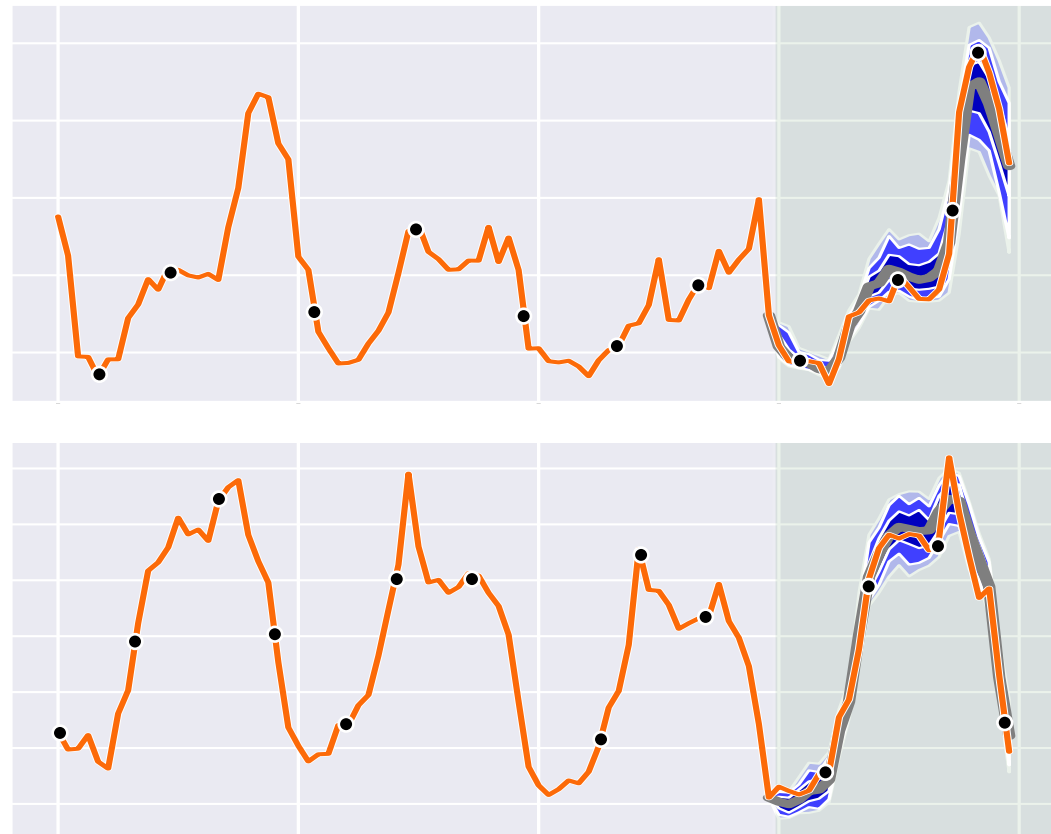


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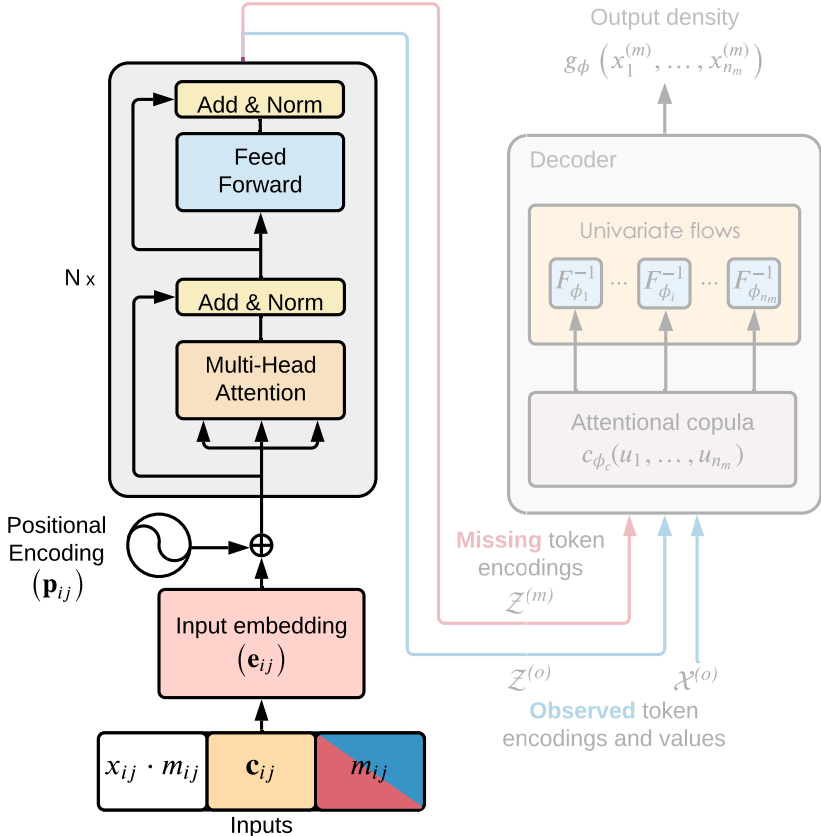


