

Neural-Symbolic Models for Logical Queries on Knowledge Graphs

Zhaocheng Zhu, Mikhail Galkin, Zuobai Zhang, Jian Tang

ICML 2022



Mila

Université
de Montréal 

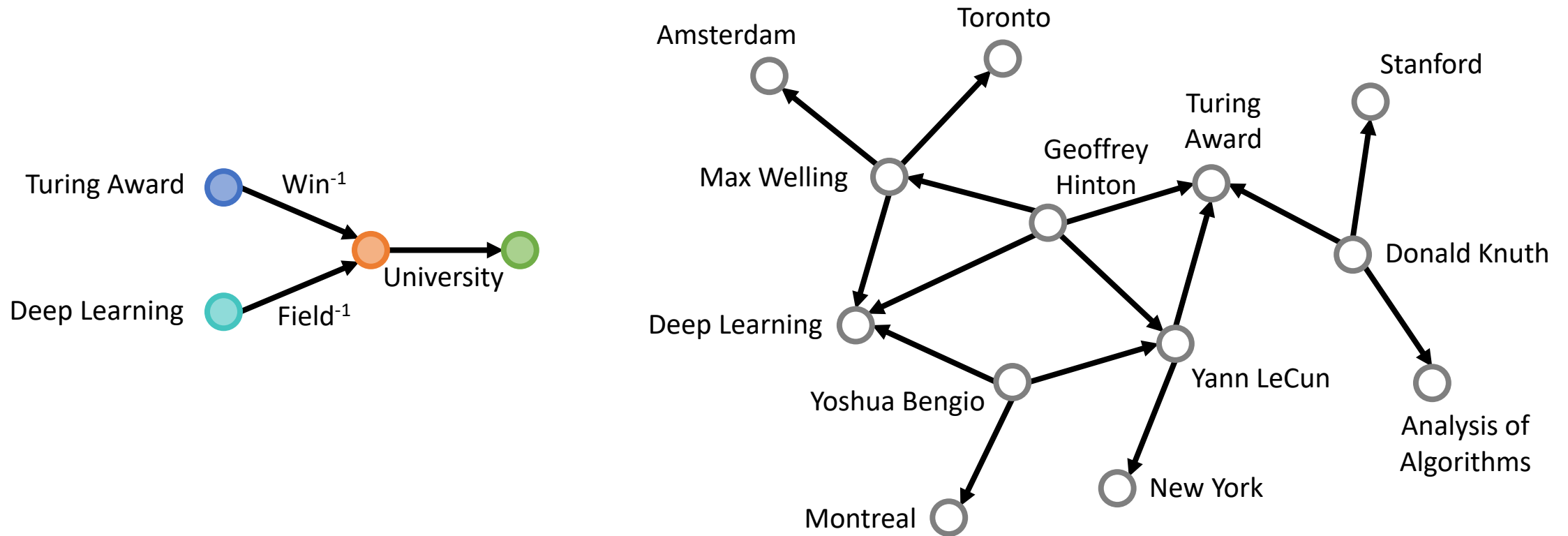


McGill



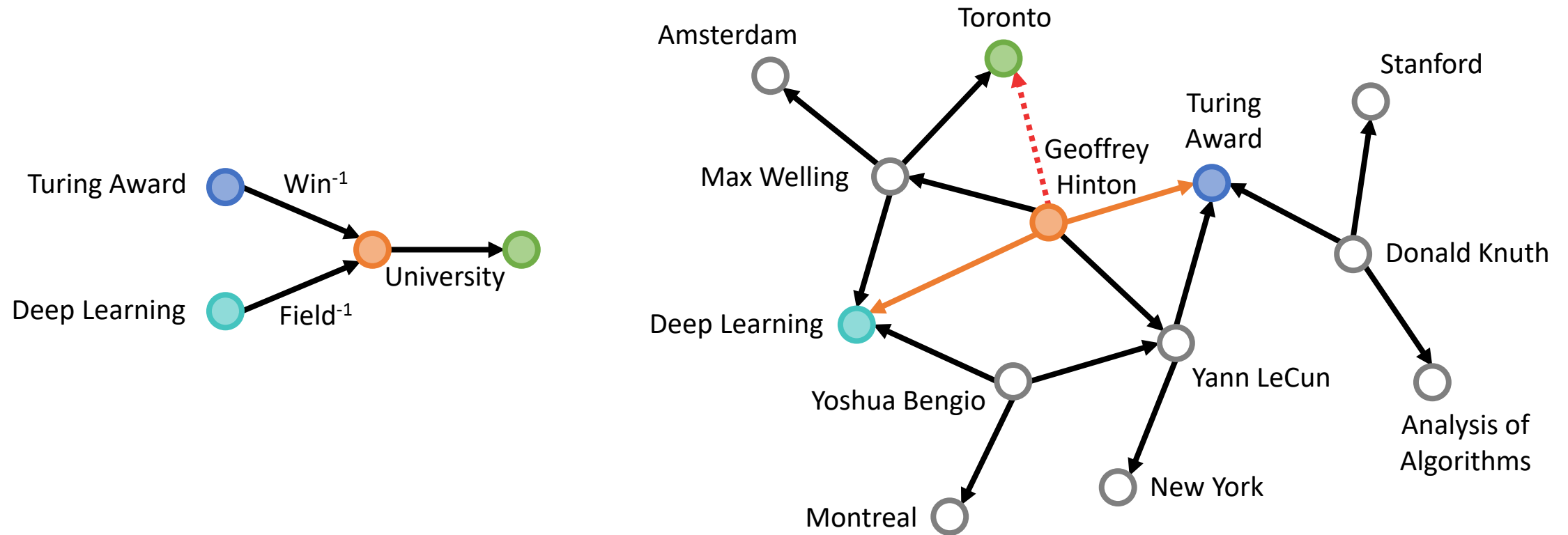
First-Order Logic Queries

Which universities do the Turing Award winners of deep learning work in?

