# Large-Scale Meta-Learning with Continual Trajectory Shifting

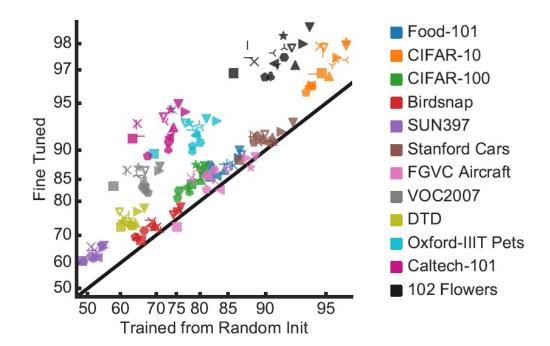
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(\*: Equal contribution)

**ICML 2021** 

# **Beyond Few-shot Learning**

- Meta-learning is effective for solving few-shot learning.
- What if **many-shot**? We already know that knowledge transfer is effective for many-shot dataset as well (e.g. ImageNet finetuning).

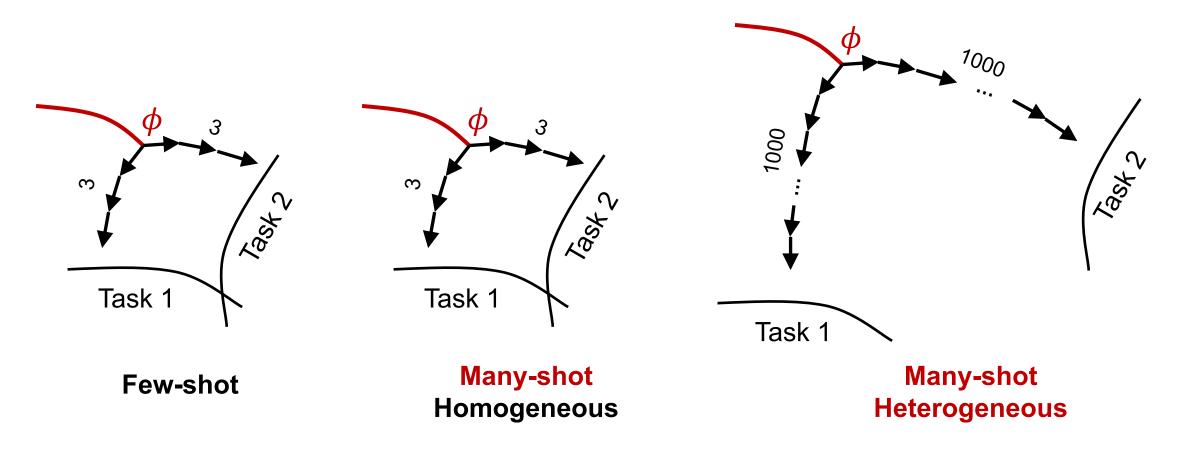


Kornblith et al., Do Better ImageNet Models Transfer Better?, CVPR 2019

# Large-Scale Meta-Learning

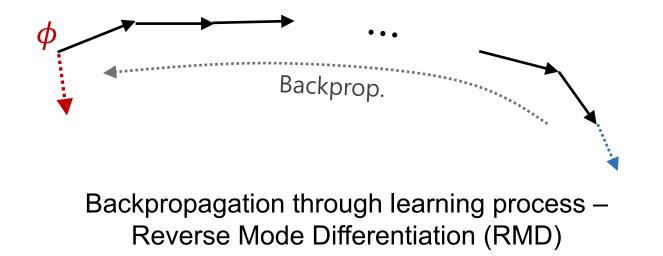
Large-scale meta-learning: many-shot and heterogeneous task distribution.

 $\rightarrow$  Requires long horizon for inner-optimizations.



### Large-Scale Meta-Learning

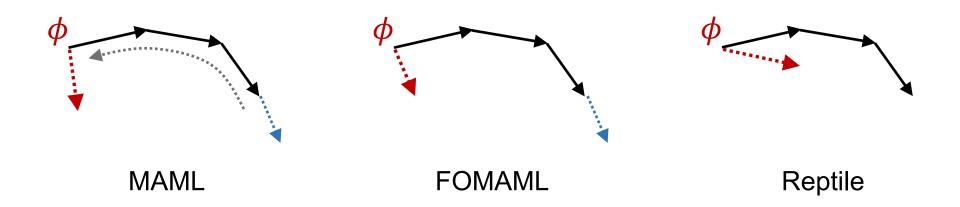
High computational cost of backpropagating through long inner process.



