

# Adversarial Attacks on Gaussian Process Bandits

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# Motivation

GP bandits is the problem of optimizing a black-box function  $f$  by using derivative-free queries guided by a GP surrogate model; where  $f$  is assumed to be in the RKHS:

$$\max_x f(x).$$

Function observations are typically subject to **corruptions** in the real-world, which are not adequately captured by random noise alone:

1. Rare outliers - i.e. equipment failures,
2. Bad actors - i.e. malicious users.

# Related Work

In literature, methods primarily **focused on proposing methods that defend against the proposed uncertainty model** to improve robustness for GP optimization:

- ▶ Presence of outliers,
- ▶ Random perturbations to sampled points,
- ▶ Adversarial perturbations to the final point / samples.

Minimal work studying the problem from an **attacker's perspective**.

## Our Goal

Examine from an attacker's perspective, focusing on adversarial perturbations.

## Setup

At time  $t$ , with random Noise  $z_t \sim \mathcal{N}(0, \sigma^2)$ , adversarial noise  $c_t$  and budget  $C$ :

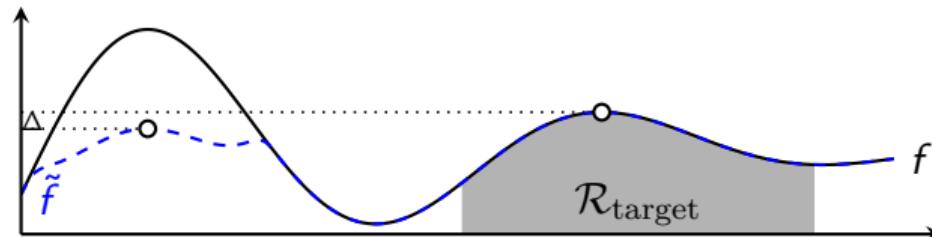
$$y_t = f(\mathbf{x}_t) + c_t + z_t, \quad \text{where } \sum_{t=1}^n |c_t| \leq C.$$

With various levels of knowledge available to the adversary:

1. Targeted Attack - make the player choose actions in a particular region  $\mathcal{R}_{\text{target}}$ .
2. Untargeted Attack - make the player's cumulative regret as high as possible.

# Theoretical Study

Theory applies<sup>1</sup> to **any** algorithm that gets sublinear regret in non-corrupted setting.



## Theorem 1 (Rough Sketch)

Adversary performs an attack shifting the original function  $f$  to  $\tilde{f}$ , with sufficient conditions, resulting in linear regret with high probability.

<sup>1</sup>Also even in certain cases where the attacker doesn't know  $f$ .

# Subtraction Attack (Known $f$ )

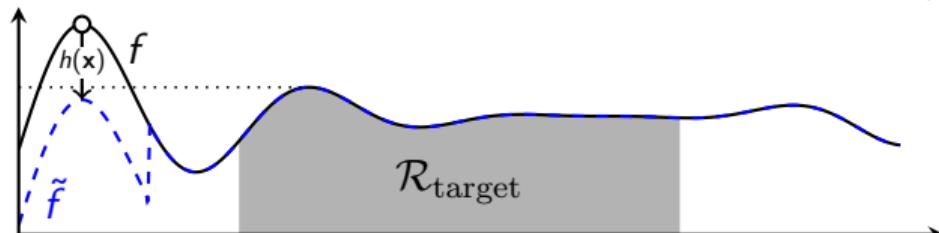
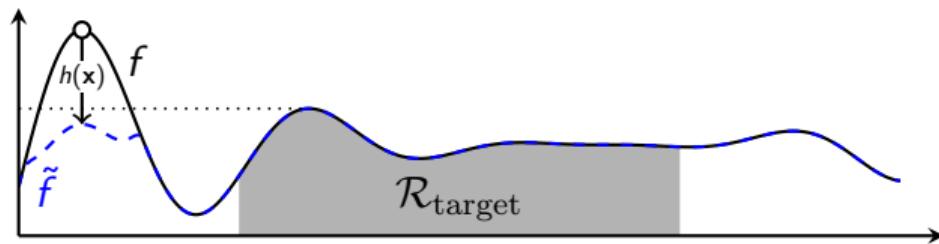
**Idea** is to ‘swallow’ the peaks of the function  $f$ .

Set  $\tilde{f}(x) = f(x) - h(x)$ , where  $h$ :

- ▶ Subtraction Rnd - bump fn.
- ▶ Subtraction Sq - indicator fn.

Discussion:

1. Strong theoretical guarantees<sup>2</sup>.
2. Requiring knowledge of  $f$ .
3. Difficult to construct  $h$ .



Subtraction Rnd (top) and Sq (bottom).

<sup>2</sup>Only for Subtraction Rnd; depending on the properties of  $h$ .

# Clipping Attack (Known $f$ )

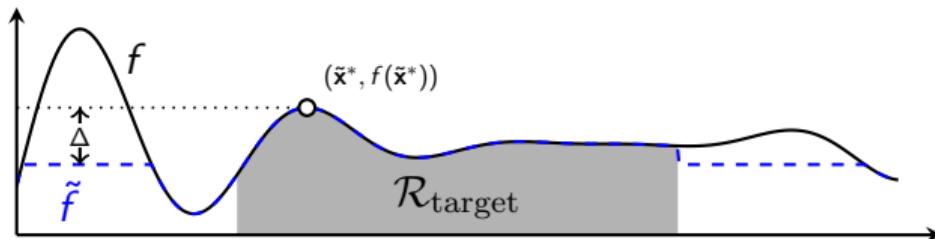
**Idea** is to 'cut' the rest of the function  $f$  off by  $\Delta$  from the peak in  $\mathcal{R}_{\text{target}}$ .

