

# Massively Parallel k-Means Clustering for Perturbation Resilient Instances

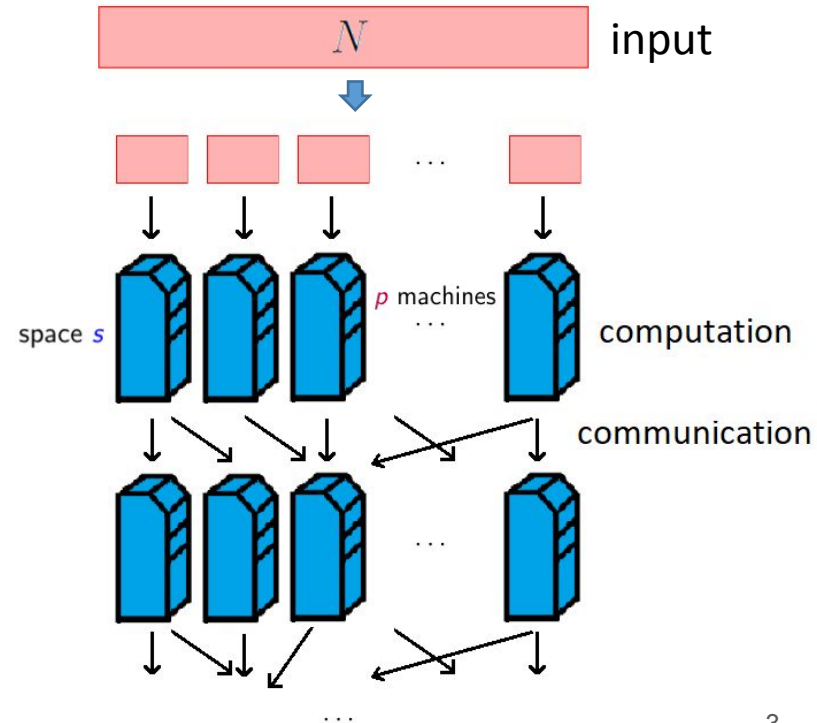
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# Euclidean k-Means Clustering

- Unsupervised learning
  - Partition points into  $k$  groups
  - Similar points are in the same group
  
- Euclidean k-means clustering
  - Input:  $n$  points  $p_1, p_2, \dots, p_n \in \mathbf{R}^d$
  - Goal: find centers  $c_1, c_2, \dots, c_k \in \mathbf{R}^d$  s.t. the clustering cost  $\sum_{i \in [n]} \min_{j \in [k]} \|p_i - c_j\|_2^2$  is minimized
  
- Scalable parallel/distributed algorithms are desired to handle massive data

# Massively Parallel Computation (MPC)

- MPC model
  - An abstraction of MapReduce
  - Sublinear local memory
  - Computation proceeds in rounds
  - Bounded communication
- Efficiency Measure
  - Number of rounds (parallel time)
  - Total space
  - Local memory

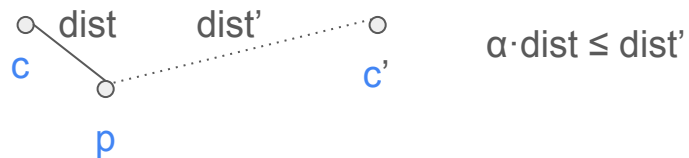


# MPC k-Means Clustering

- **Input:**  $n$ -point set  $P$  in  $\mathbb{R}^d$  distributed on several machines
- **Output:**  $k$  center points distributed on several machines
  
- Previous results
  - **Small** # of rounds & local space but **large**  $\Omega(\log n)$  approximation
  - **Small** approximation factor & # of rounds but **large**  $\Omega(k)$  local space
  - **Small** approximation factor & local space but **large**  $\Omega(\log n)$  number of rounds
  - $O(1)$  approximation,  $o(\log n)$  rounds,  $o(k)$  local space is impossible under certain conditions
  
- Our result
  - Consider natural well-structured point set
  - $O(1)$  rounds,  $n^\delta$  local space for any constant  $\delta > 0$ ,  $1+\epsilon$  approximation, near **linear** total space
  - If local space is  $\Omega(k)$ , the **exact** optimal  $k$ -means solution is obtained

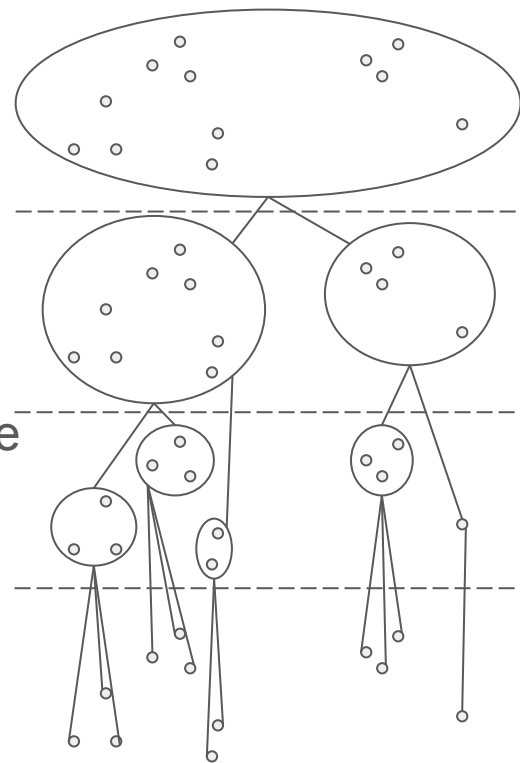
# Perturbation Resilient Instances

- $\alpha$ -Perturbation resilience  $\rightarrow$   $\alpha$ -center proximity
  - Let  $C$  be the optimal solution
  - If  $p$  is in a cluster with center  $c \in C$ , then  $\alpha \cdot \|p - c\|_2 \leq \|p - c'\|_2$  for any other center  $c' \in C$



# Our Techniques

- Candidate clusters via locality sensitive hashing (LSH)
  - LSH → near neighbor graph for different scales
  - Optimal cluster → connected component
  - Candidate clusters → Hierarchical tree structure
- $O(1)$ -round dynamic programming over small depth tree
  - A novel task scheduling process via subtree generation



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