Encoder: each point in each time series is a token

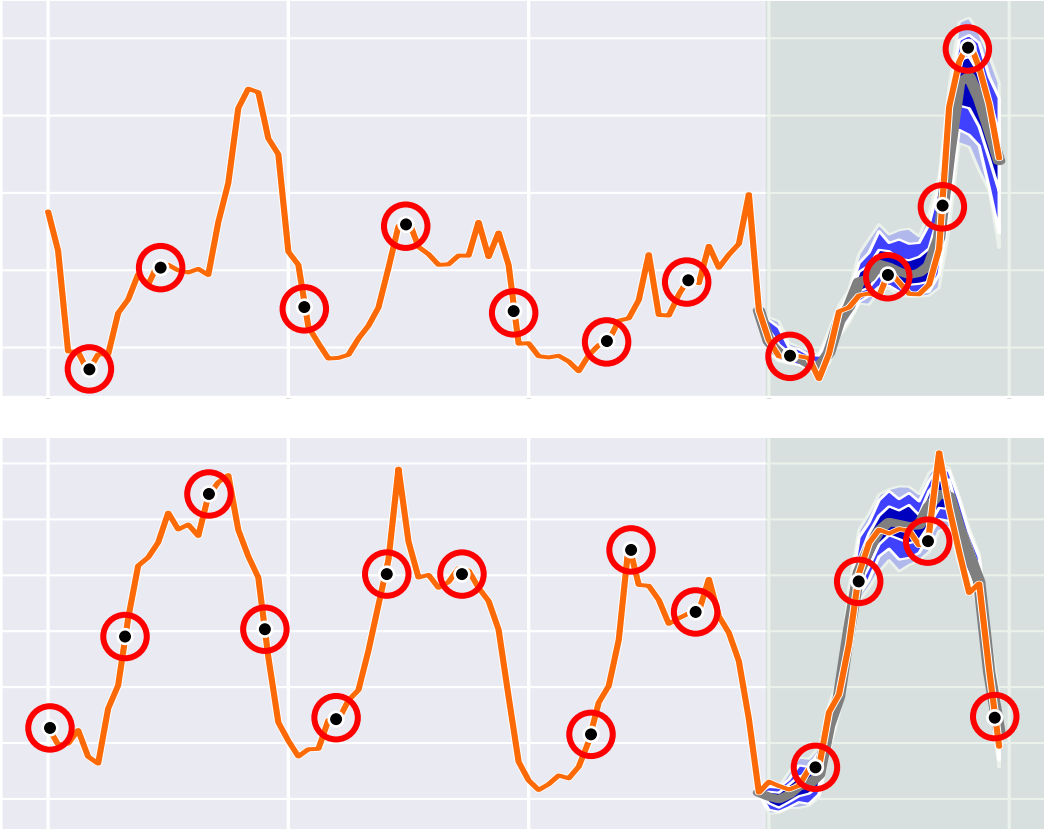


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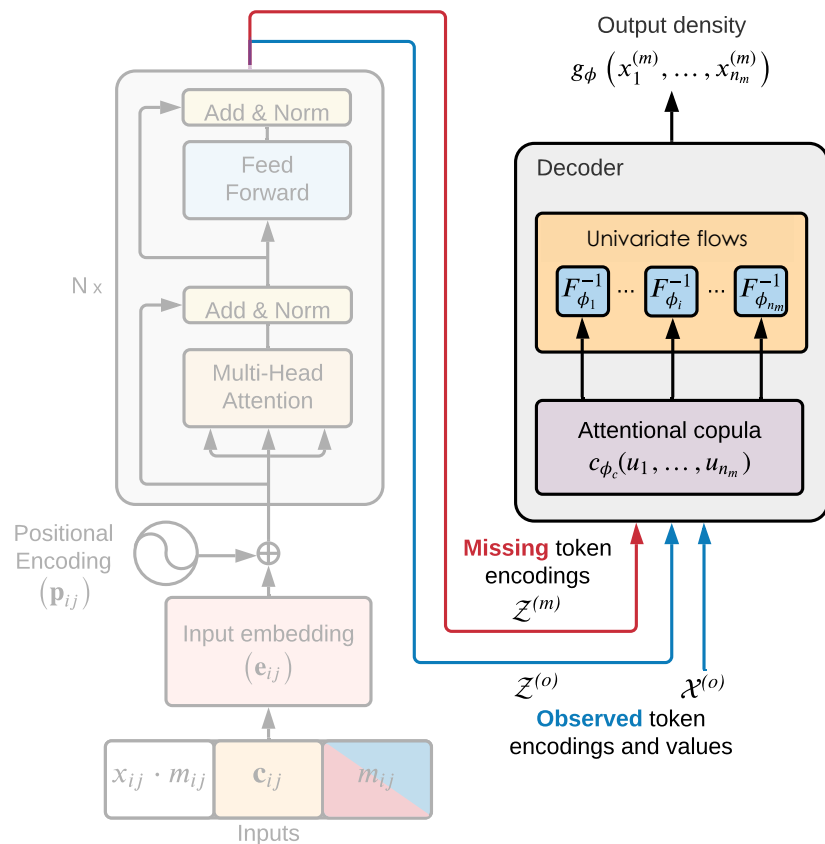


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Overview of the model

TACTiS is an encoder-decoder model, similar to standard transformers.



