

GenLabel: Mixup Relabeling using Generative Models

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Preview

- **Goal:** Data augmentation (DA) for robust ML
- **Motivation:** Classifiers are brittle to adversarial attacks
- **Key results:**



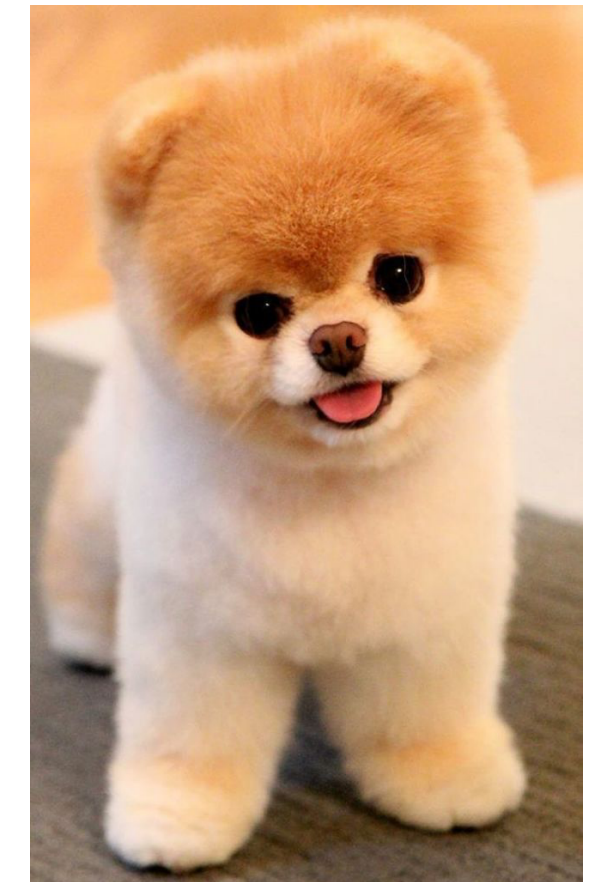
Preliminary: Mixup

cat dog
[1 0]



Feature x
Label y

cat dog
[0 1]



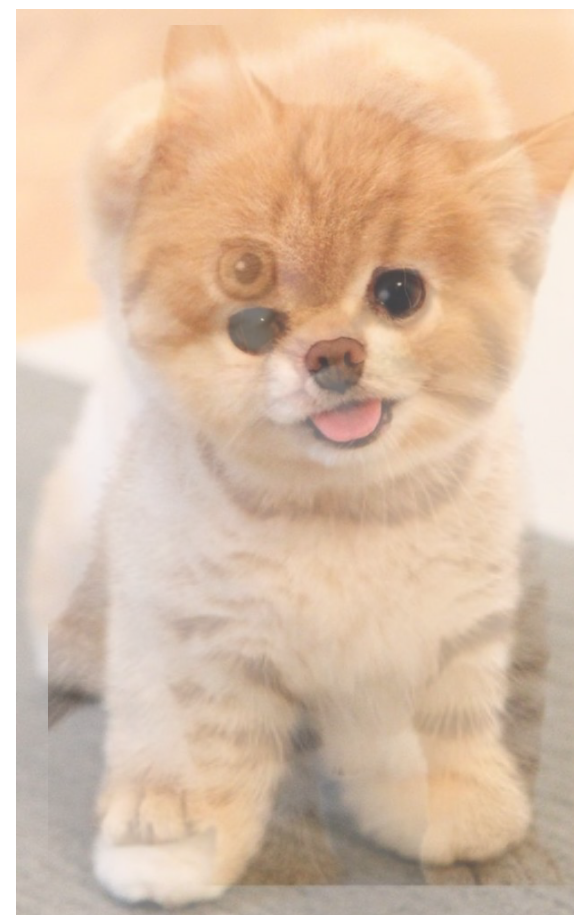
Feature x'
Label y'

Preliminary: Mixup

cat dog
[1 0]

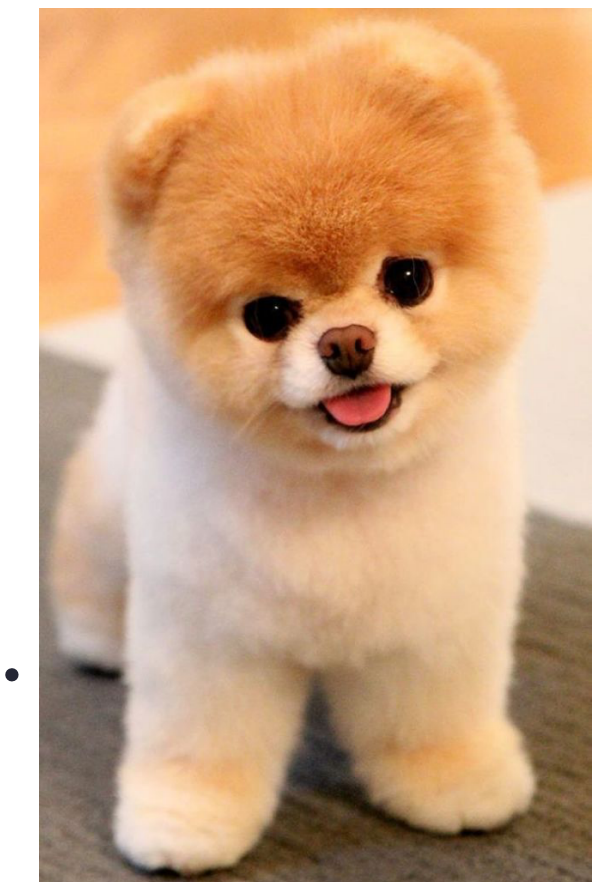


Feature \mathbf{x}
Label \mathbf{y}



cat dog
[0.5 0.5]

cat dog
[0 1]