Franceschi et al., Forward and Reverse Gradient-Based Hyperparameter Optimization, ICML 2017

## **First-order Approximations**

First-order approximation can be used to reduce the computational cost.



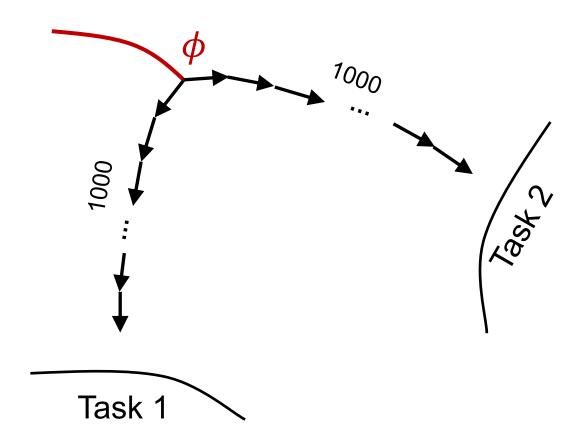
However, even Reptile is inefficient for long-horizon case.



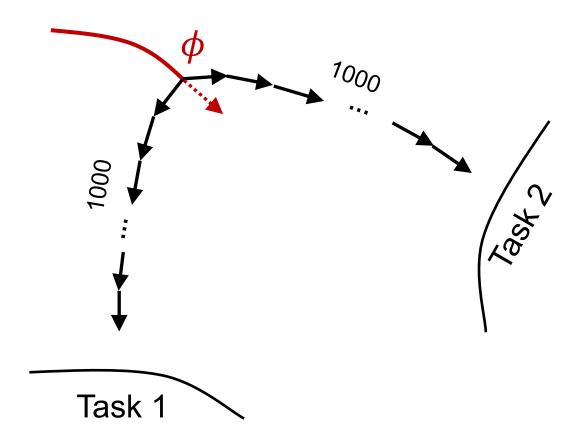
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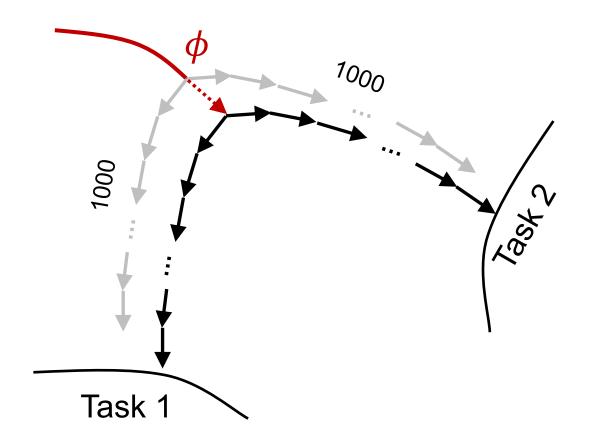
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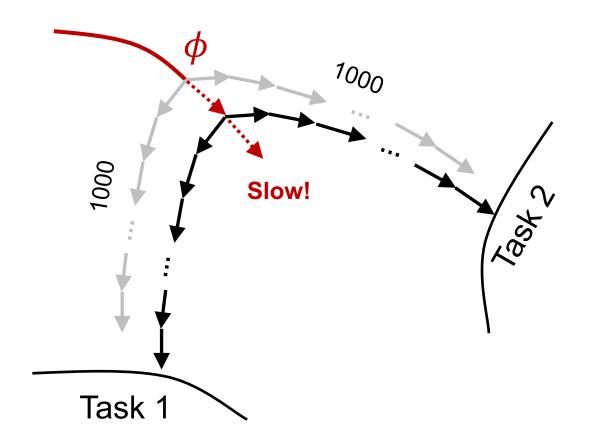
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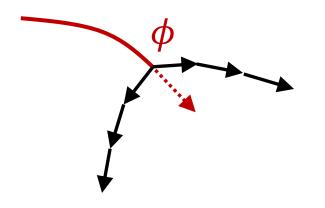
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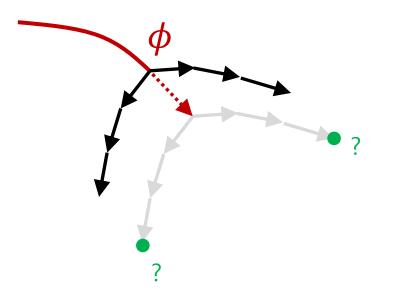


