

# Message Passing Adaptive Resonance Theory for Online Active Semi-supervised Learning

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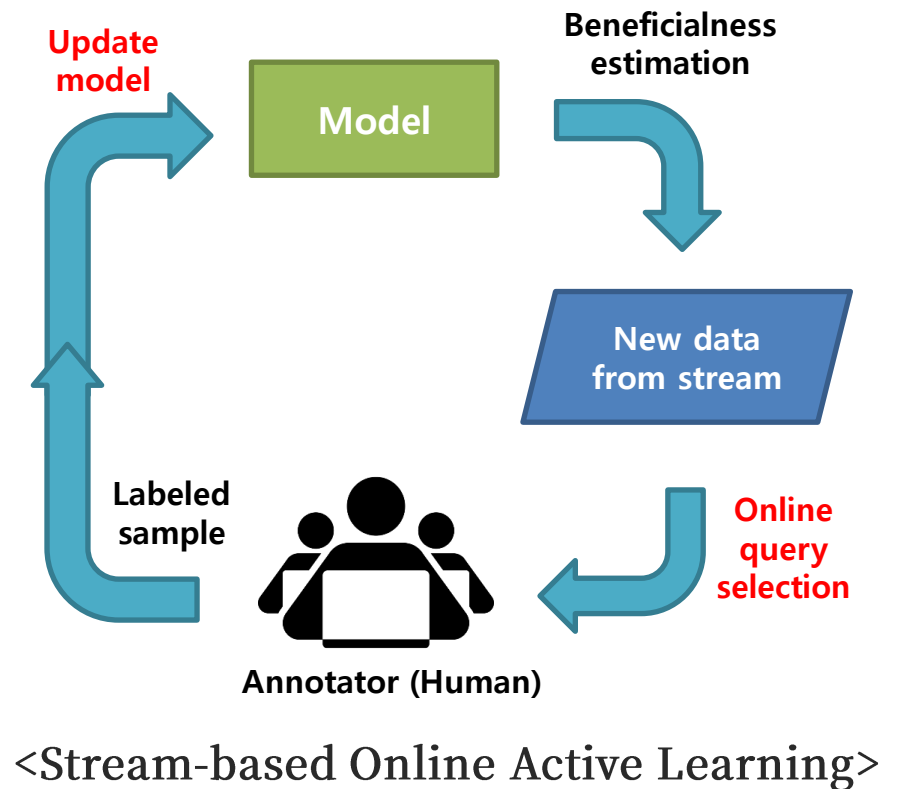
# The Real-world Problems

❖ The recent success of deep learning is largely attributed to massive amount of labeled data.