Feature \mathbf{x}'
Label \mathbf{y}'

$$\begin{aligned}\text{Feature } \mathbf{x}^{\text{mix}} &= \lambda \mathbf{x} + (1 - \lambda) \mathbf{x}' \\ \text{Label } \mathbf{y}^{\text{mix}} &= \lambda \mathbf{y} + (1 - \lambda) \mathbf{y}'\end{aligned}$$

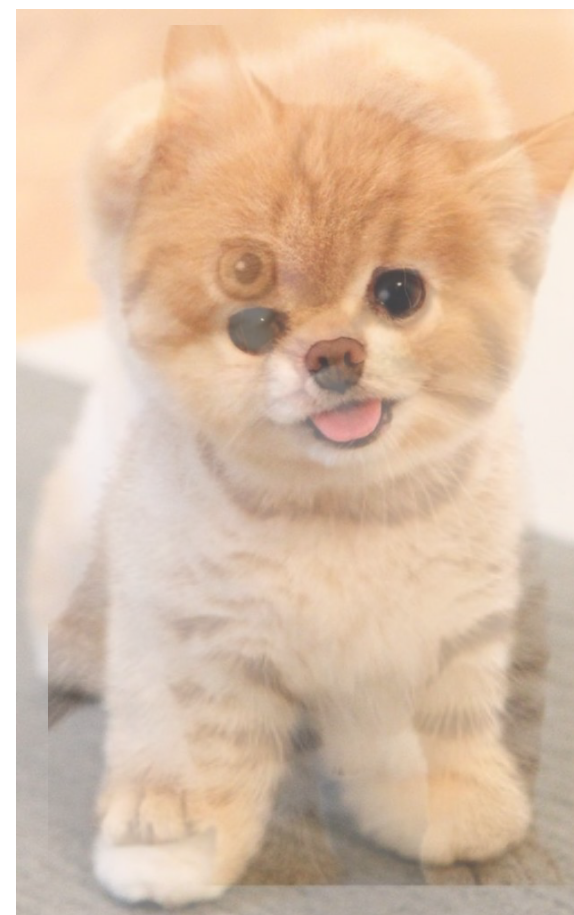
Mixup: Convex combination in
feature & label domain

Preliminary: Mixup

cat dog
[1 0]

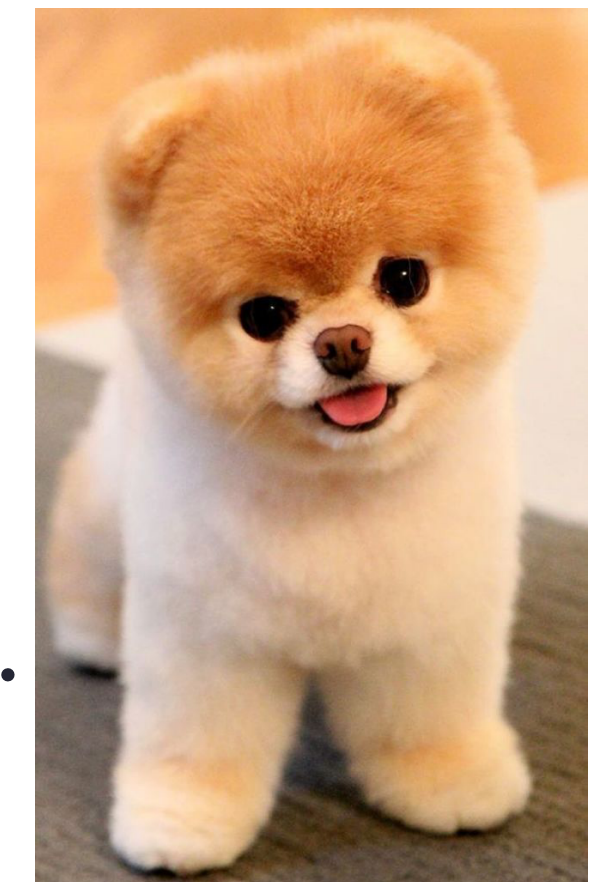


Feature x
Label y



cat dog
[0.5 0.5]

cat dog
[0 1]