Decoder: a copula-based autoregressive decoder

Theorem (Sklar): any joint distribution can be expressed as a combination of two components:

1. **Marginal** distribution of each variable
2. **Copula:** joint distribution on the unit cube

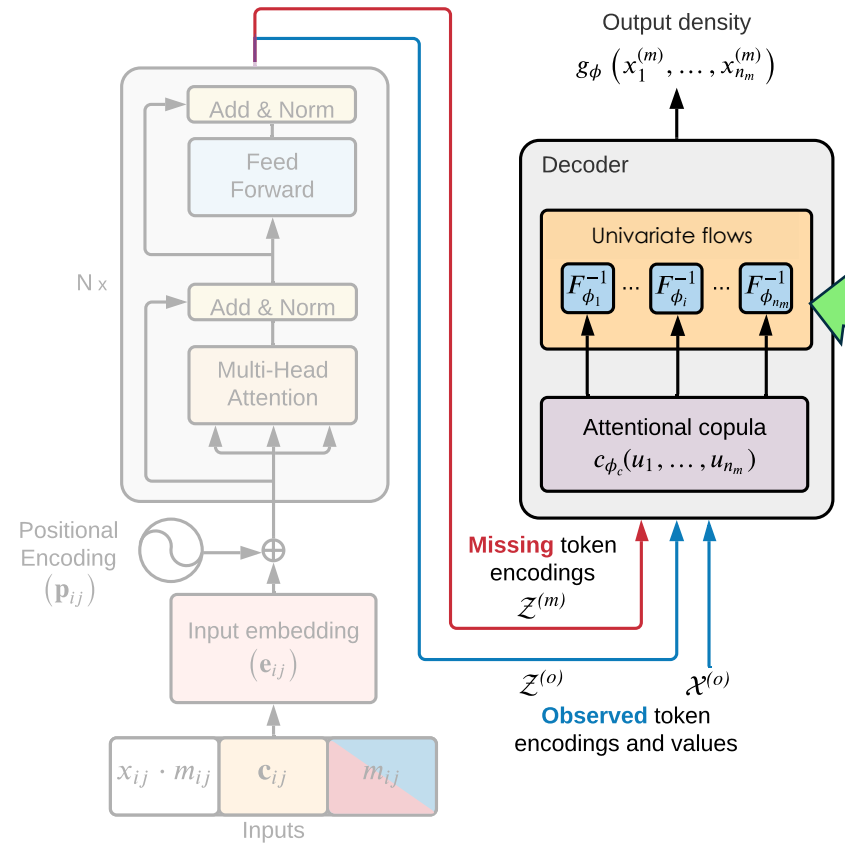
Why?