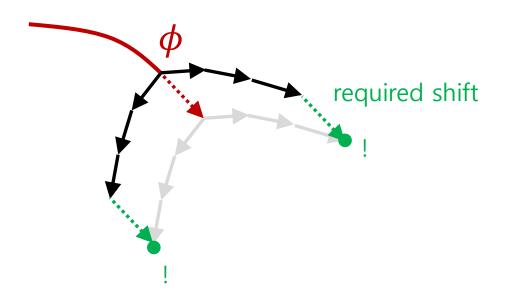
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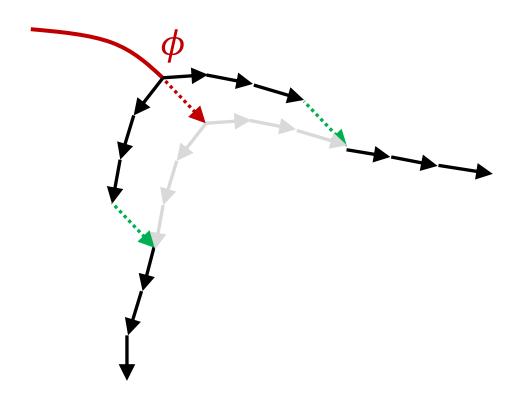


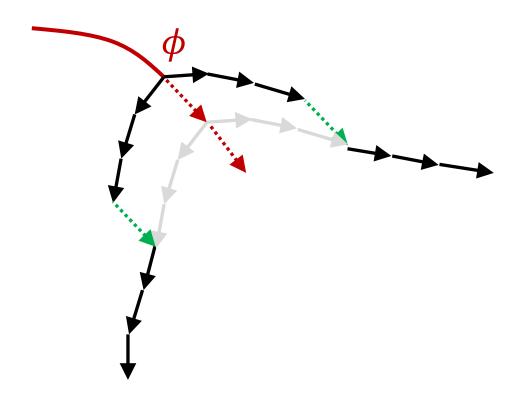
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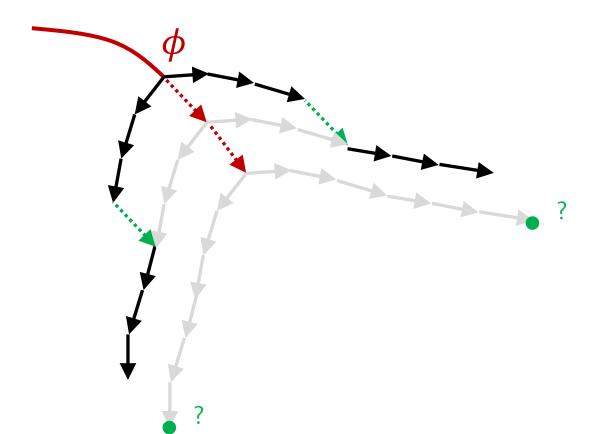