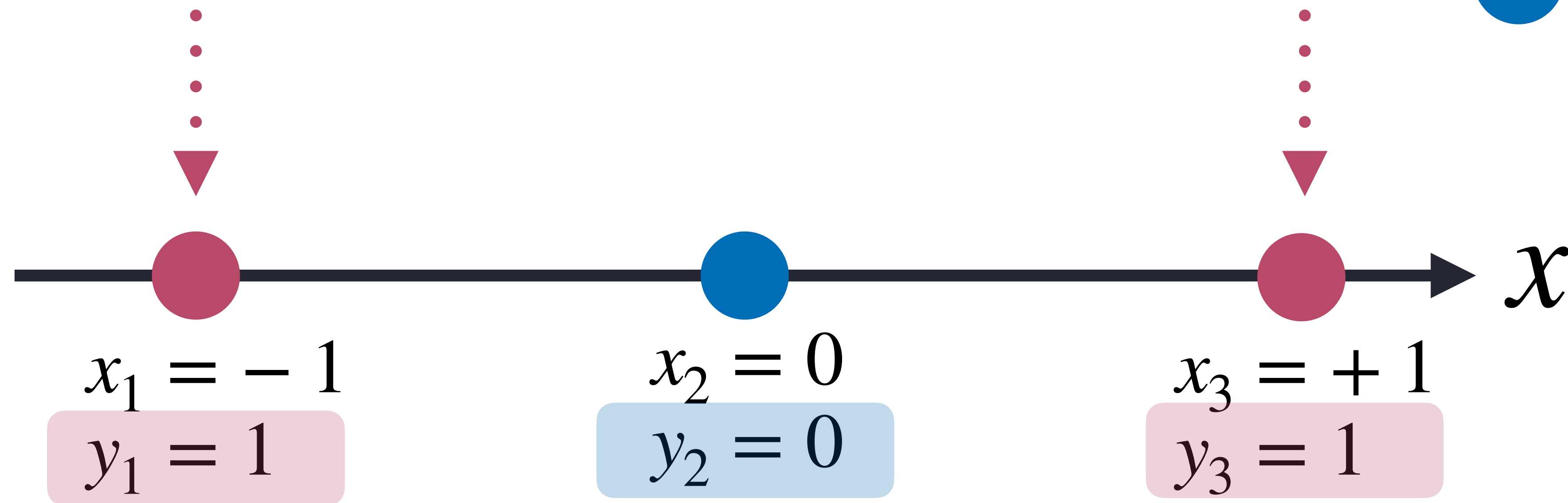
Feature x'
Label y'

$$\begin{aligned}\text{Feature } x^{\text{mix}} &= \lambda x + (1 - \lambda)x' \\ \text{Label } y^{\text{mix}} &= \lambda y + (1 - \lambda)y'\end{aligned}$$

Train with **mixup sample**
improves accuracy/robustness

Problem: Label Conflict

● : Class 1
● : Class 0



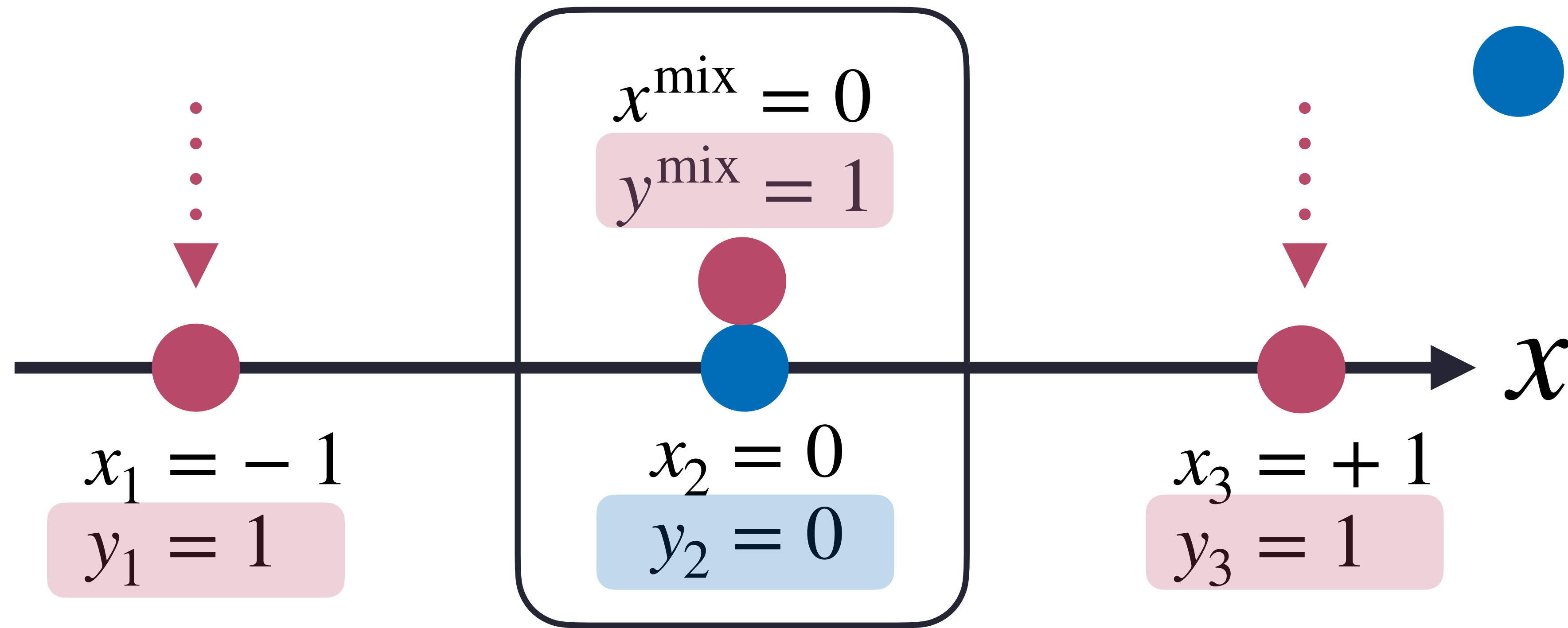
Mixing (x_1, y_1) and (x_3, y_3) generates