- Interpretability
- Robustness to distribution shifts

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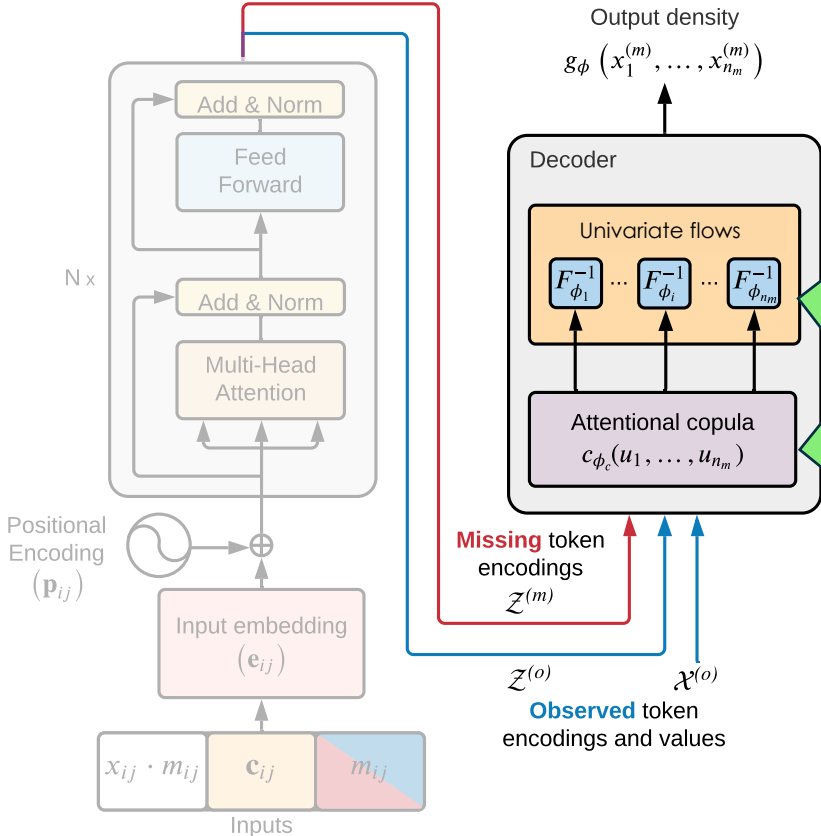
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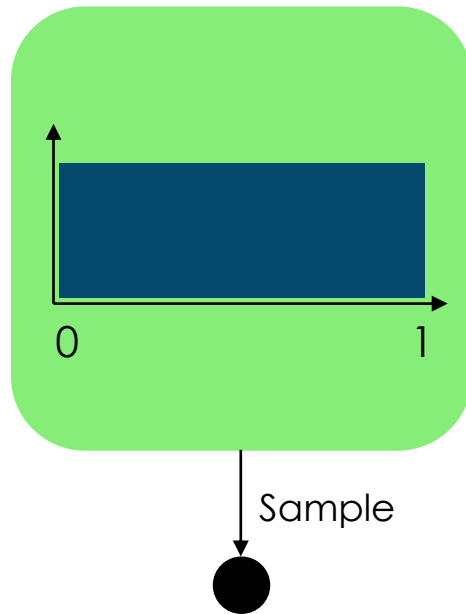
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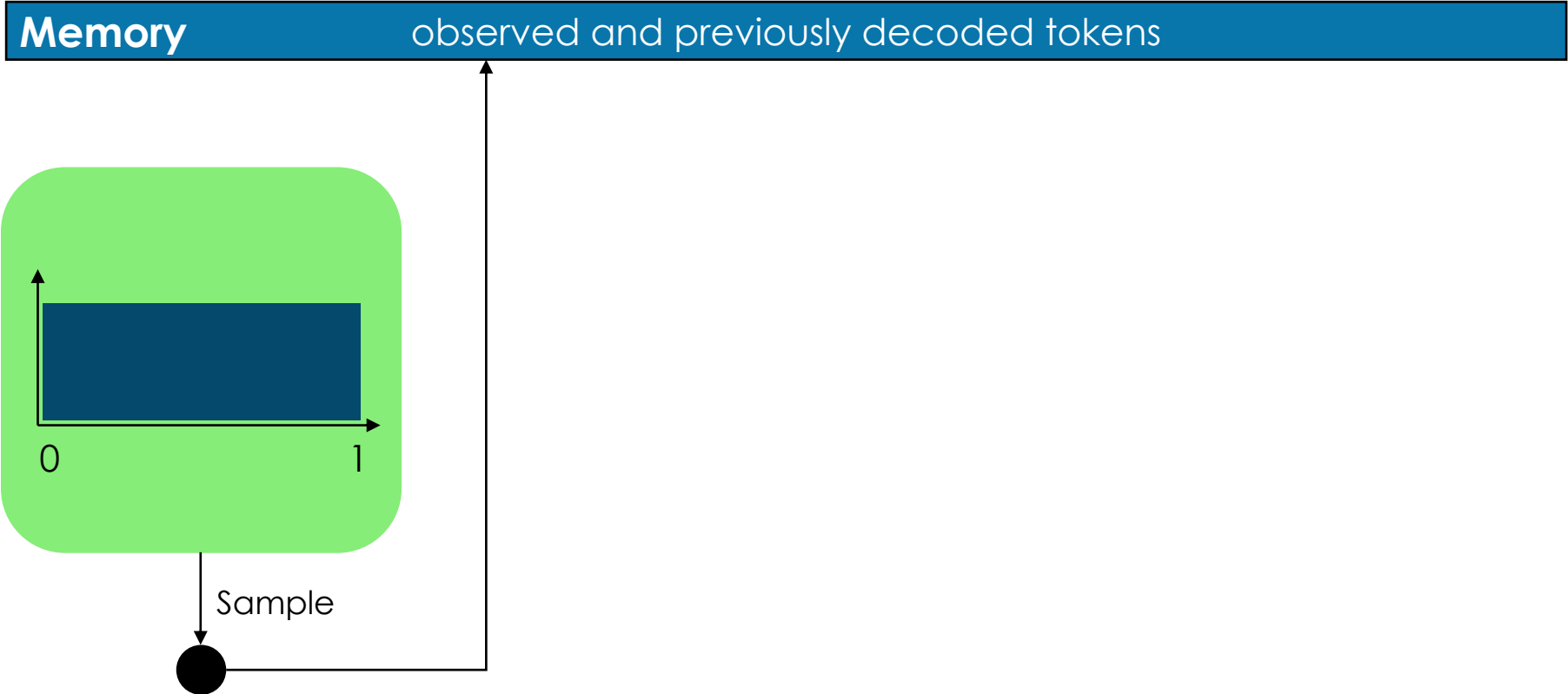
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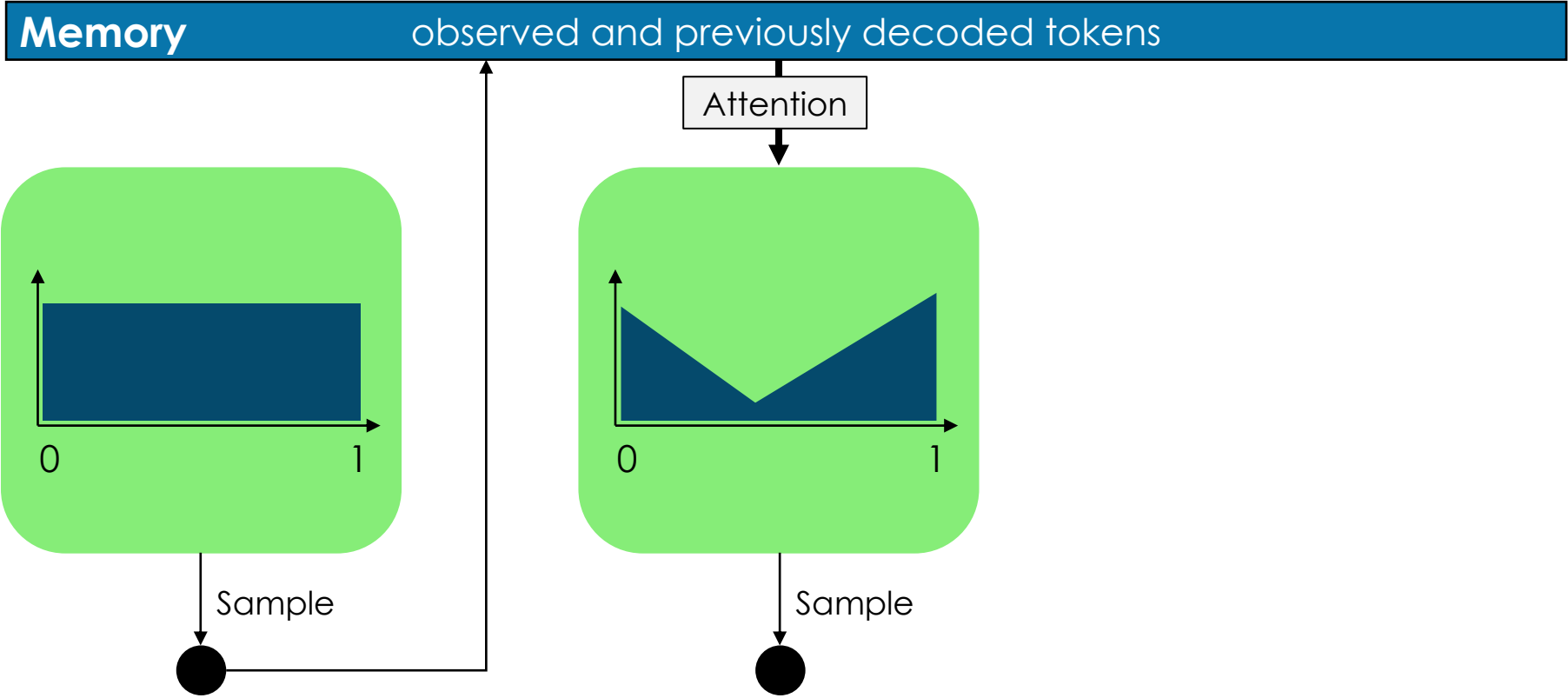
Decoding using attentional copulas