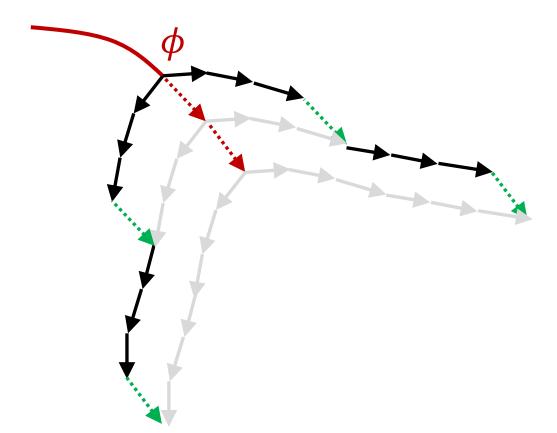


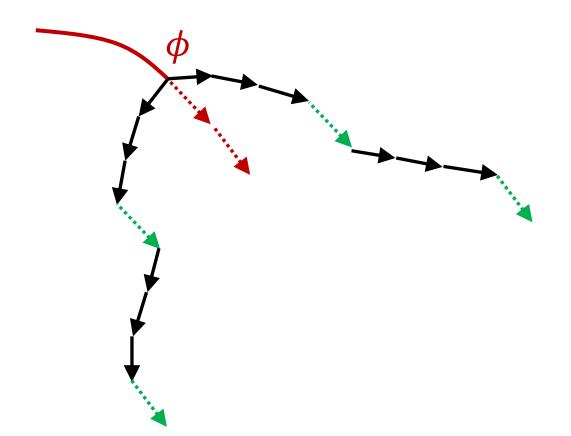






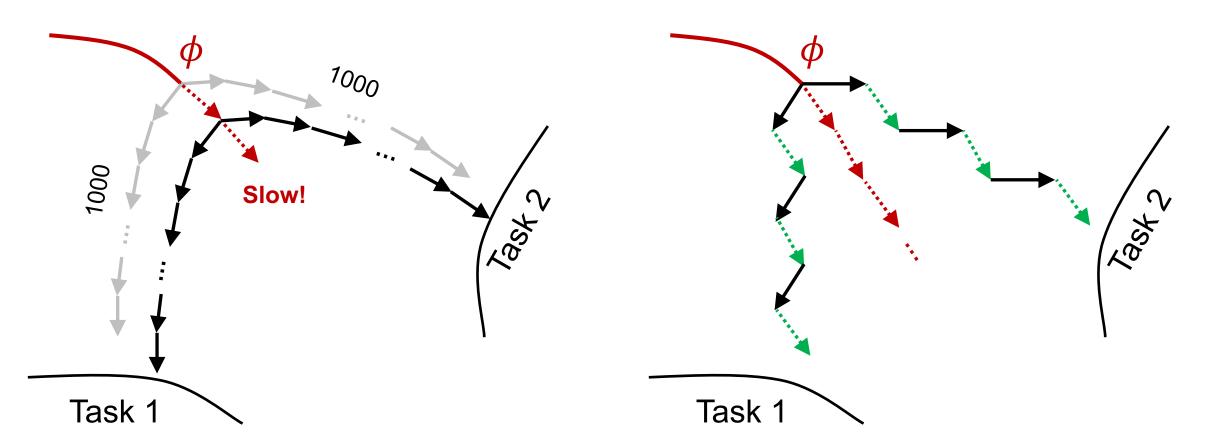






If we perform trajectory shifting for every meta-update...

 $\rightarrow$  1000 times more frequent meta-update !!



#### **How to Estimate?**

 $U_3(\dot{\phi})$ 

 $U_3(\phi + \Delta)$ 

**1.** First-order Taylor Approximation ( $U_k(\phi)$  : Update k steps from  $\phi$ )

$$U_k(\phi + \Delta) \approx U_k(\phi) + \frac{\partial U_k(\phi)}{\partial \phi} \Delta$$

2. Hessian Approximation

$$\frac{\partial U_k(\phi)}{\partial \phi} = \frac{\partial U_k(\phi)}{\partial U_{k-1}(\phi)} \cdots \frac{\partial U_2(\phi)}{\partial U_1(\phi)} \frac{\partial U_1(\phi)}{\partial \phi} = \prod_{i=0}^{k-1} (I - \alpha H_i) \approx I$$

Therefore,

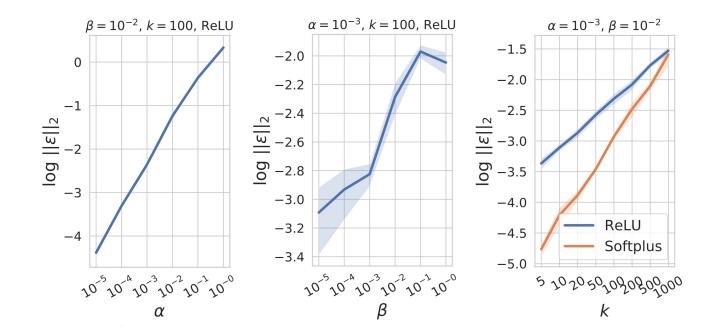
 $U_k(\phi + \Delta) \approx U_k(\phi) + \Delta$ 

#### **Approximation Error**

The approximation errors compound as we keep shifting.