Clipping Attack by setting:

$$\tilde{f}(x) = \begin{cases} f(x) & x \in \mathcal{R}_{\text{target}} \\ \min \{f(x), f(\tilde{x}^*) - \Delta\} & x \notin \mathcal{R}_{\text{target}}, \end{cases}$$

Discussion:

1. Practical, easy to implement.
2.  $\tilde{f}$  not in RKHS.



# Aggressive Subtraction Attack (Unknown $f$ )

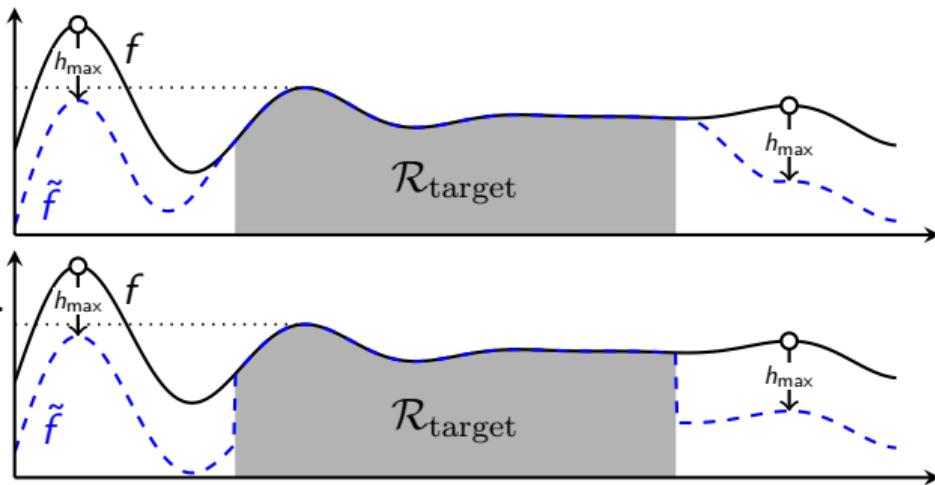
**Idea** is to subtract *all* points outside  $\mathcal{R}_{\text{target}}$  by roughly the same value  $h_{\max}$ .

Simplified Aggressive Subtraction,  
without “transition region”:

$$\tilde{f}(x) = \begin{cases} f(x) & x \in \mathcal{R}_{\text{target}} \\ f(x) - h_{\max} & x \notin \mathcal{R}_{\text{target}} \end{cases}$$

Discussion:

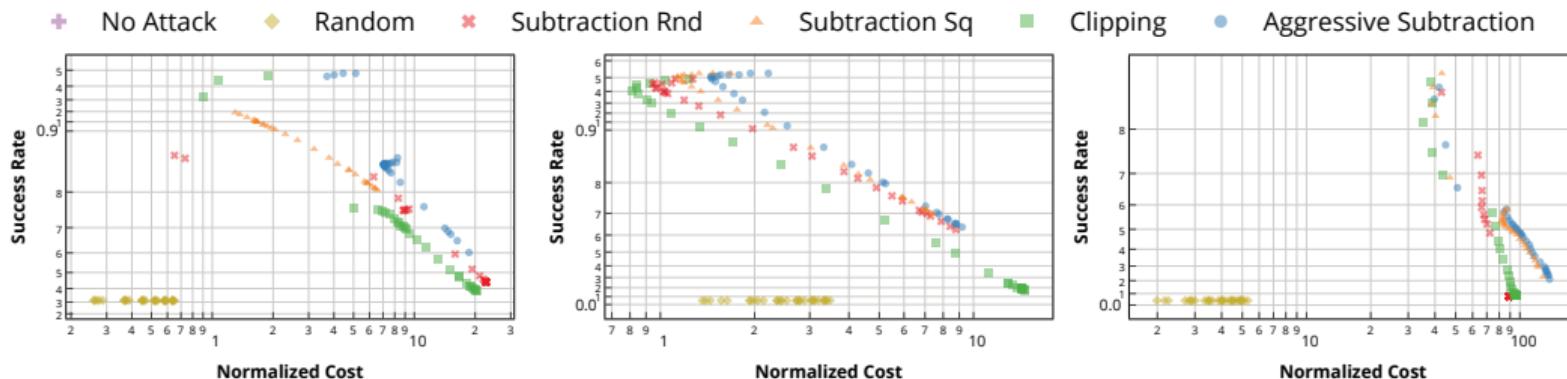
1. Strong theoretical guarantees<sup>3</sup>.



With “transition region” (top) and without (bottom).

<sup>3</sup>Only for Aggressive Subtraction with “transition region”.

## Results for Synthetic1D, Forrester1D, Levy-Hard1D



- ▶ Clipping works consistently.
- ▶ Aggressive Subtraction works, but with higher cost.
- ▶ Subtraction Rnd and Subtraction Sq is 'in between'.
- ▶ Subtraction Rnd tends to narrowly beat Subtraction Sq (due to smooth  $h(x)$ ).

# Key Contributions

1. Study conditions under which an adversarial attack can succeed.
2. Present various attacks:
  - 2.1 Known  $f$ : Subtraction Rnd and Subtraction Sq, Clipping Attack.
  - 2.2 Unknown  $f$ : Aggressive Subtraction.

Demonstrated their effectiveness on a diverse range of objective functions.

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