

# Adversarial Robustness against Multiple and Single $l_p$ -Threat Models via Quick Fine-Tuning of Robust Classifiers

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# Some context

- A classifier  $f : [0, 1]^d \rightarrow \mathbb{R}^K$  is robust wrt a **single**  $l_p$ -norm at radius  $\epsilon$  at a point  $x$  with correct label  $c$  if

$$\arg \max_{r=1,\dots,K} f_r(x + \delta) = c, \quad \text{for every } \delta \text{ s. th. } \|\delta\|_p \leq \epsilon, \ x + \delta \in [0, 1]^d$$

- **Adversarial training** is commonly used to obtain robust models  $\rightarrow$  **more expensive** than standard training
- **Multiple norm robustness** means simultaneous robustness to several threat models, in our case  $l_\infty$ ,  $l_2$  and  $l_1$
- SOTA methods for multiple norm robustness perform adversarial training for every  $l_p \rightarrow$  mostly **more expensive** than adversarial training wrt single norms

# Fine-tuning robust classifiers

**Goal:** obtaining models with multiple norm robustness **efficiently**

**Idea:** **short fine-tuning** of  $l_p$ -robust classifiers for multiple norm robustness

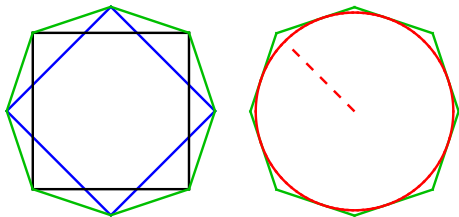
<i>model</i>	<i>clean</i>	$l_\infty (\epsilon_\infty = \frac{8}{255})$	$l_2 (\epsilon_2 = 0.5)$	$l_1 (\epsilon_1 = 12)$	<i>average</i>	<i>union</i>	<i>time/epoch</i>
RN-18 $l_\infty$ -AT	83.7	48.1	59.8	7.7	38.5	7.7	151 s
+ SAT	$83.5 \pm 0.2$	$43.5 \pm 0.2$	$68.0 \pm 0.4$	$47.4 \pm 0.5$	$53.0 \pm 0.2$	$41.0 \pm 0.3$	161 s
+ AVG	$84.2 \pm 0.4$	$43.3 \pm 0.4$	$68.4 \pm 0.6$	$46.9 \pm 0.6$	$52.9 \pm 0.4$	$40.6 \pm 0.4$	479 s
+ MAX	$82.2 \pm 0.3$	$45.2 \pm 0.4$	$67.0 \pm 0.7$	$46.1 \pm 0.4$	$52.8 \pm 0.3$	$42.2 \pm 0.6$	466 s
+ MSD	$82.2 \pm 0.4$	$44.9 \pm 0.3$	$67.1 \pm 0.6$	$47.2 \pm 0.6$	$53.0 \pm 0.4$	$42.6 \pm 0.2$	306 s
+ E-AT	$82.7 \pm 0.4$	$44.3 \pm 0.6$	$68.1 \pm 0.5$	$48.7 \pm 0.5$	$53.7 \pm 0.3$	$42.2 \pm 0.8$	160 s

Fine-tuning  $l_p$ -robust models with any  $p \in \{\infty, 2, 1\}$  for multiple norm robustness for **3 epochs (CIFAR-10) or 1 epoch (ImageNet)** is sufficient to reach competitive robustness in the union of threat models!

# Extreme norm Adversarial Training

**Problem:** MAX (Tramèr & Boneh, 2019) and MSD (Maini et al., 2020) are 2-3x **more expensive** than single norm adversarial training.

**Note:** Croce & Hein (2020) show that, for linear classifiers, robustness wrt  $l_\infty$  and  $l_1$  (extreme norms) is sufficient for robustness wrt  $l_p$  for  $p \in (1, \infty)$ .



We propose **Extreme norm Adversarial Training (E-AT)**, which

- performs adversarial training for a **single** norm,  $l_\infty$  or  $l_1$ , for each batch,
- **adaptively** samples the threat model to use,
- is **as expensive** as single norm adversarial training.