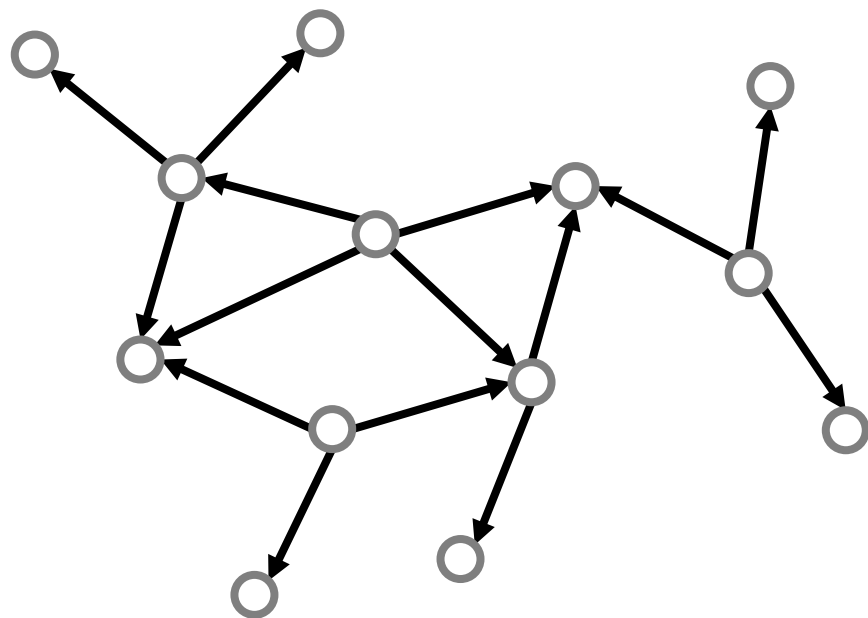


Symbolic Methods

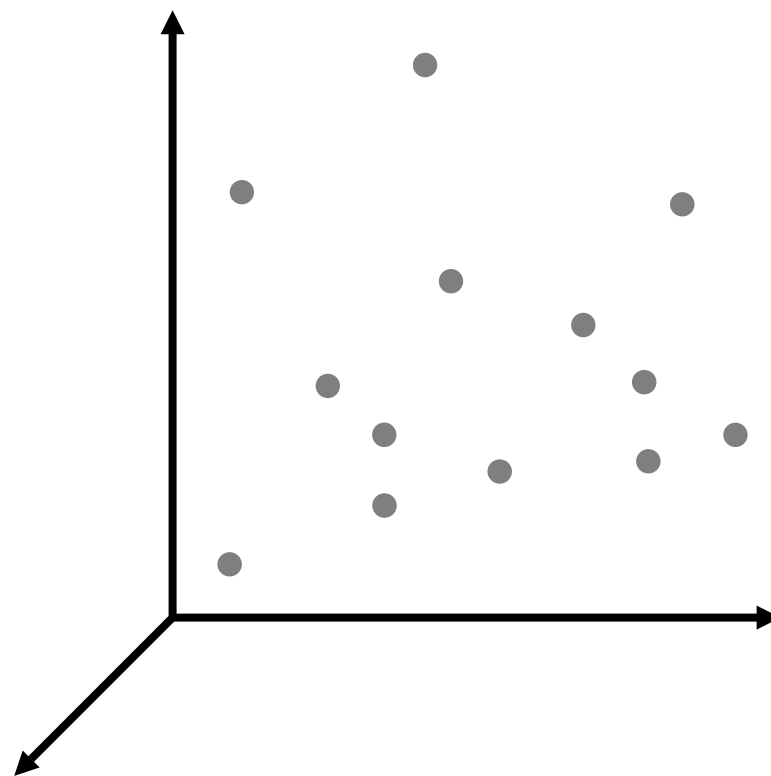
Can't deal with **missing links**



Neural Methods

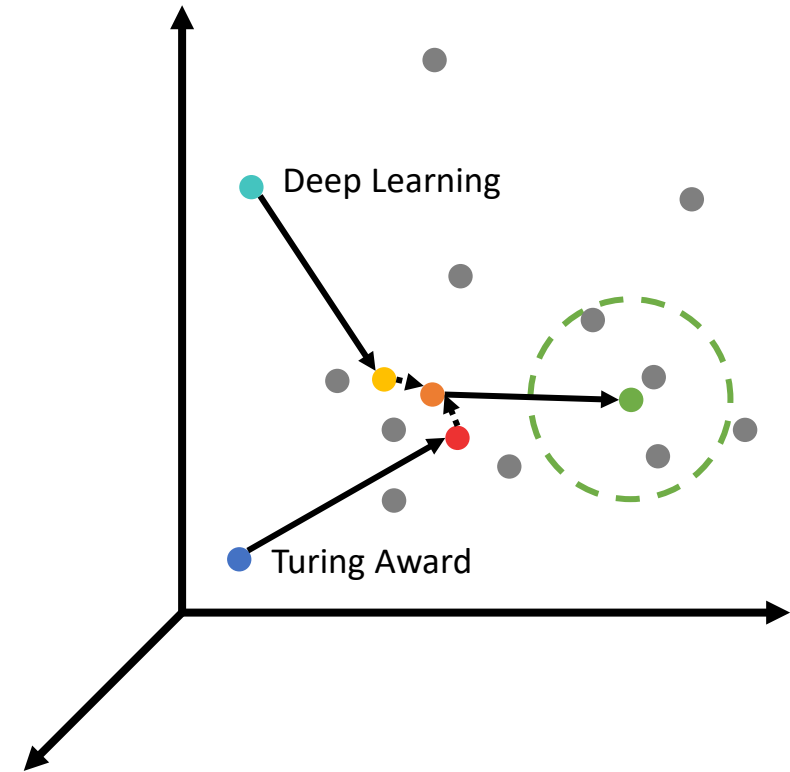
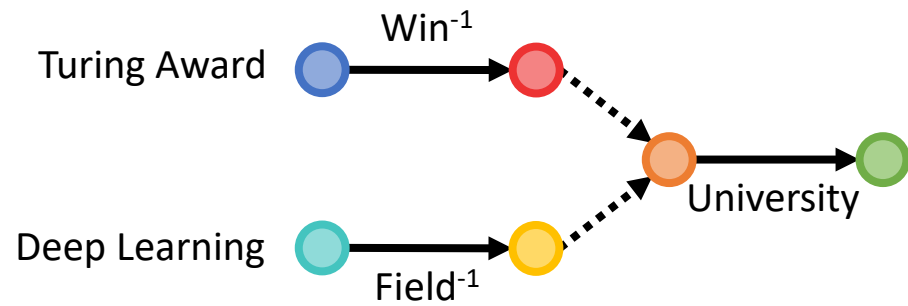


Embed



Neural Methods

Can't interpret intermediate variables



Goal

Can we answer logical queries on **incomplete** knowledge graphs, with **interpretability** for intermediate variables?