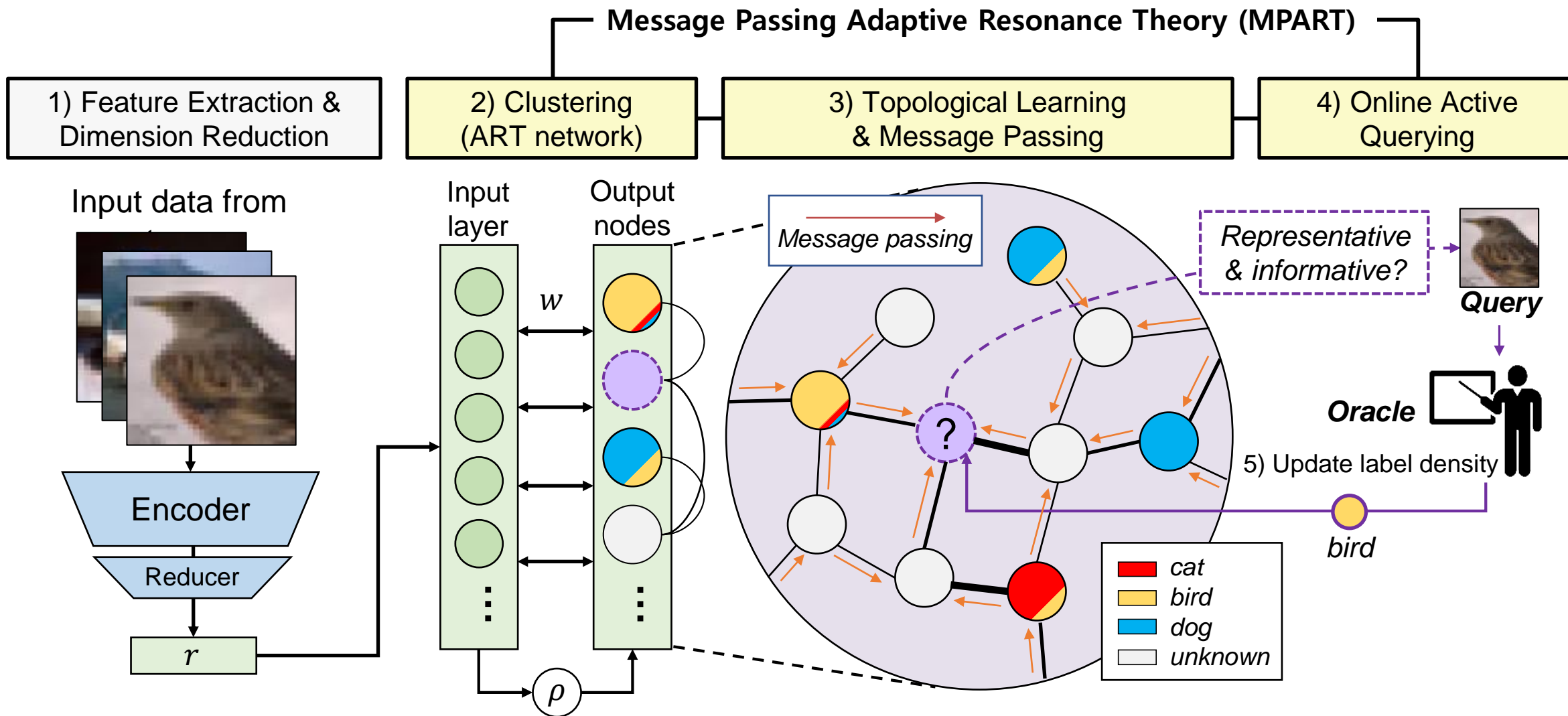
❖ **However, the real-world problems..**

- Most of the data samples are **not labeled**.
- The **collection and storage** of personal data are **prohibited** due to privacy concerns.

❖ This burden impedes the **widespread** use of deep learning in **real-world applications**.