$$x^{\text{mix}} = 0.5x_1 + 0.5x_3 = 0$$

$$y^{\text{mix}} = 0.5y_1 + 0.5y_3 = 1$$

Problem: Label Conflict

● : Class 1
● : Class 0



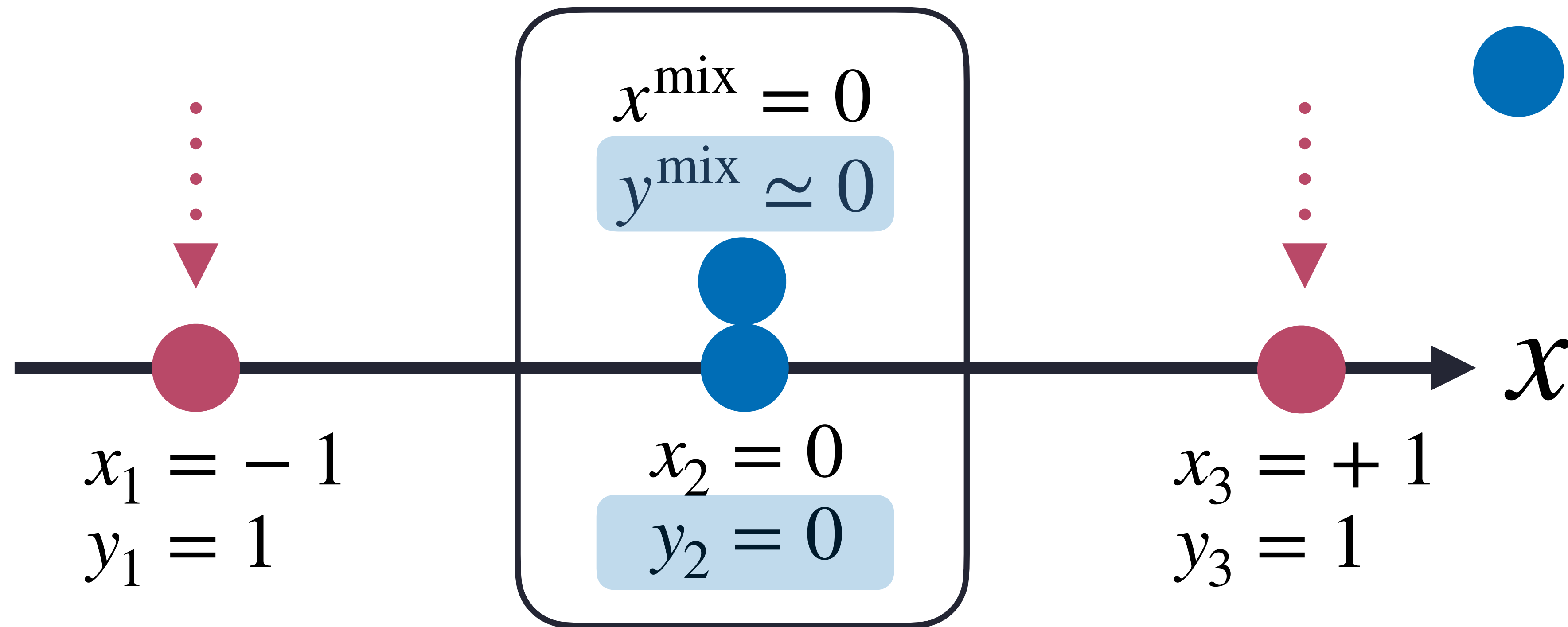
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$$x^{\text{mix}} = 0.5x_1 + 0.5x_3 = 0$$

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Our Solution: Re-Label

● : Class 1
● : Class 0



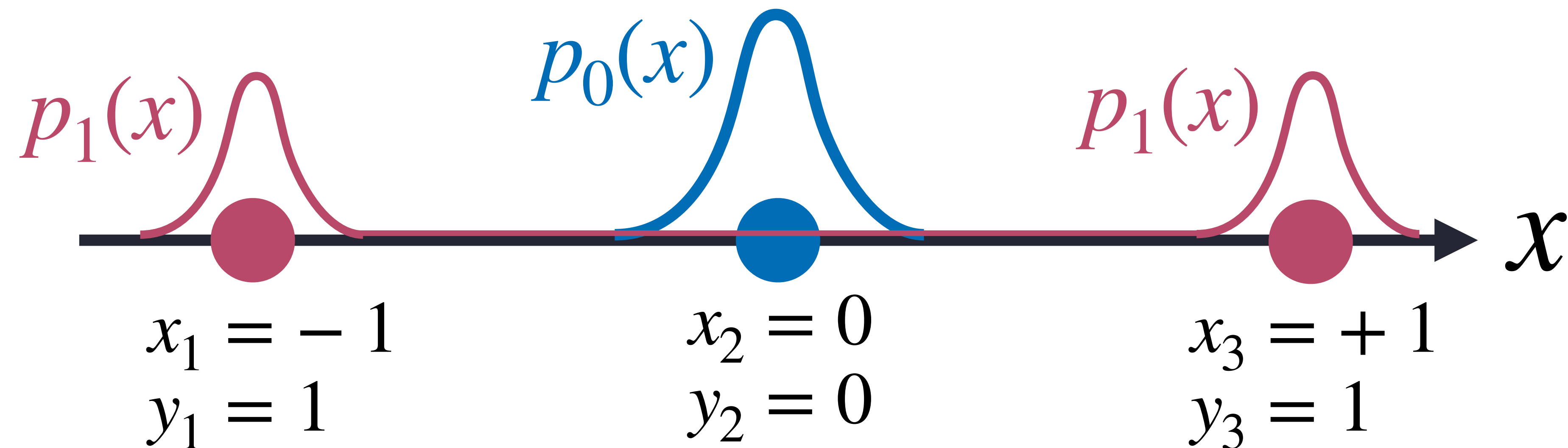
Mixing (x_1, y_1) and (x_3, y_3) generates

