

# Partial Label Learning via Label Influence Function

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# Problem Setting

## Partial Label Learning (PLL)

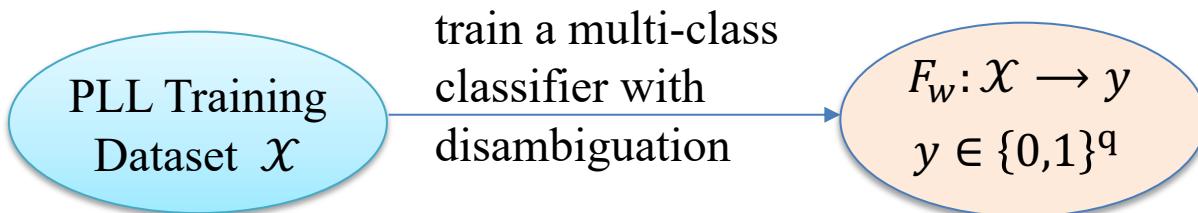
- Each instance is associated with a set of candidate labels, but only one is the ground-truth label, while others are false-positive labels.

## Applications

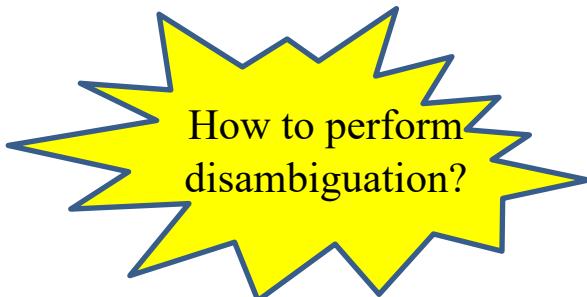
- Document annotation;
- Image annotation;
- Video annotation.

# The Aim and Main Challenge for PLL

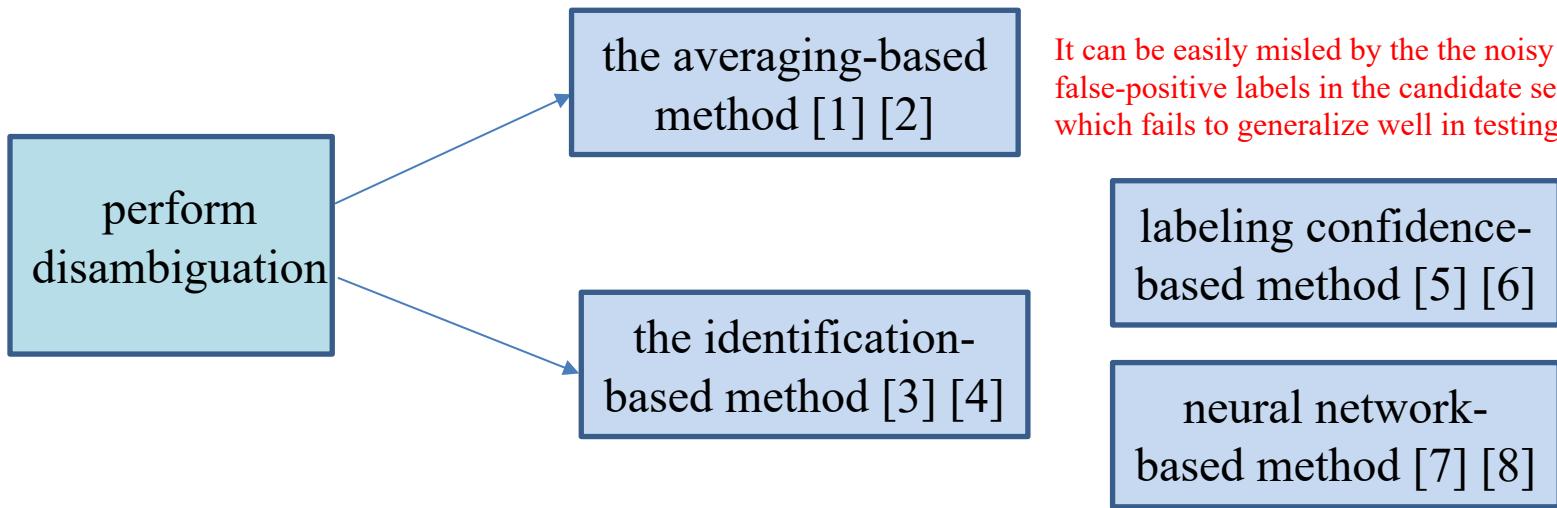
The Aim



The Main Challenge



# Motivation



The identification-based method usually update the model parameter and latent label/confidence variable via an iterative procedure. As the ground-truth variable is discrete, the optimization is often NP-hard. Existing approaches usually take the label that incurs a minimal loss as the ground-truth label or use the weight to represent which label has a high likelihood to be the ground-truth label.

Little work has been done to investigate from how a candidate label changing a predictive model. Motivated by influence function (IF) that characterizes how a model's predictive loss changes when a small fraction of data points being perturbed, this paper first attempts to apply IF to deal with PLL.

# Partial Label Learning via Label Influence Function

## Our Contributions

We provide a new insight into partial label learning (PLL) from the perspective of influence function, and develop a novel framework called Partial Label Learning via Label Influence Function (PLL-IF),

We first define a quantity called Label Impact to quantify how a candidate label changes a predictive model, which can be further employed as an indicator to identify the most influential candidate label with highest impact on a model optimizer.