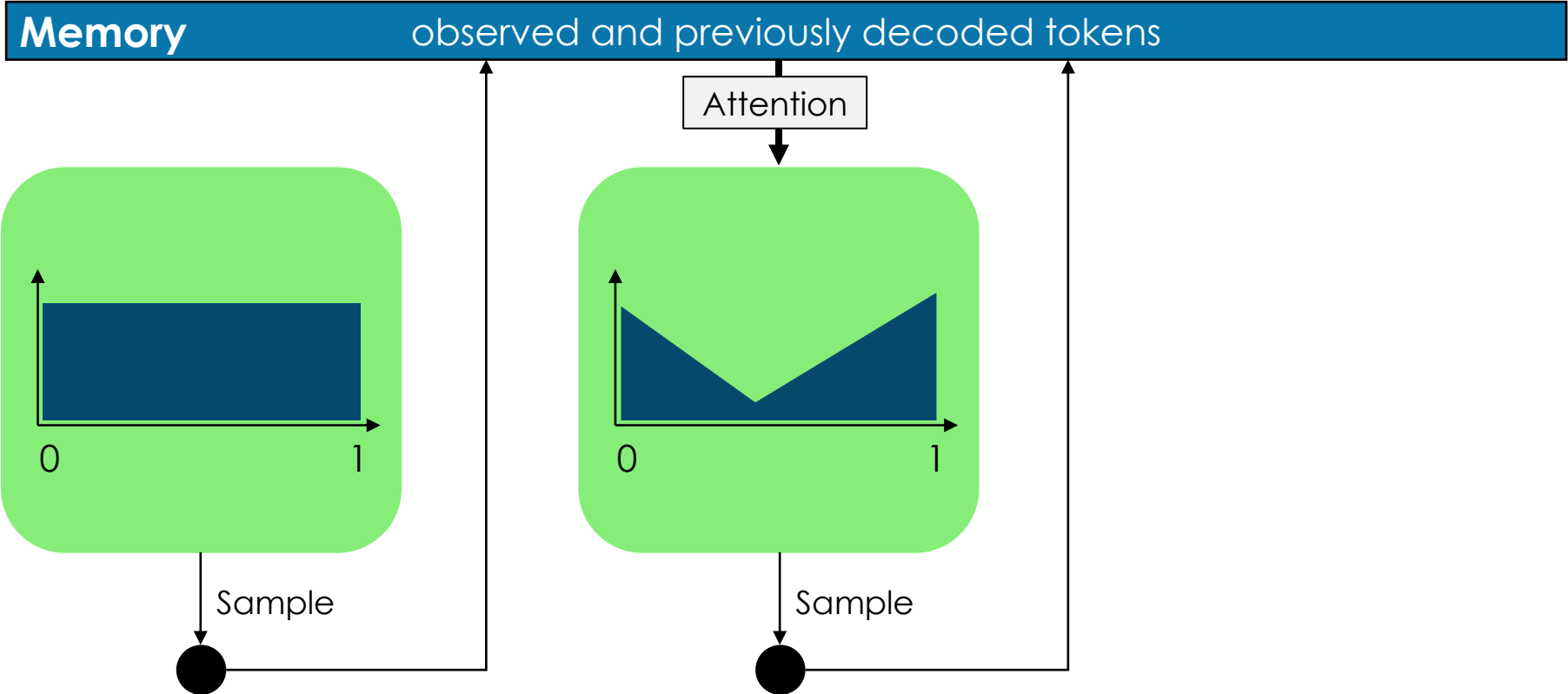
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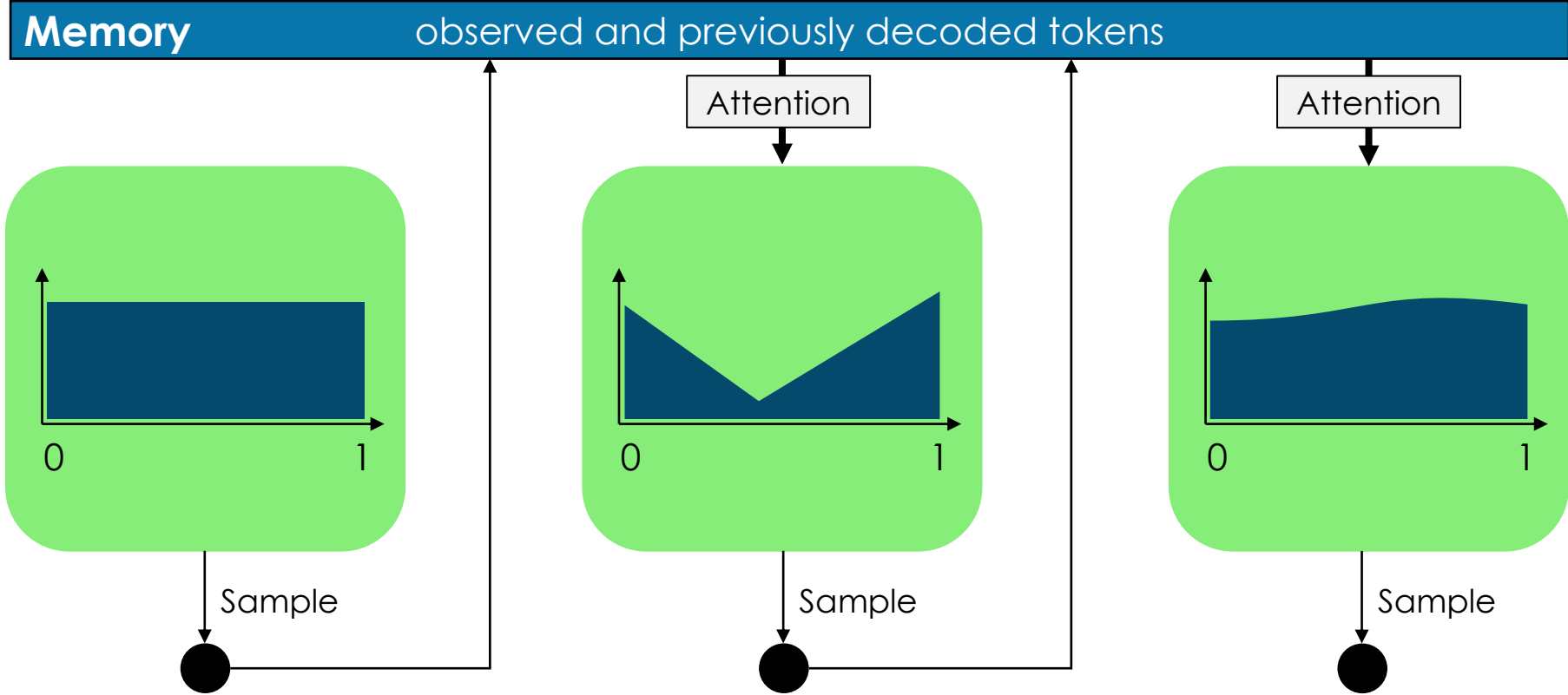
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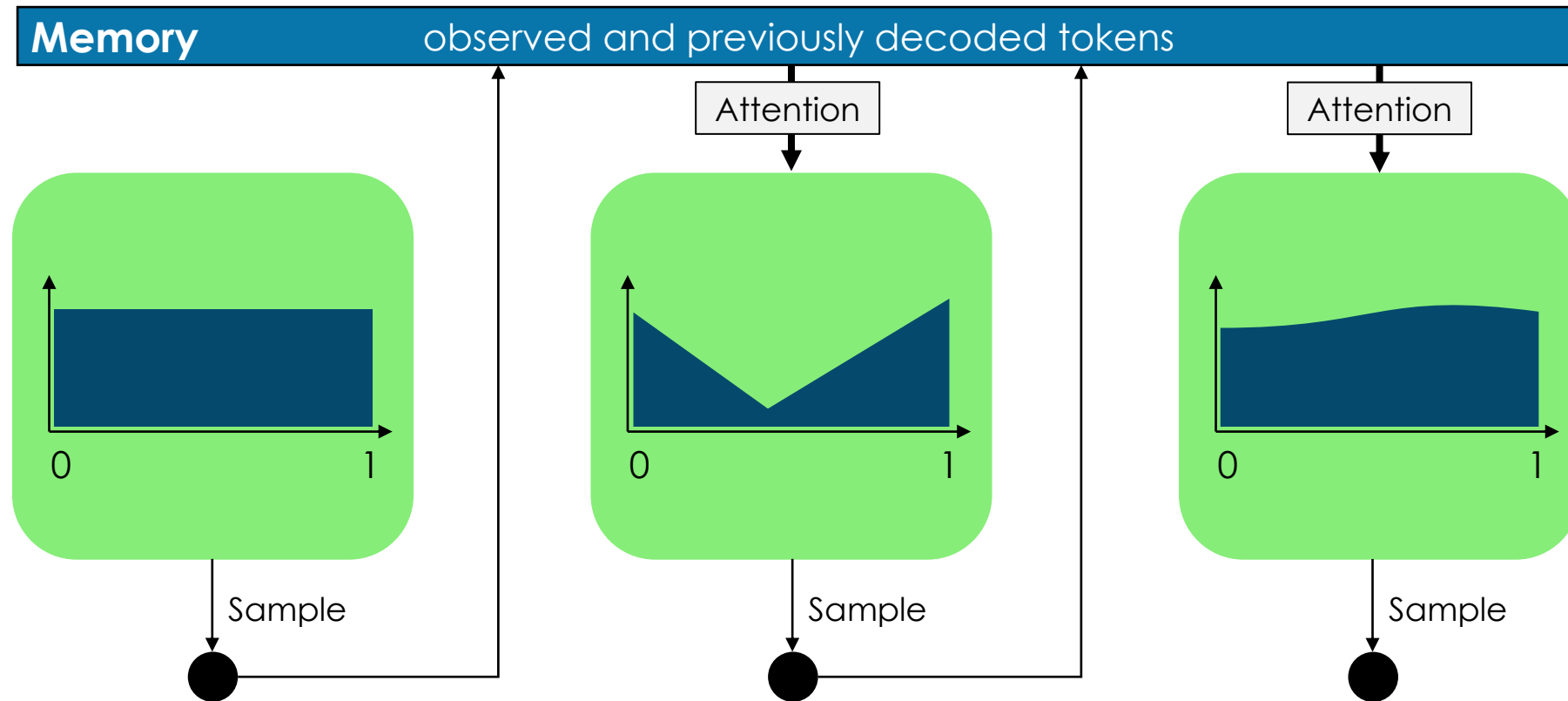
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Theorem: decoding in a **random order** guarantees convergence to **valid copulas**