1 shift  $\rightarrow U_1(\phi + \Delta) = U_1(\phi) + \Delta + O(\beta \alpha h + \beta^2)$ 

K shift 
$$\rightarrow U_k(\phi + \Delta_1 + \dots + \Delta_{k-1})$$
  
=  $U_1(\dots U_1(U_1(\phi) + \Delta_1) \dots + \Delta_{k-1}) + O(\beta \alpha h k^2 + \beta^2 k)$ 



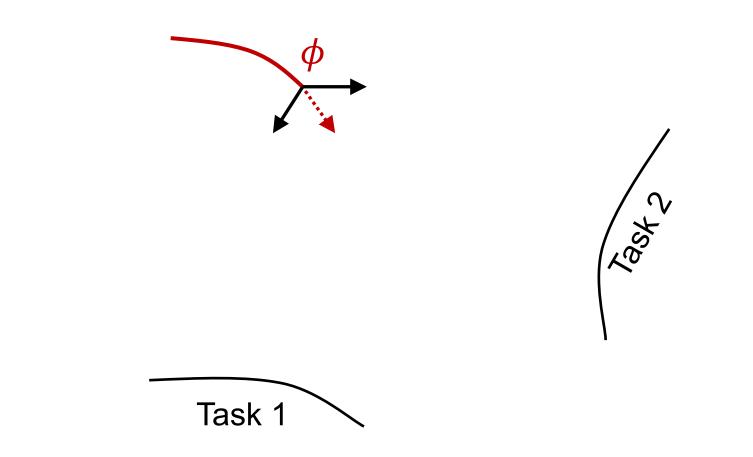
Then, why should it work?

 $U_3(\dot{\phi})$ 

 $U_3(\phi + \Delta)$ 

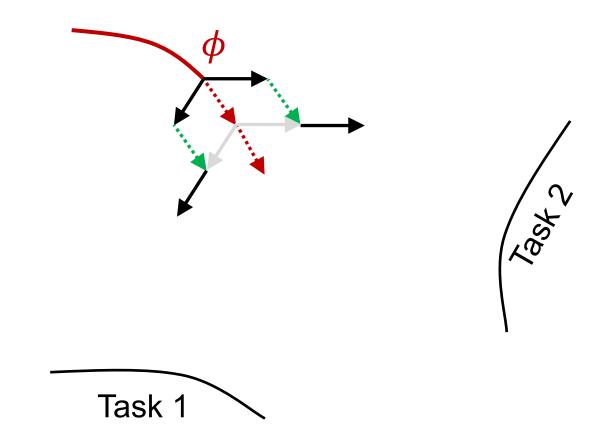
# **Gradually Increasing k**

The horizon size *k* gradually increases. What does it mean?