Graph Neural Network - Query Executor (GNN-QE)

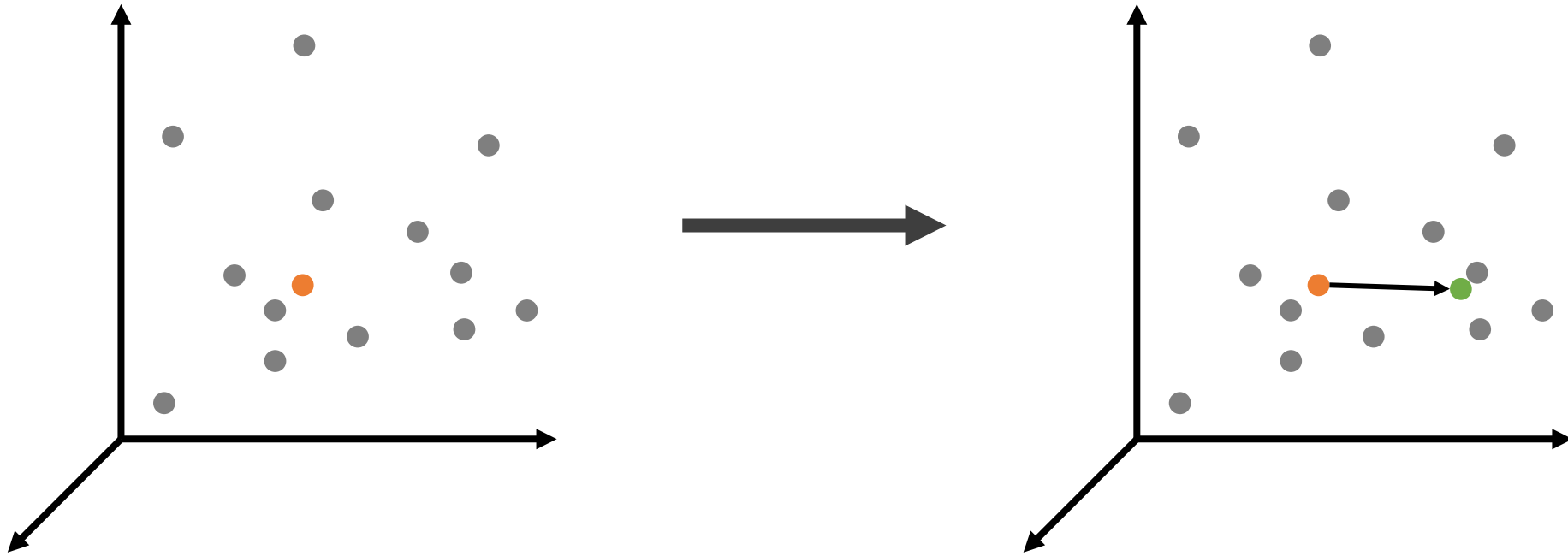
Neural + **Symbolic**

Symbolic: Decompose a logical query as operations over fuzzy sets

