# Intermediate Layer Optimization for Inverse Problems using Deep Generative Models

**ICML 2021** 

Giannis Daras\*, Joseph Dean\*, Ajil Jalal, Alexandros G. Dimakis The University of Texas at Austin

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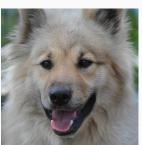
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The central question that we want to address in this work is how to optimally use pre-trained generative models to solve inverse problems.

#### Contributions:

We propose a novel optimization method, Intermediate Layer
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- We theoretically analyze our framework by establishing sample complexity and error bounds.
- We show experimentally significant improvements over previous state-of-the-art methods for solving inverse problems with pre-trained generators.

## **Problem Setup and Prior Work**

Goal: Recover an unknown image x by observing some noisy measurements  $\mathcal{A}(x) + \eta$ . Prior work:

• CSGM [1]. Assume access to a pre-trained generator  $G(z): \mathbb{R}^k \to \mathbb{R}^n$ . Use Gradient Descent to solve the following problem:

$$z^* = \min_{z \in \mathbb{R}^k} ||\mathcal{A}(G(z)) - \mathcal{A}(x)||. \tag{1}$$

 PULSE [2]. Improves upon CSGM by refining the latent space optimization and using the StyleGAN [3, 4] pretrained model. Excellent results for super-resolution.

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- Pre-trained generators reflect or amplify dataset biases.
- Existing algorithms fail to achieve reconstruction of images that are outside of the training distribution.
- Previous state-of-the-art methods address each inverse problem separately, instead of providing a unified framework to solve all of them.

We propose Intermediate Layer Optimization (ILO), a novel optimization algorithm that expands the range of the generator to solve general inverse problems. Our algorithm has the following key ideas:

• We split the generator G into multiple parts, i.e.  $G = G_l \circ G_{l-1} \circ ... \circ G_2 \circ G_1$ .

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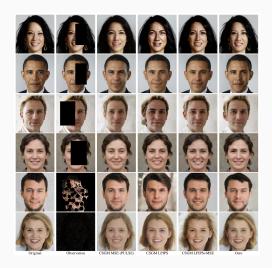
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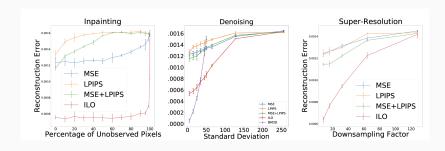
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- We follow this idea to optimize over the input space of deeper layers, effectively expanding the range of the generator.
- To avoid overfitting to the measurements, we constrain the solutions
  of the optimization problem to an l<sub>1</sub> ball around the range of the
  previous layer.

# **Experiments (Visual Results)**



## **Experiments (Qualitative Results)**



# Experiments (Out of distribution generation)



## ILO (Theory)

#### Theorem

Let  $G = G_2 \circ G_1$  with  $G_1 : \mathbb{R}^k \to \mathbb{R}^p$  be an  $L_1$ -Lipschitz function and  $G_2 : \mathbb{R}^p \to \mathbb{R}^n$  be an  $L_2$ -Lipschitz function. Let  $A \in R^{m \times n}$  be the measurements matrix with  $A_{ij} \sim \mathcal{N}(0, 1/m)$  i.i.d. entries.

Let K be a parameter of our choice where  $K \leq \sqrt{p}$ , and  $r_2 = \frac{K\delta}{L_2}$ . Consider the true optimum in the extended range

$$\bar{z}^p = \operatorname{argmin}_{z^p \in G_1(B_2^k(r_1)) \oplus B_1^p(r_2)} ||x - G_2(z^p)||, \tag{2}$$

and the measurements optimum in the extended range

$$\tilde{z}^{p} = \operatorname{argmin}_{z^{p} \in G_{1}(B_{2}^{k}(r_{1})) \oplus B_{1}^{p}(r_{2})} ||Ax - AG_{2}(z^{p})||. \tag{3}$$

Then, if the number of measurements is sufficiently large:

$$m = \frac{1}{(1 - \gamma)^2} \Omega\left(k \log \frac{L_1 L_2 r_1}{\delta} + K^2 \log p\right),\tag{4}$$

then with probability at least  $1-e^{-\Omega((1-\gamma)^2\cdot m)}$ , we have the following error bound:

$$||x - G_2(\tilde{z}^p)|| \le \left(1 + \frac{4}{\gamma}\right) ||x - G_2(\bar{z}^p)||$$

$$+ \delta \cdot \frac{\log(4K)}{\gamma} \cdot \frac{\sqrt{p}}{K} \log \frac{\sqrt{p}}{K}.$$
(5)

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