$$x^{\text{mix}} = 0.5x_1 + 0.5x_3 = 0$$

$$y^{\text{mix}} = \cancel{0.5y_1 + 0.5y_3} = 1$$

Step 1. Learn Distribution

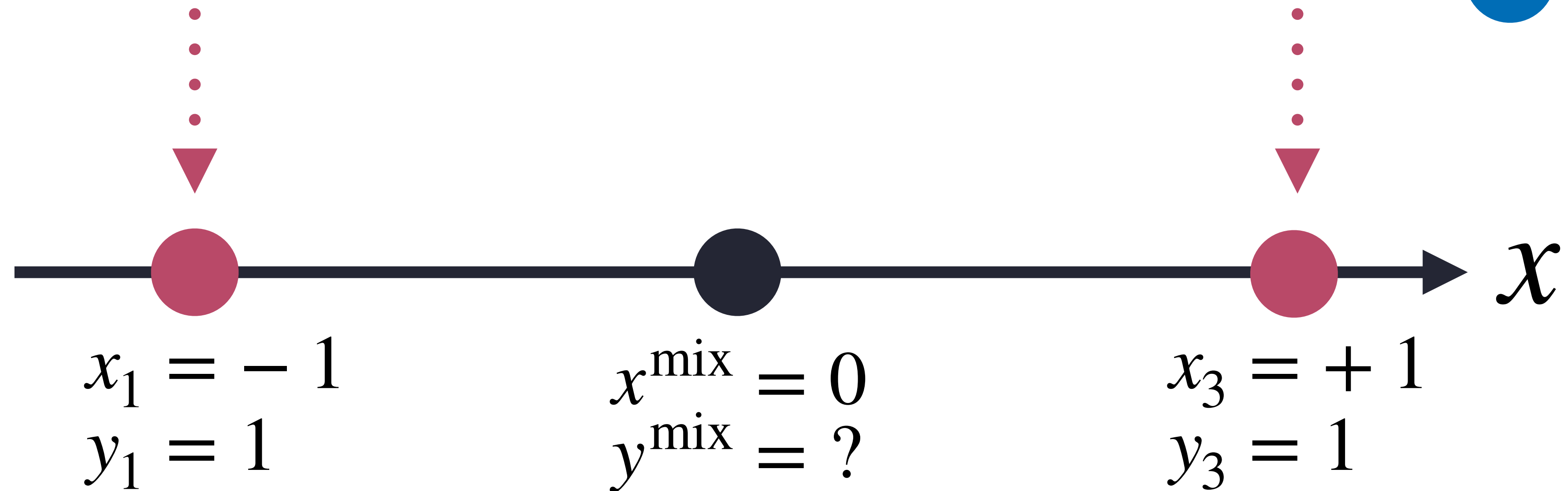
● : Class 1
● : Class 0



Step 2. Generate Mixup Sample

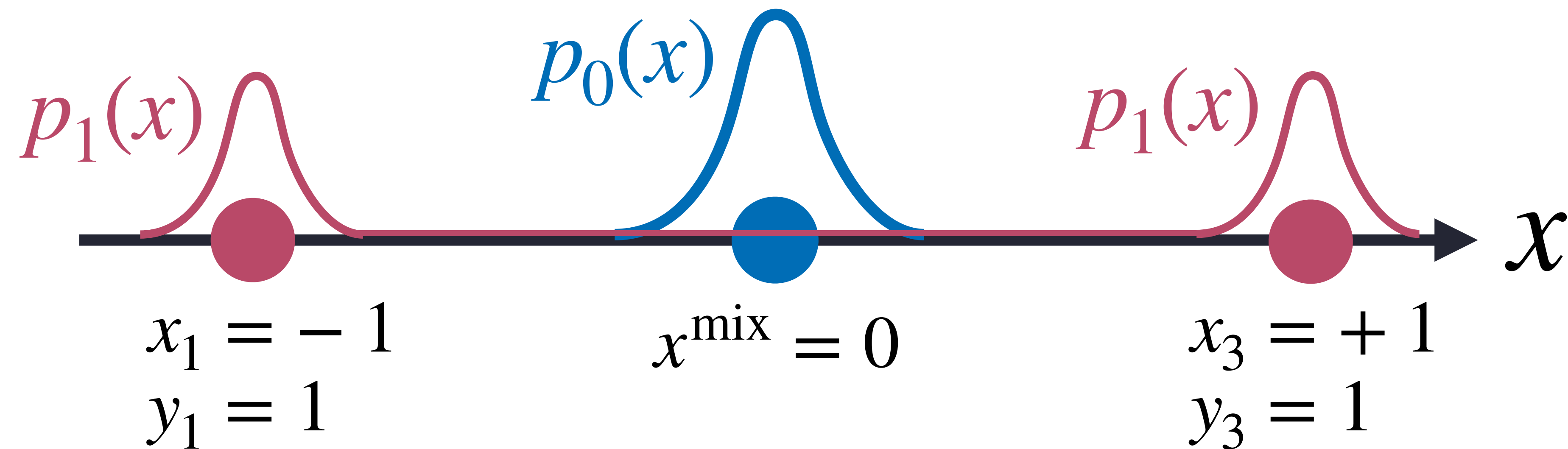
● : Class 1

● : Class 0



Step 3. Label Mixup Sample