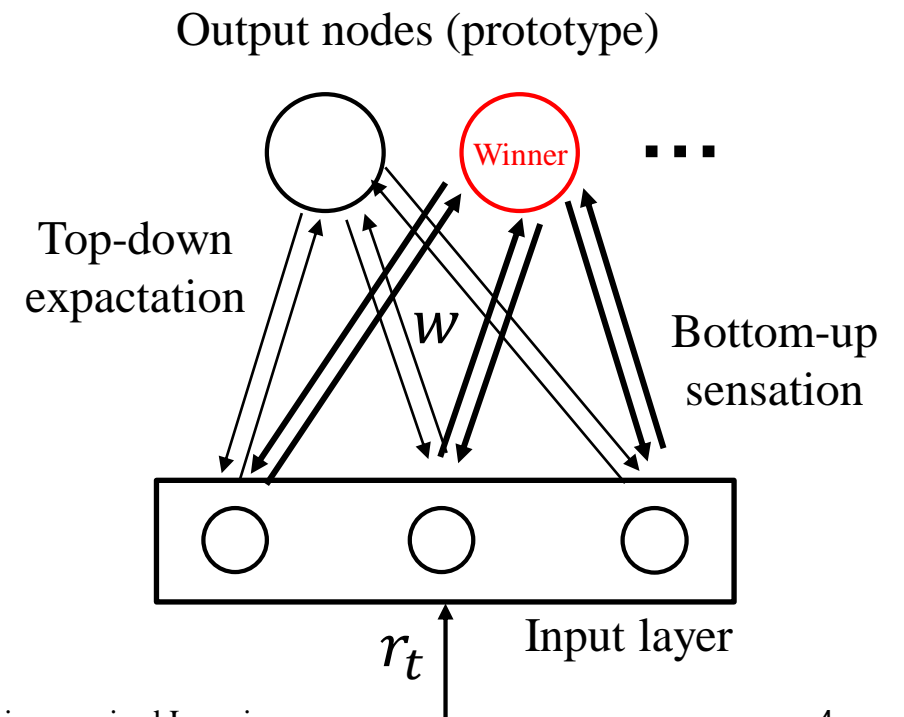


# Model Overview

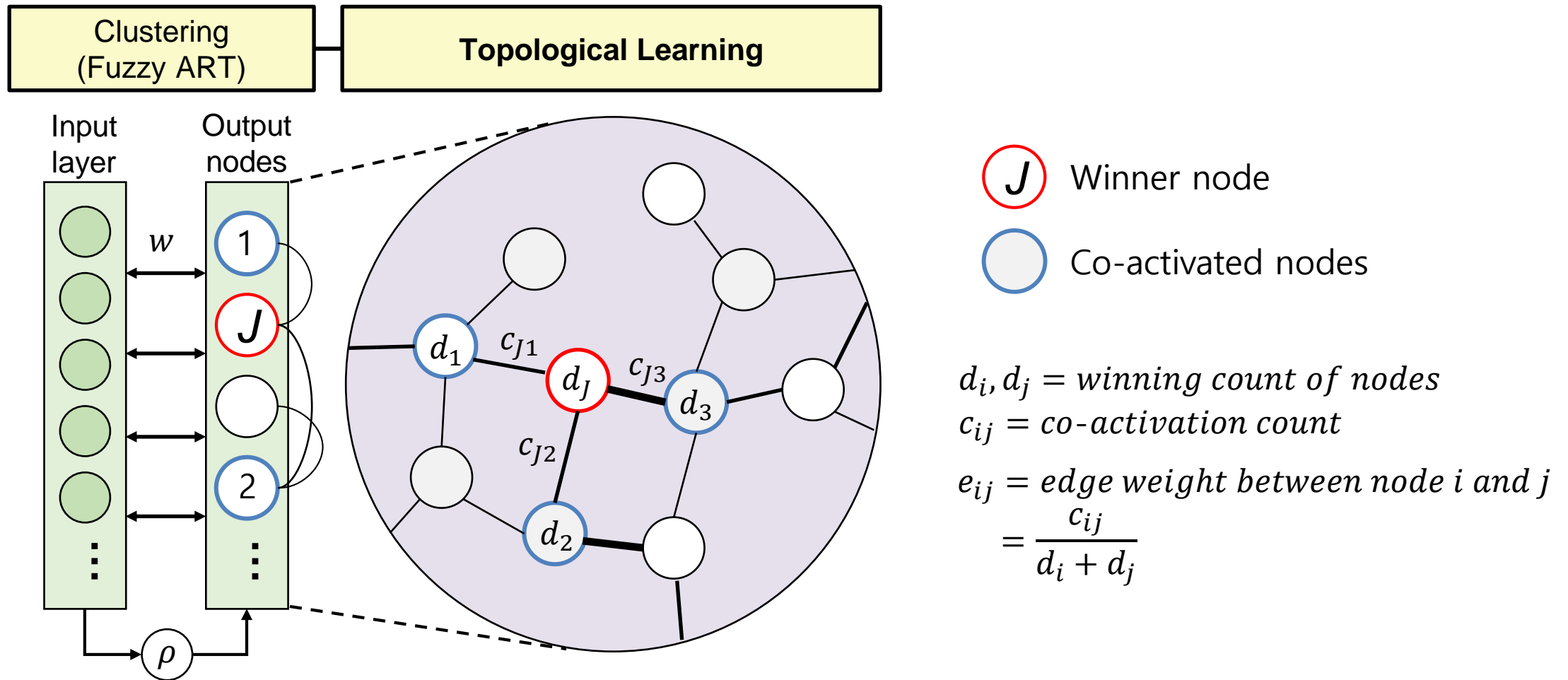


# ART Networks

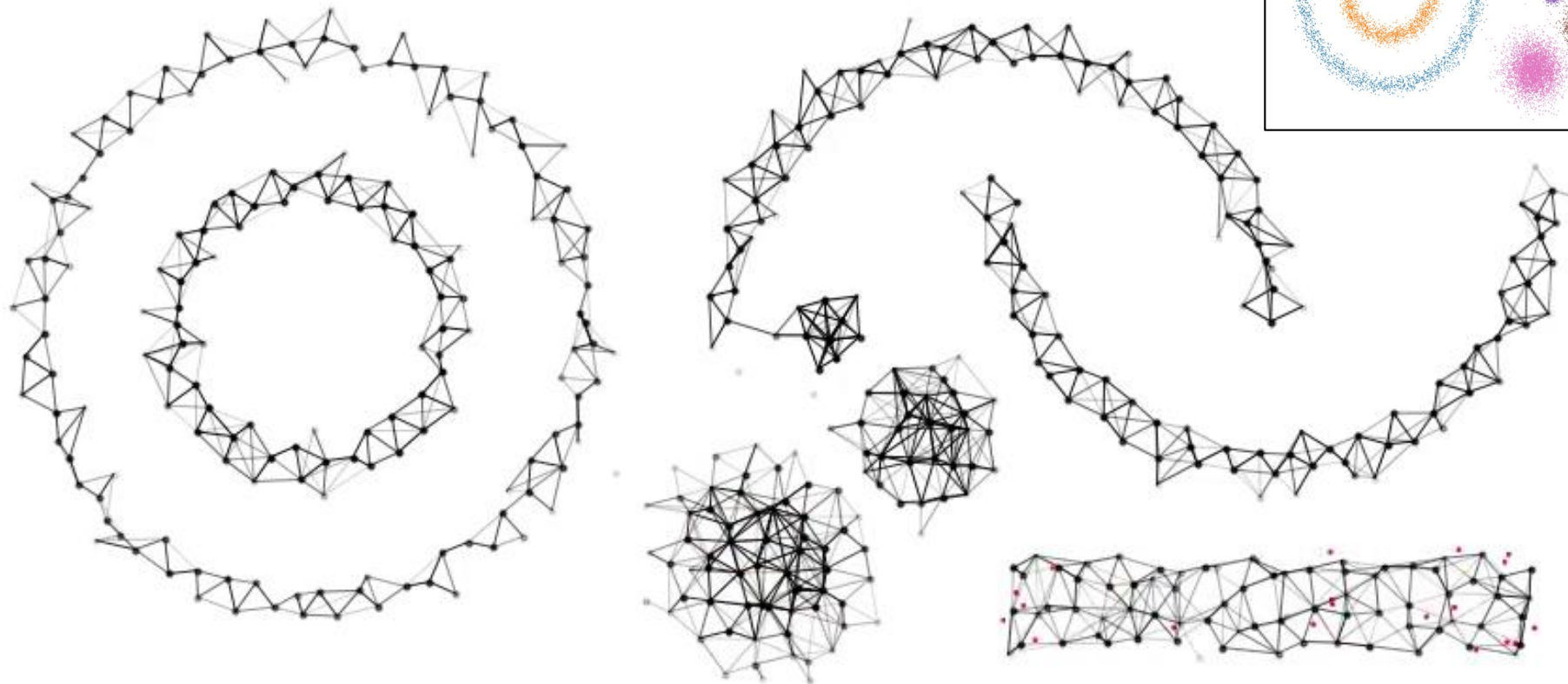
- ❖ Adaptive Resonance Theory (ART), inspired by brain information processing mechanisms, is an **unsupervised learning method** for pattern recognition.
- ❖ In terms of **being conservative while learning new**, the ART networks can be a **solution for the online learning**.
- ❖ We use Fuzzy ART to **form nodes in a topological graph** through clustering of input data.



