Iterative Linearized Control: Stable Algorithms and Complexity Guarantees

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Problem

Nonlinear control $\begin{array}{rcl} & \longrightarrow & \text{Iterative linearization (ILQR)} \\ & \text{around current } x_t, u_t \\ & \text{around current } x_t, u_t \\ & \underset{x_0, \dots, x_T}{\min} \sum_{t=0}^{T} \left(h_t(x_t) + g_t(u_t) \right) \\ & \text{s.t.} & x_{t+1} = \phi_t(x_t, u_t) \\ & x_0 & = \hat{x}_0 \end{array}$

ightarrow Next iterate $u_t^+ = u_t + v_t^*$

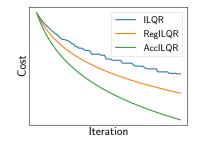
Questions

- 1. Does ILQR converge? Can it be accelerated?
- 2. How do we characterize complexities for nonlinear control?

Contributions

Regularized and Accelerated ILQR

- 1. ILQR is Gauss-Newton
 - \rightarrow Regularized ILQR gets convergence to a stationary point
- 2. Potential acceleration by extrapolation steps
 - \rightarrow Accelerated ILQR akin to Catalyst acceleration



Contributions

Oracles complexities

- 1. Oracles are solved by dynamic programming
 - \rightarrow Gradient and Gauss-Newton have both cost in $\mathcal{O}(\mathcal{T})$
- 2. Automatic-differentiation software libraries available
 - \rightarrow Use auto.-diff. as oracle for direct implementation

Code summary available at https://github.com/vroulet/ilqc

```
dynamics, cost = define_ctrl_pb()
ctrl = rand(dim_ctrl)
auto_diff_oracle = define_auto_diff_oracle(ctrl, dynamics)
dual_sol = sovle_dual_step(ctrl, cost, auto_diff_oracle)
next_ctrl = get_primal(dual_sol, auto_diff_oracle, cost)
```

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