## CIFAR-10

<i>model</i>		<i>clean</i>		$l_\infty (\epsilon_\infty = \frac{8}{255})$	$l_2 (\epsilon_2 = 0.5)$	$l_1 (\epsilon_1 = 12)$	<i>union</i>			
<b>Fine-tuning</b> $l_\infty$ -robust models	RN-50 - $l_\infty$ (Engstrom et al., 2019) + FT	88.7 86.2	 -2.5	50.9 46.0	 -4.9	59.4 70.1	5.0 49.2	5.0 44.2	5.0 43.4	38.4
	WRN-34-20 - $l_\infty$ (Gowal et al., 2020) + FT	87.2 88.3	 1.1	56.6 49.3	 -7.3	63.7 71.8	8.5 51.2	8.5 42.7	8.5 46.2	37.7
	WRN-28-10 - $l_\infty$ (*) (Carmon et al., 2019) + FT	90.3 90.3	 0.0	59.1 52.6	 -6.5	65.7 74.7	8.0 54.0	8.0 46.0	8.0 48.7	40.7
	WRN-28-10 - $l_\infty$ (*) (Gowal et al., 2020) + FT	89.9 91.2	 1.3	62.9 53.9	 -9.0	67.2 76.0	10.8 56.9	10.8 46.1	10.8 50.1	39.3
	WRN-70-16 - $l_\infty$ (*) (Gowal et al., 2020) + FT	90.7 91.6	 0.9	65.6 54.3	 -11.3	66.9 78.2	8.1 58.3	8.1 50.2	8.1 51.2	43.1

## ImageNet

<i>model</i>		<i>clean</i>	$l_\infty$ ( $\epsilon_\infty = \frac{4}{255}$ )	$l_2$ ( $\epsilon_2 = 2$ )	$l_1$ ( $\epsilon_1 = 255$ )	union
<b>Fine-tuning</b> $l_\infty$ -robust models	RN-50 - $l_\infty$	62.9	29.8	17.7	0.0	0.0
	(Engstrom et al., 2019) + FT	58.0 -4.9	27.3 -2.5	41.1 23.4	24.0 24.0	21.7 21.7
	RN-50 - $l_\infty$	68.2	36.7	15.6	0.0	0.0
	(Bai et al., 2021) + FT	60.1 -8.1	29.2 -7.5	42.1 26.5	24.5 24.5	22.6 22.6
	DeiT-S - $l_\infty$	66.4	35.6	40.1	3.1	3.1
	(Bai et al., 2021) + FT	62.6 -3.8	32.2 -3.4	46.1 6.0	24.8 21.7	23.6 20.5
	XCiT-S - $l_\infty$	72.8	41.7	45.3	2.7	2.7
	(Debenedetti, 2022) + FT	68.0 -4.8	36.4 -5.3	51.3 6.0	28.4 25.7	26.7 24.0

Quick fine-tuning with E-AT is effective on different architectures, datasets, with or without extra data.

## CIFAR-10

	<i>model</i>	<i>clean</i>	$l_\infty (\epsilon_\infty = \frac{8}{255})$	$l_2 (\epsilon_2 = 0.5)$	$l_1 (\epsilon_1 = 12)$	<i>union</i>
<b>Fine-tuning</b> $l_\infty$ -robust models	RN-50 - $l_\infty$ (Engstrom et al., 2019) + FT	88.7 86.2	-2.5 -4.9	50.9 46.0	59.4 70.1 10.7	5.0 49.2 44.2 5.0 43.4 38.4
	WRN-34-20 - $l_\infty$ (Gowal et al., 2020) + FT	87.2 88.3	1.1 -7.3	56.6 49.3	63.7 71.8 8.1	8.5 51.2 42.7 8.5 46.2 37.7
	WRN-28-10 - $l_\infty$ (*) (Carmon et al., 2019) + FT	90.3 90.3	0.0 -6.5	59.1 52.6	65.7 74.7 9.0	8.0 54.0 46.0 8.0 48.7 40.7
	WRN-28-10 - $l_\infty$ (*) (Gowal et al., 2020) + FT	89.9 91.2	1.3 -9.0	62.9 53.9	67.2 76.0 8.8	10.8 56.9 46.1 10.8 50.1 39.3
	WRN-70-16 - $l_\infty$ (*) (Gowal et al., 2020) + FT	90.7 91.6	0.9 -11.3	65.6 54.3	66.9 78.2 11.3	8.1 58.3 50.2 8.1 51.2 43.1

## ImageNet

	<i>model</i>	<i>clean</i>	$l_\infty (\epsilon_\infty = \frac{4}{255})$	$l_2 (\epsilon_2 = 2)$	$l_1 (\epsilon_1 = 255)$	<i>union</i>
<b>Fine-tuning</b> $l_\infty$ -robust models	RN-50 - $l_\infty$ (Engstrom et al., 2019) + FT	62.9 58.0	-4.9 -2.5	29.8 27.3	17.7 41.1 23.4	0.0 24.0 24.0 0.0 21.7 21.7
	RN-50 - $l_\infty$ (Bai et al., 2021) + FT	68.2 60.1	-8.1 -7.5	36.7 29.2	15.6 42.1 26.5	0.0 24.5 24.5 0.0 22.6 22.6
	DeiT-S - $l_\infty$ (Bai et al., 2021) + FT	66.4 62.6	-3.8 -3.4	35.6 32.2	40.1 46.1 6.0	3.1 24.8 21.7 3.1 23.6 20.5
	XCiT-S - $l_\infty$ (Debenedetti, 2022) + FT	72.8 68.0	-4.8 -5.3	41.7 36.4	45.3 51.3 6.0	2.7 28.4 25.7 2.7 26.7 24.0

Quick fine-tuning with E-AT allows to obtain SOTA multiple norm robustness with large architectures or datasets with low computational cost!