● : Class 1
● : Class 0



$$y^{\text{mix}} = \frac{p_1(x^{\text{mix}})}{p_0(x^{\text{mix}}) + p_1(x^{\text{mix}})} \cdot 1 \approx 0$$

$p_0(x^{\text{mix}}) \gg p_1(x^{\text{mix}})$

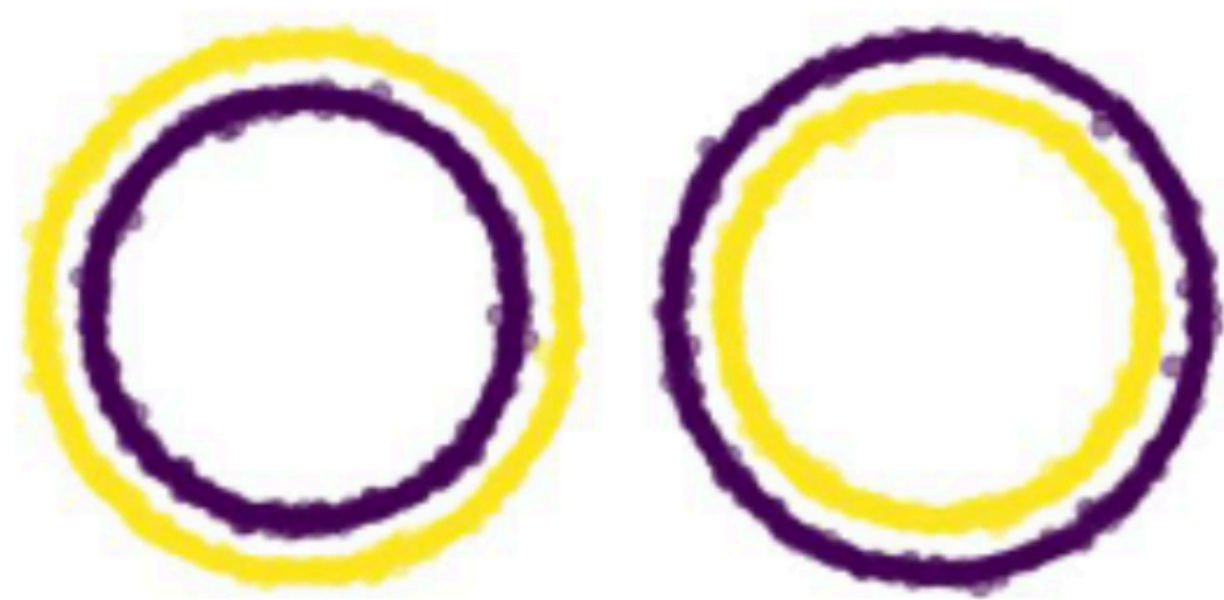
Step 3. Label Mixup Sample

GenLabel
(Generative Model-based Labeling)