Neural: Learn relation projection operation with a graph neural network

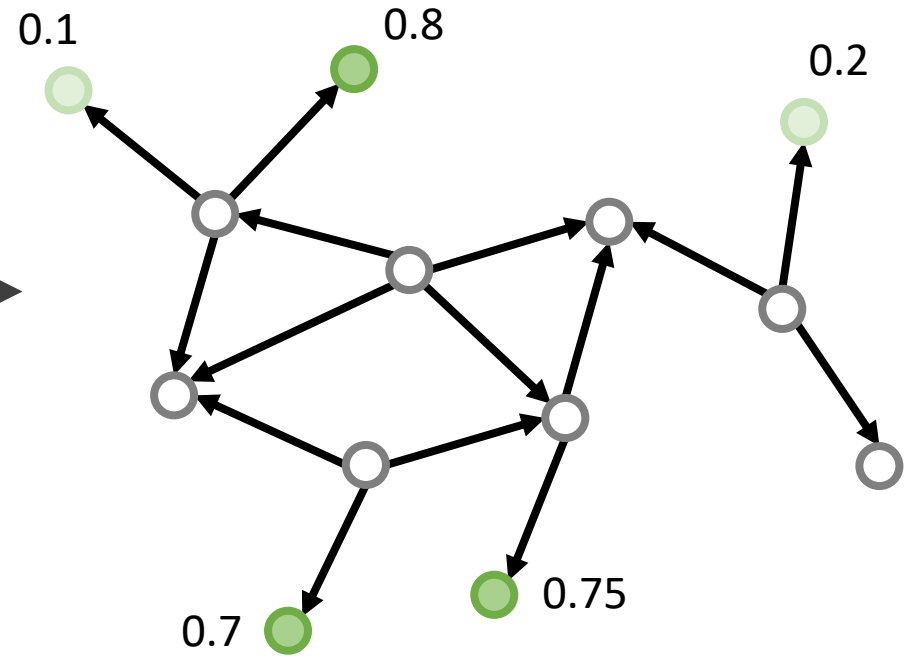
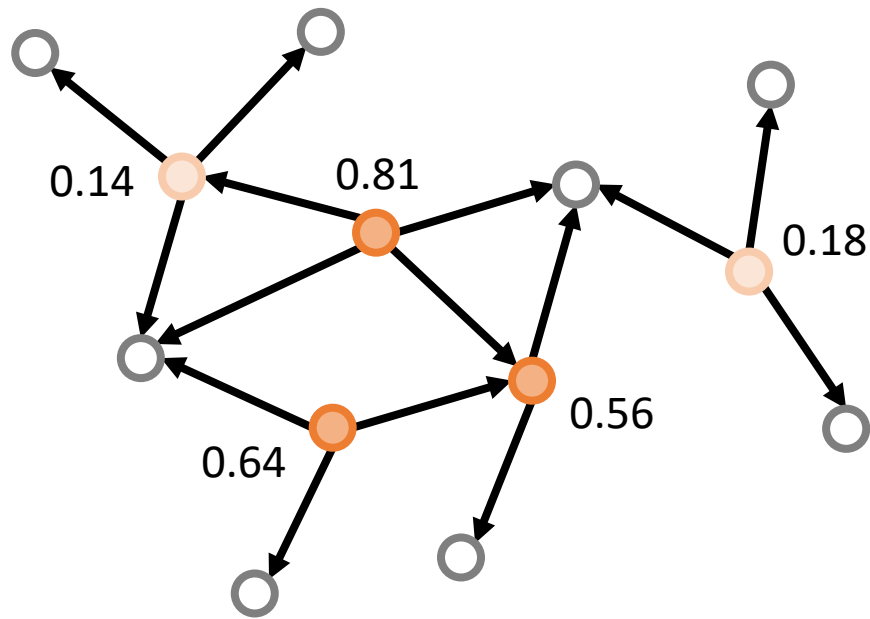
Operations over Embeddings