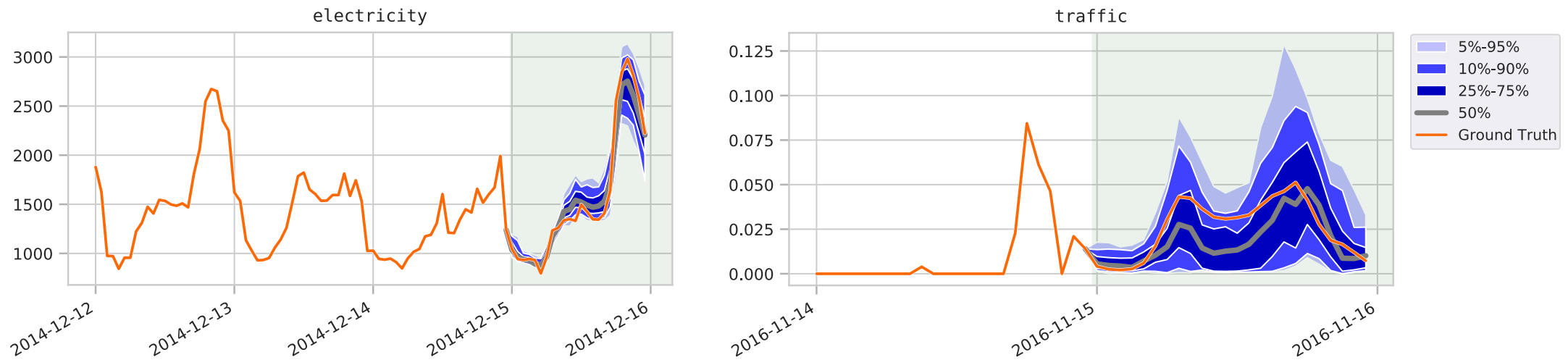
State-of-the-art forecasting performance