We then introduce Label Influence Function (LIF) to efficiently approximate the label impact, which avoids retraining the model after each label is removed or perturbed, and largely reduces the heavy computation of the label impact. We further propose a novel ground-truth label identification method called Ground-truth Label Identification via Label Influence Function (GLI-LIF)

Lastly, we implement the PLL-IF framework through a representative non-neural network model (i.e., SVM model) and a basic neural network model respectively. Extensive experiments are conducted on synthetic and real-world datasets to demonstrate the superiorities of the proposed PLL-IF framework.

# Partial Label Learning via Label Influence Function

- In order to identify the ground-truth labels from the candidate label set, we propose a novel ground-truth label identification method called Ground-truth Label Identification via Label Influence Function (GLI-LIF), the objective function can be expressed as follows:

$$y = \arg \max_{j \in Y, l \in Y \setminus j} \{ \|\Delta \hat{\mathbf{w}}_j\|_1, \|\Delta \hat{\mathbf{w}}_l\|_1 \}$$

$\|\cdot\|_1$  denotes the  $\ell_1$ -norm.

$$\Delta \hat{\mathbf{w}}_j = \epsilon \mathcal{I}(\mathbf{z})$$

$$\Delta \hat{\mathbf{w}}_l = \varepsilon (\mathcal{I}(\mathbf{z}_\delta) - \mathcal{I}(\mathbf{z}))$$

$$\mathcal{I}(\mathbf{z}) \triangleq \frac{d \hat{\mathbf{w}}_{\epsilon, -\mathbf{z}}}{d \epsilon} \Big|_{\epsilon=0} = -H_{\hat{\mathbf{w}}}^{-1} \nabla_{\mathbf{w}} \ell(\mathbf{y}, f(\mathbf{x}; \hat{\mathbf{w}}))$$

where  $H_{\hat{\mathbf{w}}} = \frac{1}{n} \sum_{i=1}^n \nabla_{\mathbf{w}}^2 \ell(\mathbf{y}_i, f(\mathbf{x}_i; \hat{\mathbf{w}}))$  is the Hessian matrix and is positive definite by assumption.

# Experiment Results

Table 3: Win/tie/loss counts of pairwise t-test (at 5% significance level) between PLL-IF+NN and each baseline.

Method Config.	PLL-IF+NN vs -					
	PL-SVM	CLPL	M3PL	SURE	PRODEN	PL-BLC
varying p, r = 1	54\0\0	54\0\0	54\0\0	53\1\0	53\1\0	47\7\0
varying p, r = 2	54\0\0	54\0\0	54\0\0	54\0\0	47\4\3	42\6\6
varying p, r = 3	54\0\0	54\0\0	54\0\0	54\0\0	50\3\1	46\3\5
Total	162\0\0	162\0\0	162\0\0	161\1\0	150\8\4	135\16\11

Table 4: Win/tie/loss counts of pairwise t-test (at 5% significance level) between PLL-IF+SVM and each baseline.

Method Config.	PLL-IF+SVM vs -					
	PL-SVM	CLPL	M3PL	SURE	PRODEN	PL-BLC
varying p, r = 1	54\0\0	51\3\0	45\5\4	40\4\10	24\4\26	9\3\42
varying p, r = 2	54\0\0	54\0\0	51\3\0	46\5\3	12\3\39	8\1\45
varying p, r = 3	54\0\0	52\2\0	49\4\1	38\4\12	8\3\43	16\5\33
Total	162\0\0	157\5\0	145\12\5	124\13\25	44\10\108	33\9\120

Table 5: Mean accuracy  $\pm$  standard deviation via five-fold cross validation on six real-world datasets for all methods. The best results are in bold.  $\bullet/\circ$  indicates that our method ( PLL-IF+NN / PLL-IF+SVM ) is significantly superior / inferior than the baseline (pairwise t-test at 5% significance level).

Method	Lost	MSRCv2	Mirflickr	BirdSong	Soccer Player	Yahoo!News
PLL-IF+NN	<b>0.809 <math>\pm</math> .041</b>	<b>0.538 <math>\pm</math> .027</b>	<b>0.569 <math>\pm</math> .030</b>	<b>0.753 <math>\pm</math> .003</b>	<b>0.560 <math>\pm</math> .004</b>	<b>0.683 <math>\pm</math> .007</b>
PLL-IF+SVM	0.782 $\pm$ .012	0.513 $\pm$ .022	0.561 $\pm$ .003	0.723 $\pm$ .017	0.554 $\pm$ .010	0.646 $\pm$ .026
PL-SVM	0.691 $\pm$ .012•	0.481 $\pm$ .037•	0.441 $\pm$ .061•	0.661 $\pm$ .067•	0.462 $\pm$ .006•	0.615 $\pm$ .015•
CLPL	0.732 $\pm$ .032•	0.433 $\pm$ .020•	0.549 $\pm$ .017	0.635 $\pm$ .019•	0.367 $\pm$ .004•	0.471 $\pm$ .049•
M3PL	0.747 $\pm$ .031•	0.499 $\pm$ .026•	0.480 $\pm$ .016•	0.694 $\pm$ .065•	0.440 $\pm$ .005•	0.623 $\pm$ .062•
SURE	0.767 $\pm$ .026	0.508 $\pm$ .021	0.562 $\pm$ .015	0.702 $\pm$ .025•	0.531 $\pm$ .014	0.632 $\pm$ .015•
PRODEN	0.765 $\pm$ .014	0.452 $\pm$ .017•	0.524 $\pm$ .011	0.721 $\pm$ .004	0.559 $\pm$ .005	0.674 $\pm$ .005
PL-BLC	0.806 $\pm$ .032	0.536 $\pm$ .037	0.558 $\pm$ .038	0.746 $\pm$ .017	0.540 $\pm$ .008	0.679 $\pm$ .005

# References

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Thank you!