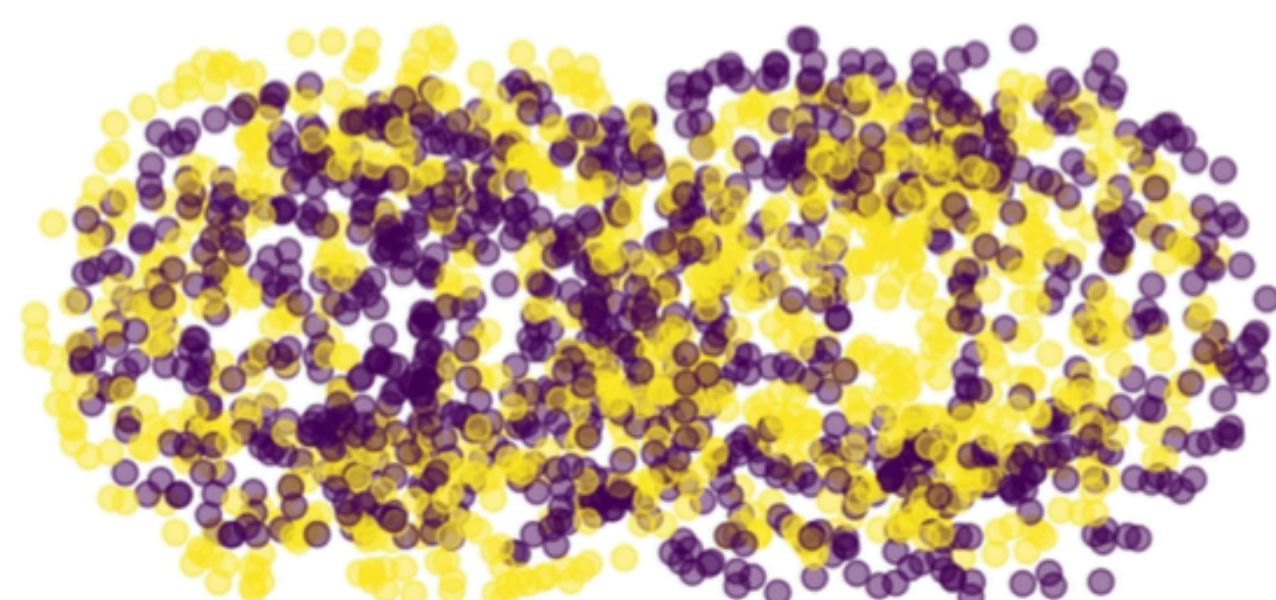
$$y^{\text{mix}} = \frac{p_1(x^{\text{mix}})}{p_0(x^{\text{mix}}) + p_1(x^{\text{mix}})} \cdot 1 \approx 0$$

$p_0(x^{\text{mix}}) \gg p_1(x^{\text{mix}})$

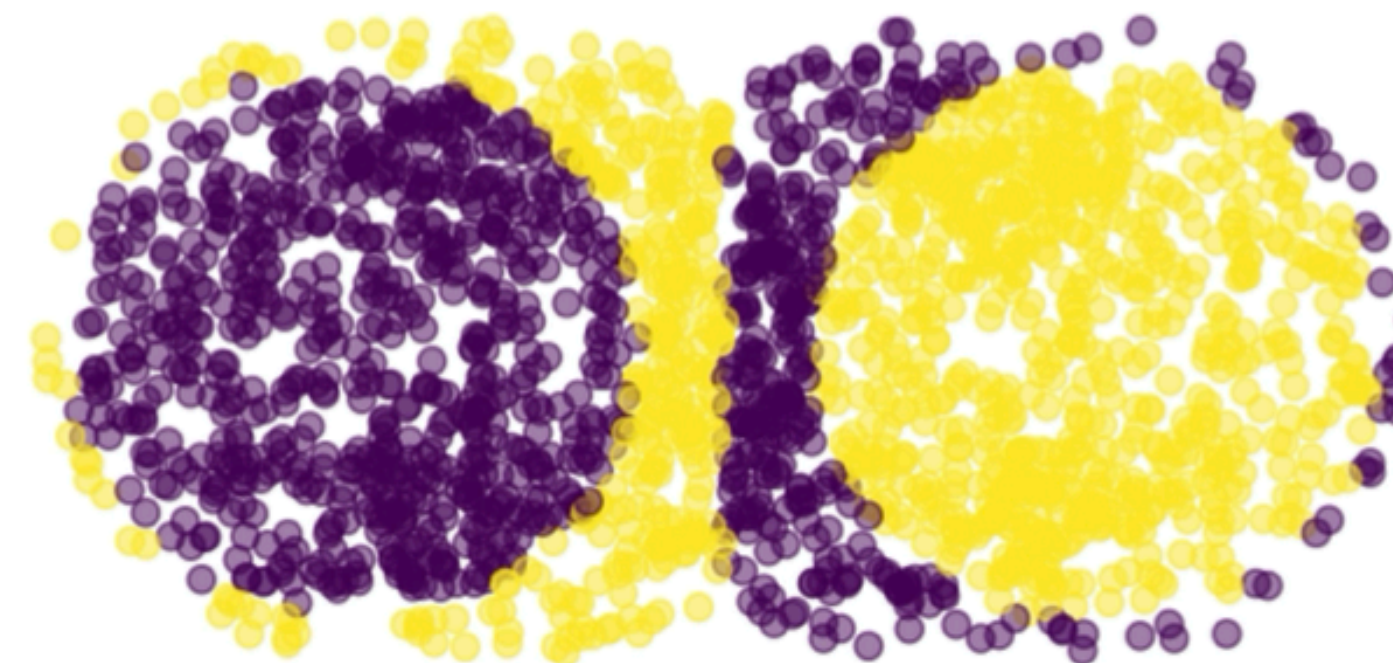
Key Results: Margin



Dataset



Top-1 label of
mixup



Top-1 label of
mixup+GenLabel



Decision boundary of
mixup



Decision boundary of
mixup+GenLabel

Key Results: Accuracy

Methods \ OpenML Dataset ID	721	777	792	830	855	913	1413	1498
Vanilla	79.67	58.67	73.20	77.60	63.33	70.80	95.56	66.91
AdaMixup	80.33	64.00	73.87	78.40	66.67	70.53	92.44	66.76
Mixup	79.33	62.67	73.47	76.27	66.00	69.87	88.00	66.76
Mixup + Excluding MI	79.67	62.67	74.53	78.13	66.40	71.47	93.33	66.33
Mixup + GenLabel (GM)	81.00	58.67	75.47	86.13	66.40	71.47	96.00	67.63
Mixup + GenLabel (KDE)	79.67	58.67	75.87	77.33	67.60	72.67	96.00	66.33
Mixup + GenLabel (CV)	80.33	64.00	75.60	84.53	67.33	73.20	96.44	67.77