CRPS-Sum means (\pm standard errors). Lower is better. Best results in bold.

Model	electricity	fred-md	kdd-cup	solar-10min	traffic	Avg. Rank
Auto-ARIMA	0.077 \pm 0.016	0.043 \pm 0.005	0.625 \pm 0.066	0.994 \pm 0.216	0.222 \pm 0.005	4.7 \pm 0.3
ETS	0.059 \pm 0.011	0.037 \pm 0.010	0.408 \pm 0.030	0.678 \pm 0.097	0.353 \pm 0.011	4.4 \pm 0.3
TempFlow	0.075 \pm 0.024	0.095 \pm 0.004	0.250 \pm 0.010	0.507 \pm 0.034	0.242 \pm 0.020	3.9 \pm 0.2
TimeGrad	0.067 \pm 0.028	0.094 \pm 0.030	0.326 \pm 0.024	0.540 \pm 0.044	0.126 \pm 0.019	3.6 \pm 0.3
GPVar	0.035 \pm 0.011	0.067 \pm 0.008	0.290 \pm 0.005	0.254 \pm 0.028	0.145 \pm 0.010	2.7 \pm 0.2
TACTiS-TT	0.021 \pm 0.005	0.042 \pm 0.009	0.237 \pm 0.013	0.311 \pm 0.061	0.071 \pm 0.008	1.6 \pm 0.2