$$y = \text{University}(x)$$



Operations over Fuzzy Sets

$$y = \text{University}(x)$$



Four Operations

Relation Projection: $University(\mathbf{x})$

Conjunction: $\mathbf{x} \wedge \mathbf{y}$

Disjunction: $\mathbf{x} \vee \mathbf{y}$

Negation: $\neg \mathbf{x}$

Four Operations

Relation Projection: $University(x)$

GNN

Conjunction: $x \wedge y$

Disjunction: $x \vee y$

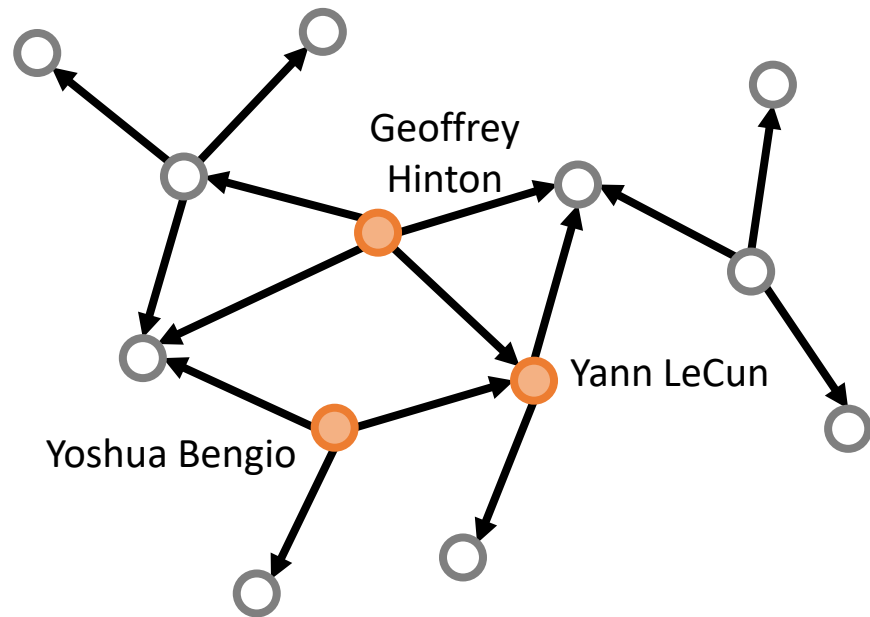
Negation: $\neg x$



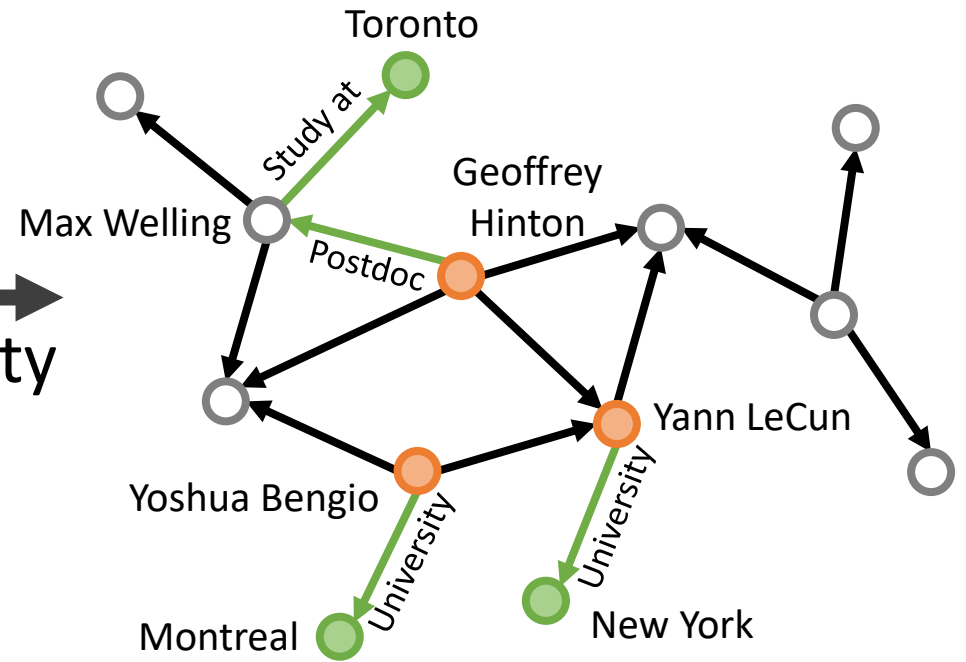
Fuzzy Logic

Relation Projection

Propagate with a GNN

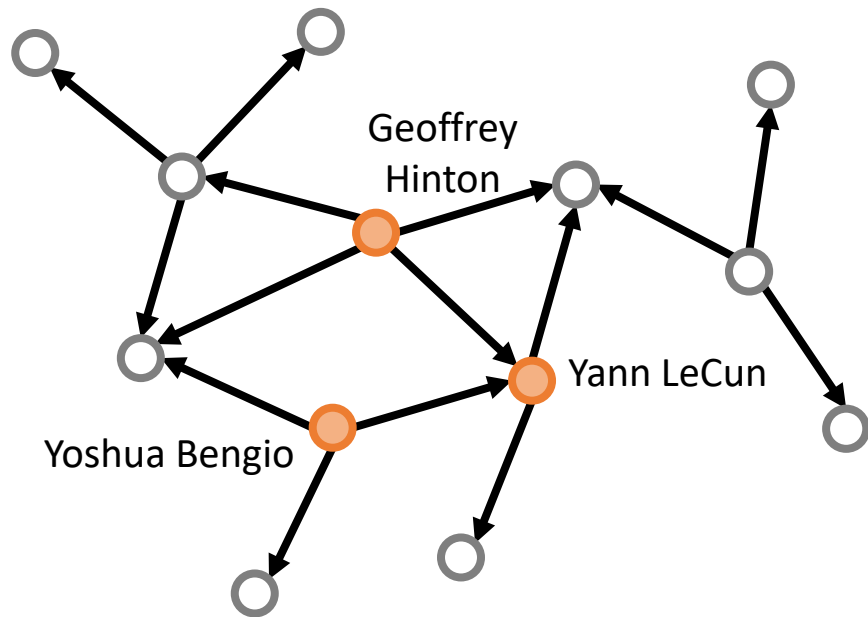


University

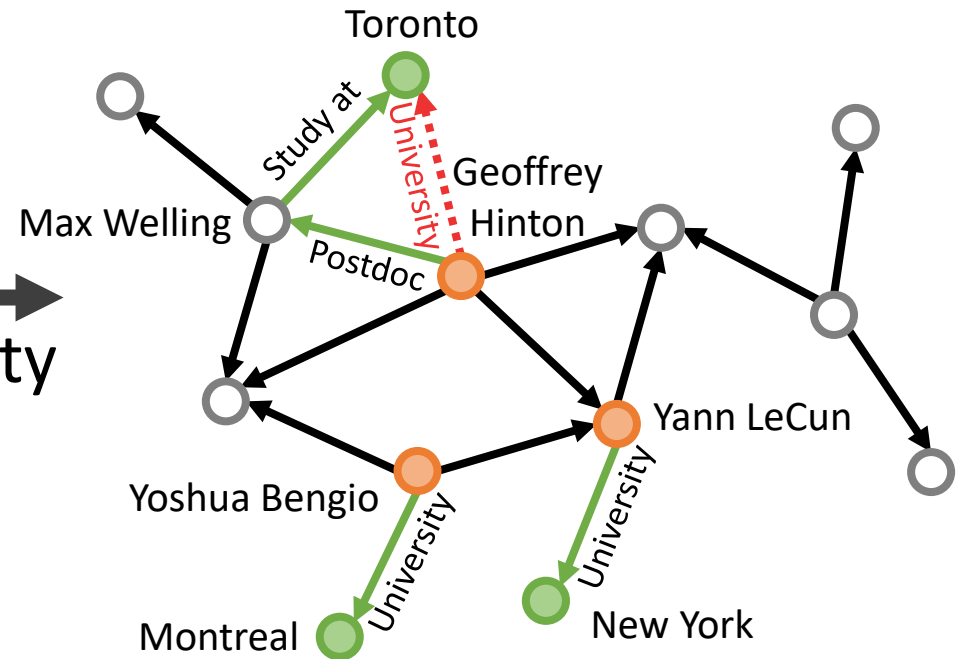


Relation Projection

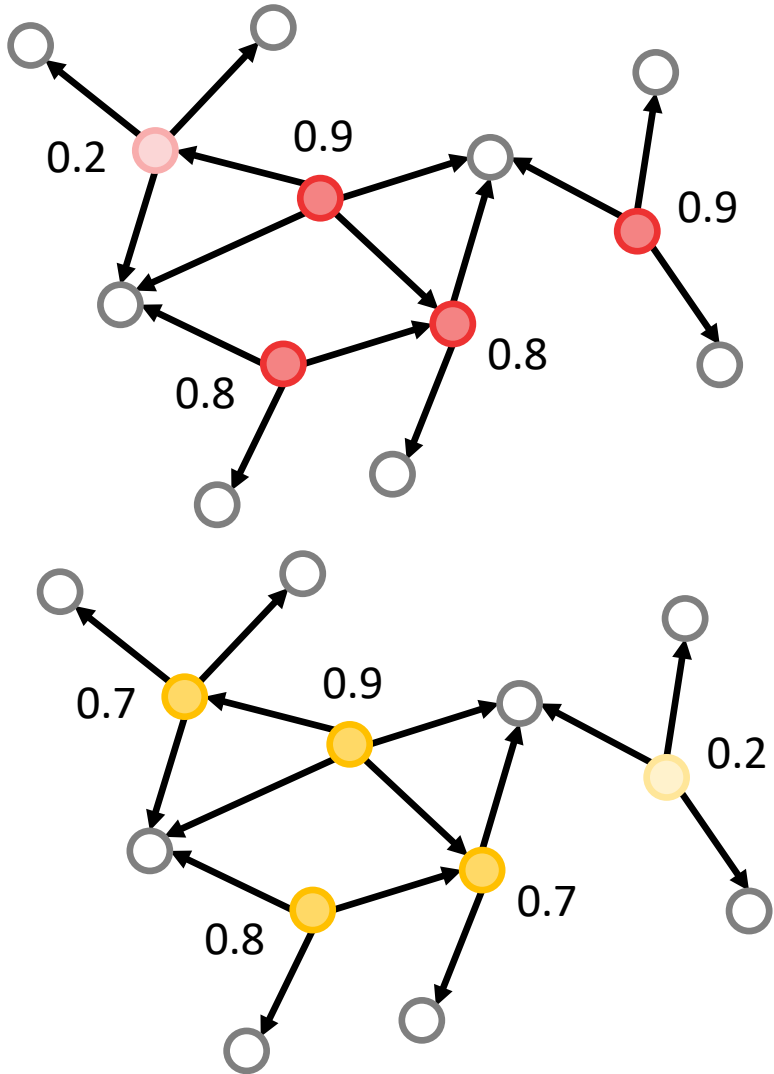