GenLabel improves accuracy of **mixup** up to 8 – 10%

Key Results: Robustness

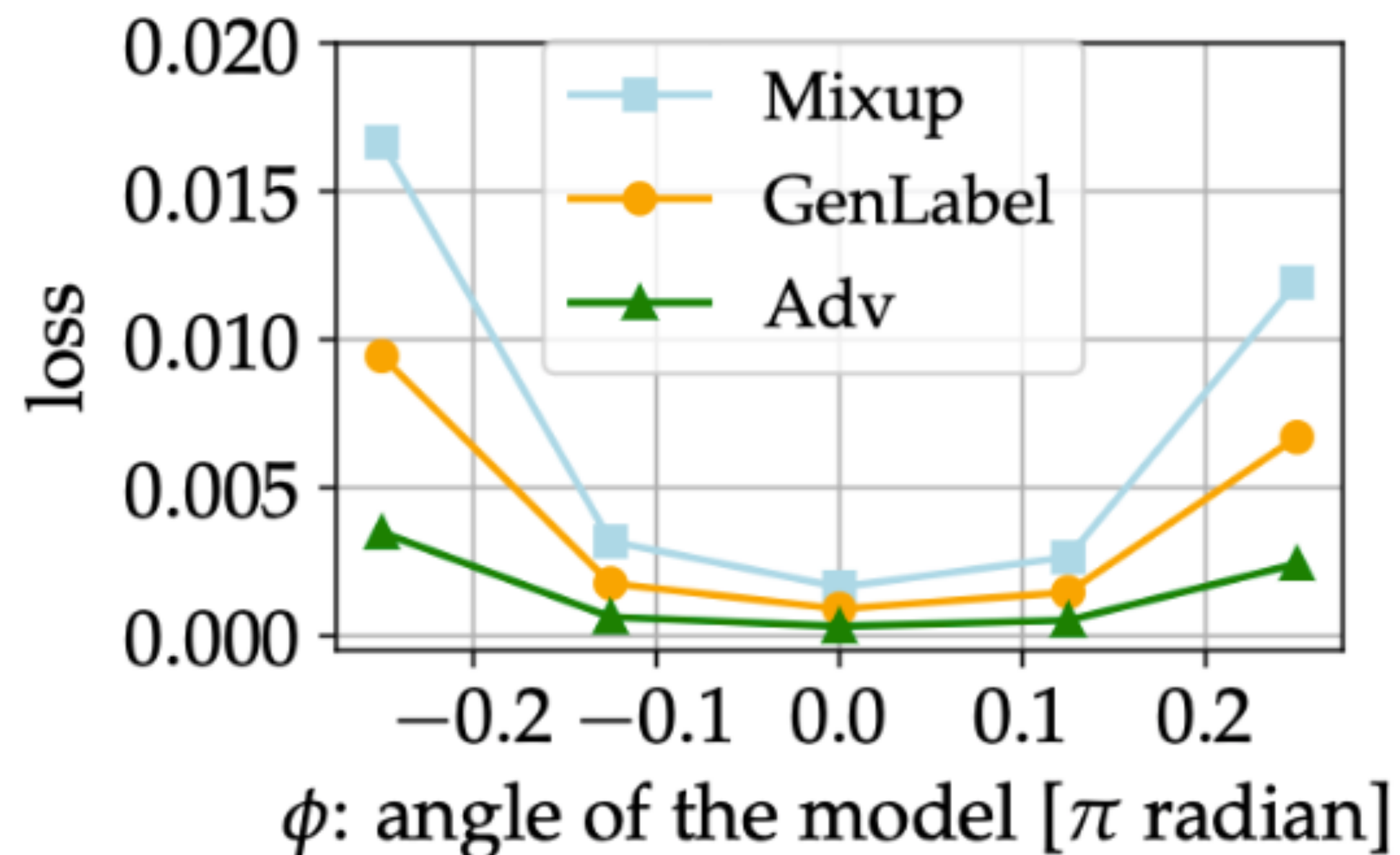
Methods \ OpenML ID	446	468	683	755	763	1413
Vanilla	29.67	34.55	51.11	41.05	64.27	68.00
AdaMixup	30.33	37.27	51.11	37.89	63.20	67.11
Mixup	30.67	37.27	50.00	36.84	65.07	67.56
Mixup + Excluding MI	31.67	31.82	52.22	38.95	63.20	70.67
Mixup + GenLabel (GM)	37.00	42.73	52.22	43.16	61.87	71.11
Mixup + GenLabel (NN)	38.00	32.73	46.67	43.16	66.93	77.33

GenLabel improves robustness of **mixup** up to 7 – 10%

* black-box attack, $\varepsilon = 0.1$

Key Results: Robustness

[Thm] For logistic regression model & FC ReLU networks,
Mixup loss \geq Mixup+**GenLabel** loss \geq Adversarial loss
(Tighter Upper Bound)





Full version available at
<https://arxiv.org/pdf/2201.02354.pdf>



**Hall E, Poster Session 2,
#525**