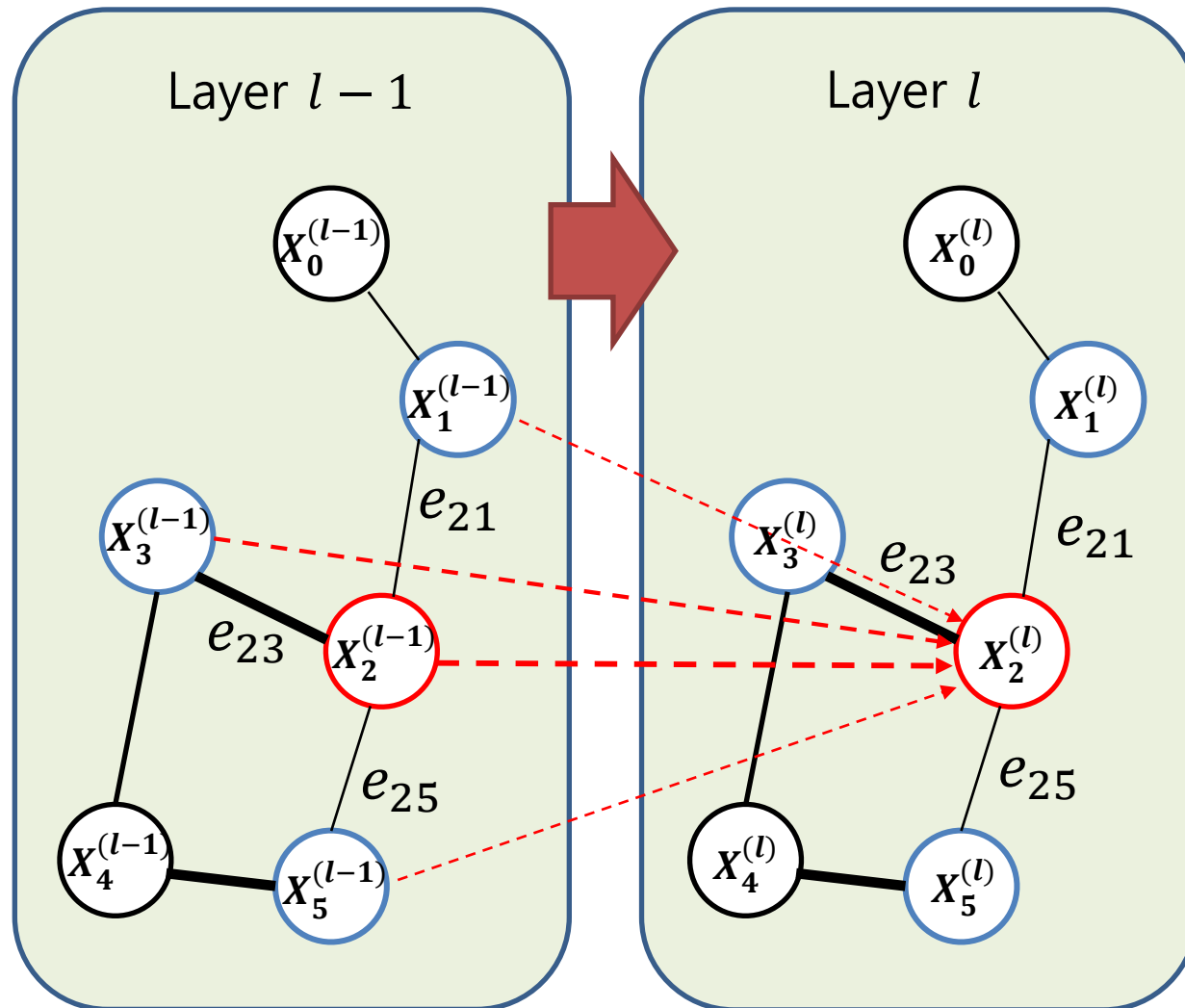
# Topology Learning with MPART



# Topology Learning with MPART



# Message Passing



$$X_i^{(l)} = X_i^{(l-1)} + \delta \sum_{j \in \mathcal{N}_i^{(l-1)}} e_{ij} X_j^{(l-1)}$$

$X_i^{(l)}$  = an information vector

$\mathcal{N}_i^{(l)}$  = a set of  $l$ -hop neighbors

$\mathcal{N}_i^{(0:l)}$  = a union of  $\mathcal{N}_i^{(0)}, \dots, \mathcal{N}_i^{(l)}$

$e_{ij}$  = edge weight

$\delta$  = propagation rate

# Node Classification

- ❖ **The class information  $q_i$**  of a node  $i$ , called the *label density*, is a distribution over a set of known class labels  $C$ .
  - Indicates how probable the node belongs to each class.
  - When a label  $y_t$  is provided with an input  $x_t$ , the corresponding density value in the winner  $J_t$ , i.e.  $q_{J_t}(y_t)$ , increases by 1.
- ❖ **Infers the class of input  $x_t$  by aggregating the class information of neighboring nodes.**
  - We obtain the class probability distribution  $p_t$  of winner node  $J_t$  by performing  $L$ -layer message passing and normalizing it as follows.

$$p_t(y) = q_{J_t}^{(L)}(y) / \sum_{y' \in C} q_{J_t}^{(L)}(y')$$



# Density-Weighted Uncertainty Estimation

❖ We use two kinds of uncertainty measures for nodes.

- Combine them to get a query selection score.