Can deal with **missing links**



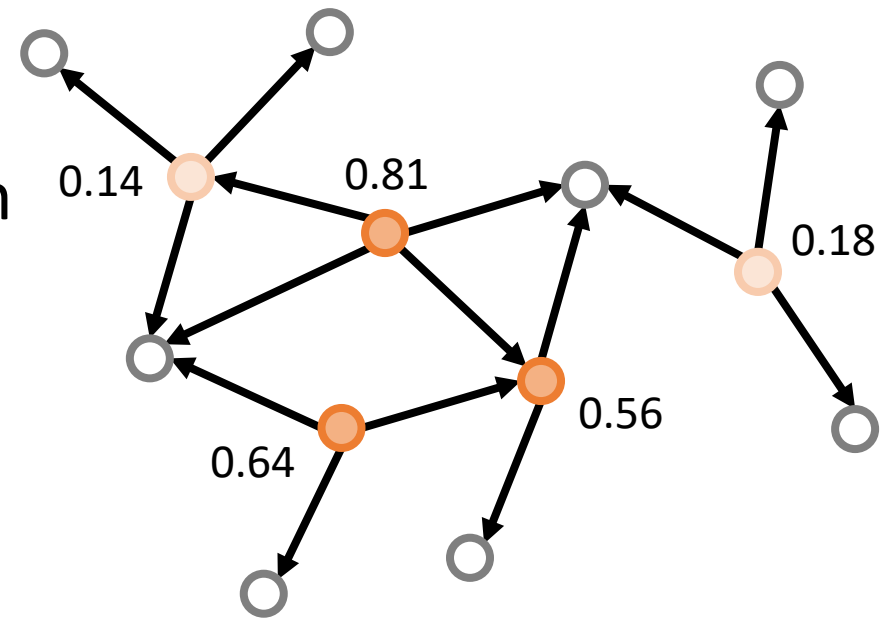
University



Fuzzy Logic Operations



Conjunction
 $x * y$



Summary

22.3% relative improvement on EPFO queries

95.1% relative improvement on negation queries

Interpret intermediate variables

Predict the number of answers without explicit supervision