TACTiS outperforms **state-of-the-art** models on **real-world datasets** with **hundreds of time series**

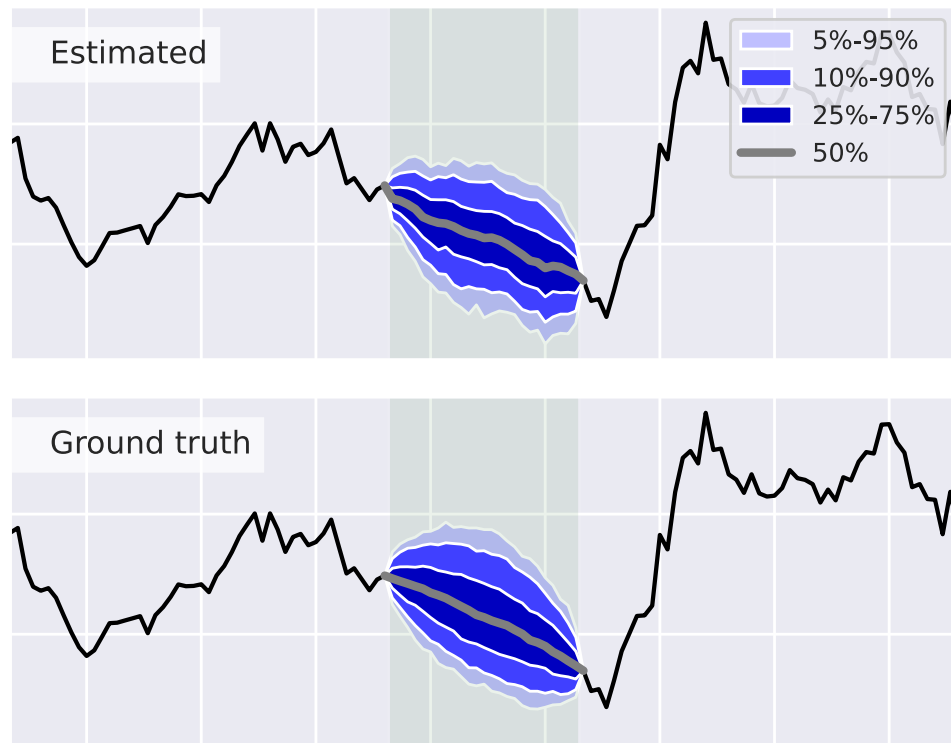
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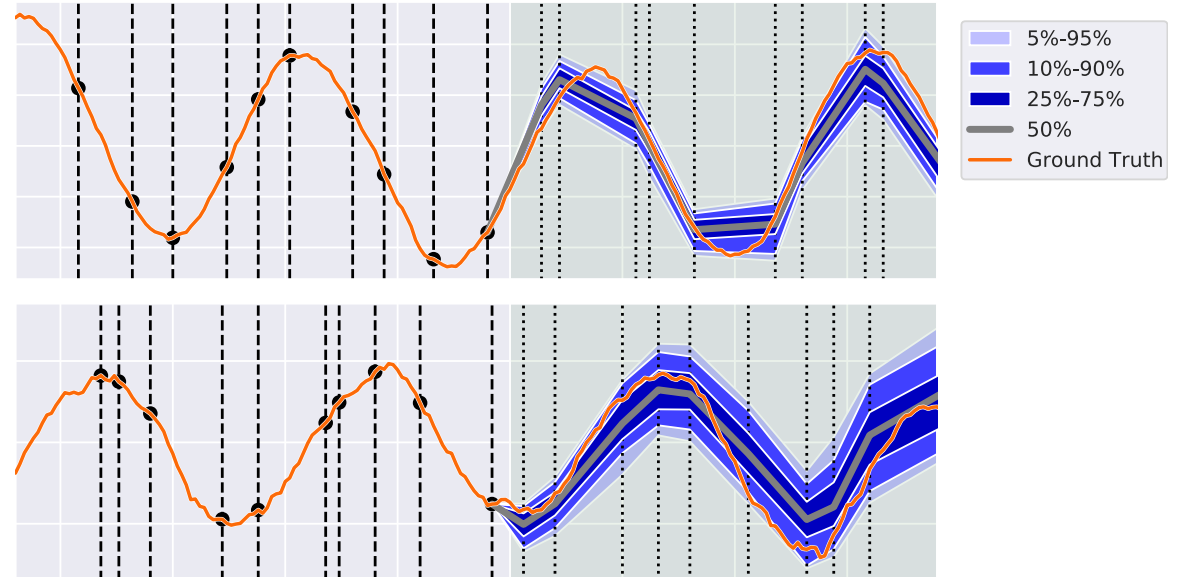
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TACTiS is very flexible

Interpolation



Unaligned and non-uniformly sampled data



Thank you!

Please come by our poster!

Code: <https://github.com/ServiceNow/TACTiS>