$$u_e = 1 - \tanh\left(k_e \sum_{y \in \mathcal{C}} q_{J_t}^{(L)}(y)\right) \quad u_a = \begin{cases} \frac{-\sum_{y \in \mathcal{C}} p_t(y) \log(p_t(y))}{\log(|\mathcal{C}|)}, & \text{if } |\mathcal{C}| > 1 \\ 0, & \text{otherwise} \end{cases}$$

$$u_t = \tau \cdot u_e + (1 - \tau) \cdot u_a$$

❖ Finally, the **density-weighted query selection score**  $s_t$  using **distribution density**  $d_{J_t}^{(L)}$  is defined as follows.

$$d_i^{(l)} = d_i^{(l-1)} + \delta \sum_{j \in \mathcal{N}_i} e_{ij} d_j^{(l-1)}$$

$$s_t = \tanh\left(k_d \cdot d_{J_t}^{(L)}\right) \cdot u_t$$

# Tasks

- ❖ Online active learning task for **stream-based selective sampling**.
  - **Multi-class classification**, where the **number of classes is not known**.
  - The number of queries is limited to a **fixed budget  $B$**  within a **period of  $W$**  consecutive inputs. (Query frequency =  $B/W$ )
- ❖ Experimental settings
  - **Four kinds of datasets with different distributions**: Mouse retina transcriptomes, Fashion MNIST, EMNIST Letters, and CIFAR-10.
  - Query frequency:  **$B = 1$  or  $2$ ,  $W = 100, 500, 1,000$  or  $2,000$  (e.g.  $1/1000, 1/500$ ).**
  - We only used **10,000 randomly sampled data from the training split per trial**.  
→ The total query budget is 10~100.