# Why multiple norm robustness?

We test the robustness of various classifiers on CIFAR-10 to **unseen non  $l_p$ -bounded** attacks (sparse attacks, adversarial corruptions).

<i>model</i>	<i>clean</i>	<i>comm. corr.</i>	$l_0$	<i>patches</i>	<i>frames</i>	<i>fog</i>	<i>snow</i>	<i>gabor</i>	<i>elastic</i>	<i>jpeg</i>	<i>avg.</i>	<i>union</i>
NAT	94.4	71.6	0.1	8.1	2.6	47.3	3.9	35.0	0.2	0.0	12.2	0.0
$l_\infty$ -AT	81.9	72.6	7.3	21.6	26.2	36.0	35.9	52.5	59.4	5.1	30.5	2.0
$l_2$ -AT	87.8	79.2	13.2	25.0	17.7	44.9	22.1	43.5	56.6	14.0	29.6	4.5
$l_1$ -AT	83.5	75.0	40.9	41.3	21.1	35.6	20.6	41.2	53.3	25.5	34.9	8.6
PAT	82.6	76.9	23.3	37.9	21.7	53.5	25.6	41.8	53.5	13.7	33.9	8.0
SAT	80.5	72.0	38.7	36.7	29.3	33.5	29.0	49.8	57.0	37.4	38.9	13.8
AVG	82.0	73.6	39.7	36.8	30.8	37.2	21.1	49.9	58.1	30.4	38.0	10.9
MAX	80.1	71.3	35.1	34.6	32.7	34.5	35.0	53.4	58.5	33.5	39.7	15.3
MSD	81.0	71.7	36.9	35.0	31.8	34.6	26.4	51.5	59.7	33.4	38.7	12.9
E-AT	79.1	71.3	39.5	37.7	30.5	34.8	33.4	50.2	58.6	38.7	40.4	15.9

Models trained wrt multiple norms show the highest robustness to unseen attacks.

# Fine-tuning to another $l_q$ -threat model

We try to fine-tune a classifier robust wrt  $l_p$  with adversarial training wrt  $l_q$  for  $q \neq p$  (3 epochs for CIFAR-10, 1 epoch for ImageNet).

CIFAR-10				
	$clean$	$l_\infty$	$l_2$	$l_1$
WRN-70-16 (Gowal et al., 2020) - $l_\infty$ (*)				
original	90.7	65.6	66.9	8.1
+ FT wrt $l_2$	92.8	47.4	80.0	34.0
+ FT wrt $l_1$	92.4	33.9	74.7	<b>70.2</b>
WRN-70-16 (Gowal et al., 2020) - $l_2$ (*)				
original	94.1	43.1	81.7	34.6
+ FT wrt $l_\infty$	92.3	58.5	73.5	11.4
+ FT wrt $l_1$	92.8	29.2	75.7	68.9
RN-18 (Croce & Hein, 2021) - $l_1$				
original	87.1	22.0	64.8	60.3
+ FT wrt $l_\infty$	82.7	44.2	66.6	25.4
+ FT wrt $l_2$	88.0	31.0	69.8	39.7

ImageNet				
	$clean$	$l_\infty$	$l_2$	$l_1$
DeiT-S (Bai et al., 2021) - $l_\infty$				
original	66.4	35.6	40.1	3.1
+ FT wrt $l_2$	66.5	31.2	46.1	9.6
+ FT wrt $l_1$	61.0	23.9	42.9	30.1
XCiT-S (Debenedetti, 2022) - $l_\infty$				
original	72.8	41.7	45.3	2.7
+ FT wrt $l_2$	71.5	35.9	51.4	9.5
+ FT wrt $l_1$	65.8	25.2	47.1	<b>33.9</b>
RN-50 (Engstrom et al., 2019) - $l_2$				
original	58.7	25.0	40.5	14.0
+ FT wrt $l_\infty$	59.1	31.5	40.1	7.5
+ FT wrt $l_1$	56.8	18.0	37.1	28.7

Fine-tuning robust classifiers allows to quickly obtain competitive baselines in other threat models!