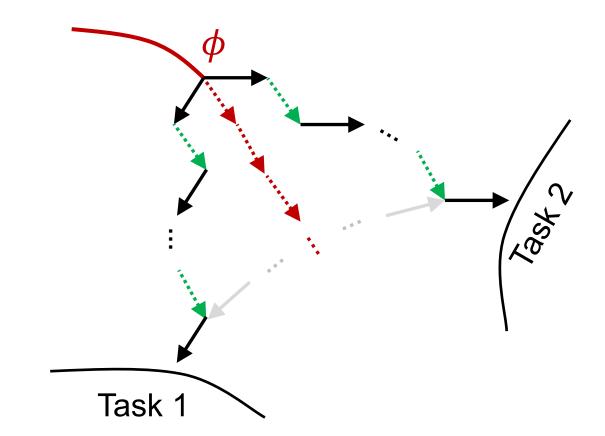
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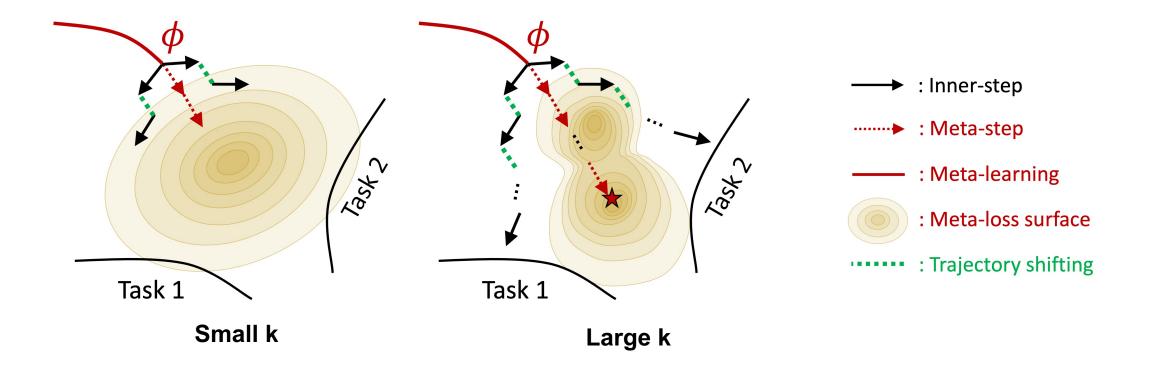
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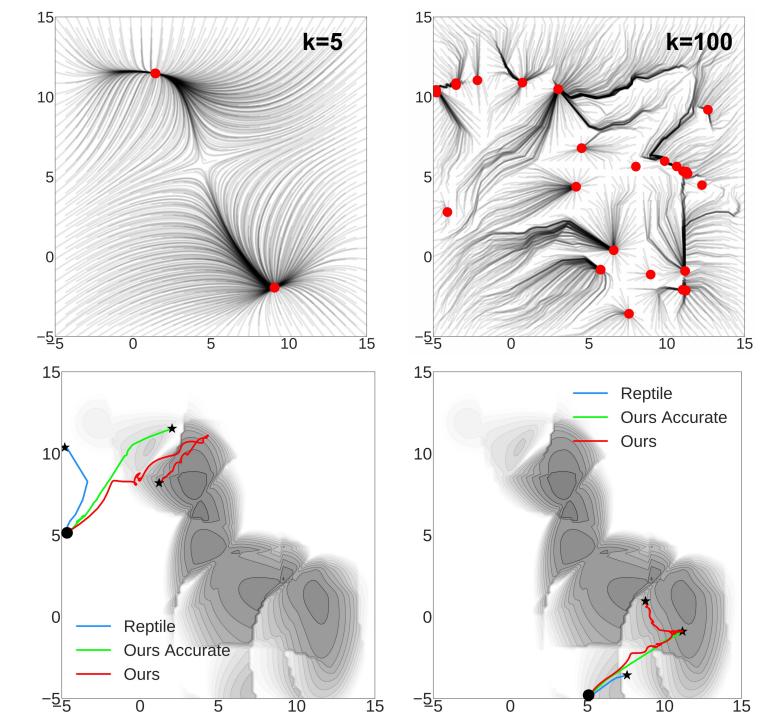


### **Meta-Level Curriculum Learning**

Meta loss surface is smoother for smaller k  $\rightarrow$  regularization effect !



# Synthetic Experiment



### **Experiments – Image Classification**

We experiment with large-scale (many-shot and heterogeneous) datasets.

Meta-train with seven datasets:

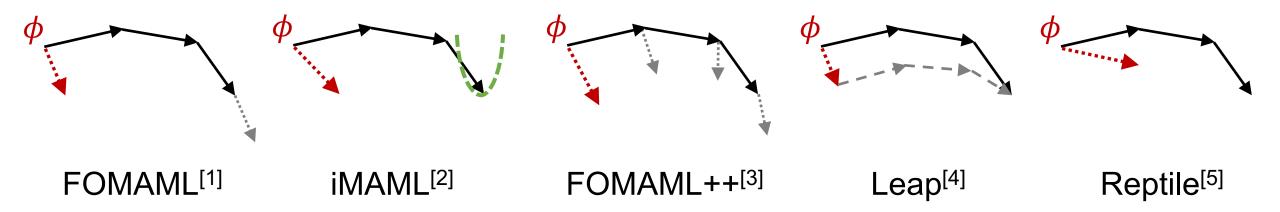
Tiny ImageNet, CIFAR-100, Stanford Dogs, Aircraft, CUB, Fashion-MNIST, and SVHN.

**Meta-test** with five datasets:

Stanford Cars, QuickDraw, VGG-Flowers, VGG-Pets, and STL10.

#### **Baselines**

We compare with the following first-order meta-learning algorithms. Our method (Continual Trajectory Shifting) has been applied to Reptile.



[1] Finn et al. 17 Model-Agnostic Meta-Learning for Fast Adaptation of Deep Networks.