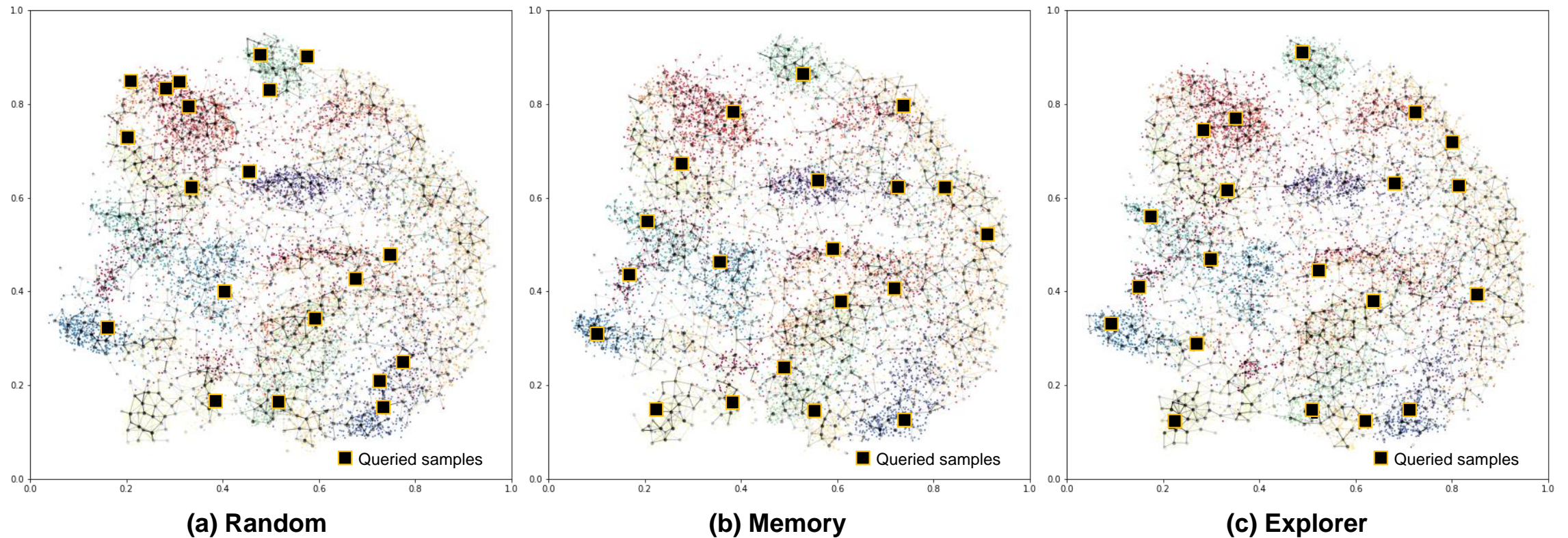
# Query Selection Strategy

- ❖ **Random** : A random query is selected from a sequence of inputs.
- ❖ **Memory** : The model has a memory that can store one sample.
  - One sample with **the maximum query selection score** is stored.
  - The stored sample is queried at the end of the query period.
- ❖ **Explorer** : The model **cannot store any input sample**.
  - **Selects  $B$  samples online** for each query period  $W$ .
  - **The uncertainty distribution** of input data is continuously **estimated**.
  - Useful samples are selected by predicting the beneficialness.

# Experimental Results

## ❖ Visualization of training results on EMNIST Letters

- The number of layer  $L = 3$  and  $B/W = 1/1000$  were used.



# Conclusions

- ❖ We propose **Message Passing Adaptive Resonance Theory (MPART)** for online active semi-supervised learning.
- ❖ **MPART learns the distribution and the topology of the input data online, infers the class of unlabeled data, and selects the informative and representative samples through message passing** between nodes on the topological graph.
- ❖ We believe MPART offers new opportunities for machine learning techniques to be widely used in real-world applications.