[2] Rajeswaran, et al. 19, Meta-learning with implicit gradients.

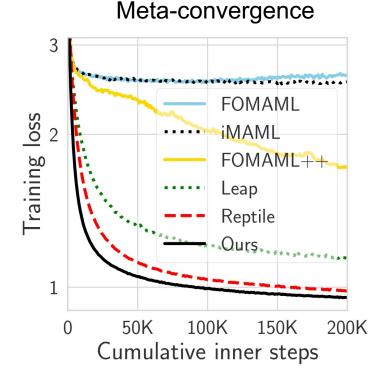
[3] Antoniou et al. 19, How to train your MAML.

[4] Flennerhag et al. 18, Transferring Knowledge across Learning Processes.

[5] Nichol et al. 18, On First-Order Meta-Learning Algorithms.

## **Image Classification Results**

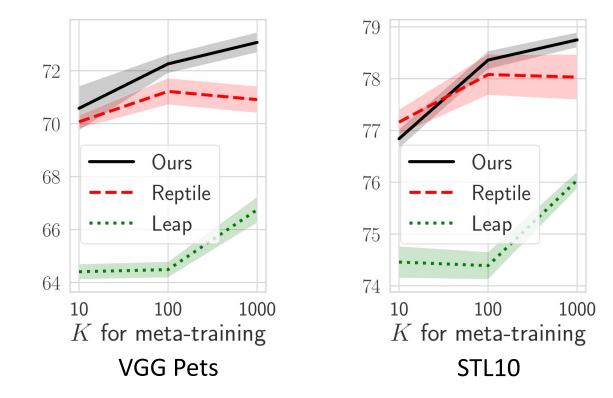
Our method outperforms meta-learning baselines, in terms of **meta-convergen ce** and **test accuracy**.



Meta-test time test accuracy 547870 527650 65 7472 48 60 7046 5568 44 5K 10K 20K 50K 100K 200K 5K 10K 20K 50K 100K 200K 10K 20K 50K 100K 200K 5K Cumulative inner steps Cumulative inner steps Cumulative inner steps Quickdraw **VGG Pets STL10** 

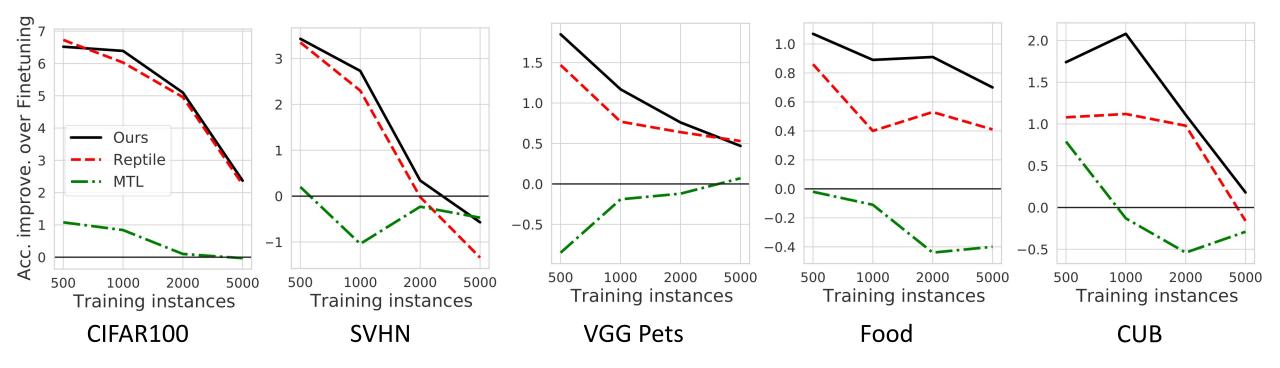
# Large K is better for many-shot

Longer inner trajectory shows better performance for many-shot learning.



#### **Improving on ImageNet Pretraining**

Our method outperforms ImageNet finetuning under limited data regime.



#### **Takeaways**

- If the task distribution is many-shot and heterogeneous, we need to increase the length of inner-optimization trajectory.
- In solving the problem, first-order approximations are still inefficient in terms of meta-update frequency.
- We can greatly increase the meta-update frequency by continuously shift the inner-learning trajectories w.r.t each meta-update.