# Learning Context-dependent Label Permutations for Multi-label Classification

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Amazon Alexa AI

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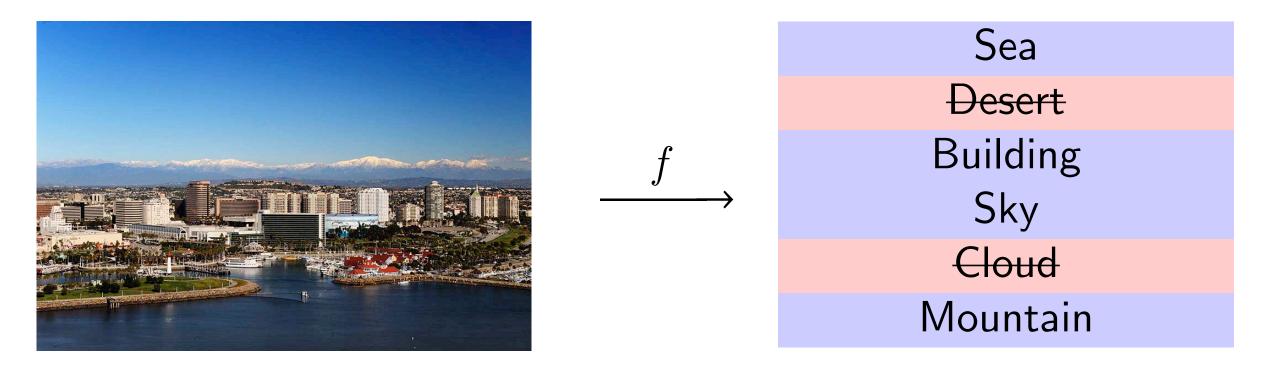
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# Multi-label Classification (MLC)

• Goal: learn a function f that maps instances to a subset of labels

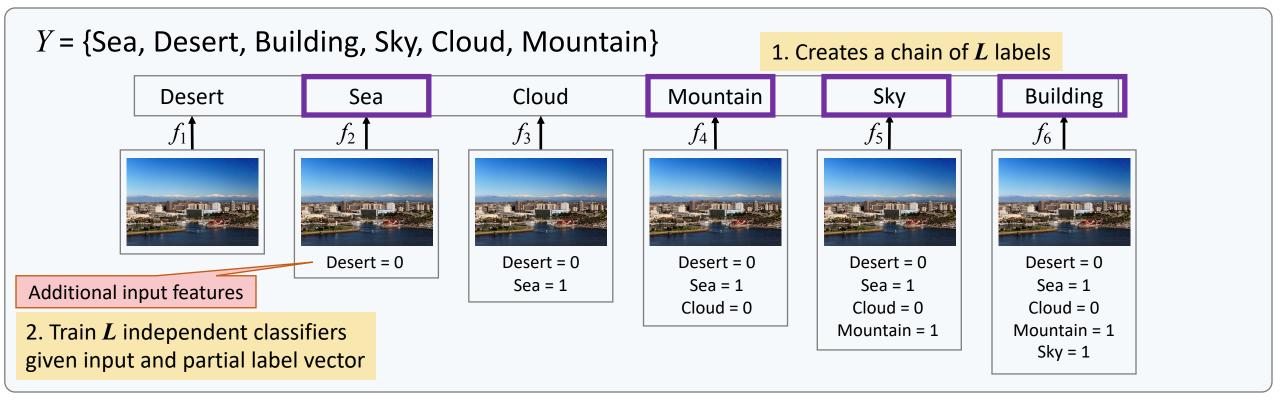


- It is important to take into account *label dependencies*.
- Joint probability of labels

$$P(y_1, y_2, \cdots, y_L | \boldsymbol{x}) = \prod_{i=1}^L P(y_i | \boldsymbol{y}_{< i}, \boldsymbol{x})$$

#### Maximization of the joint probability

- Traditional approaches for minimizing **subset 0/1 loss**:
  - (Probabilistic) classifier chain (Dembczyński et al., ICML 2010; Read et al., MLJ 2011)

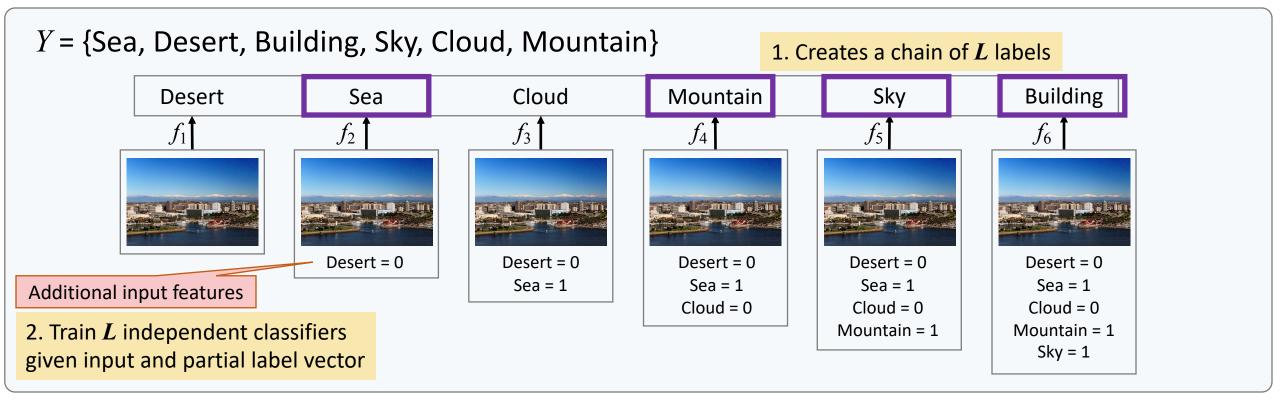


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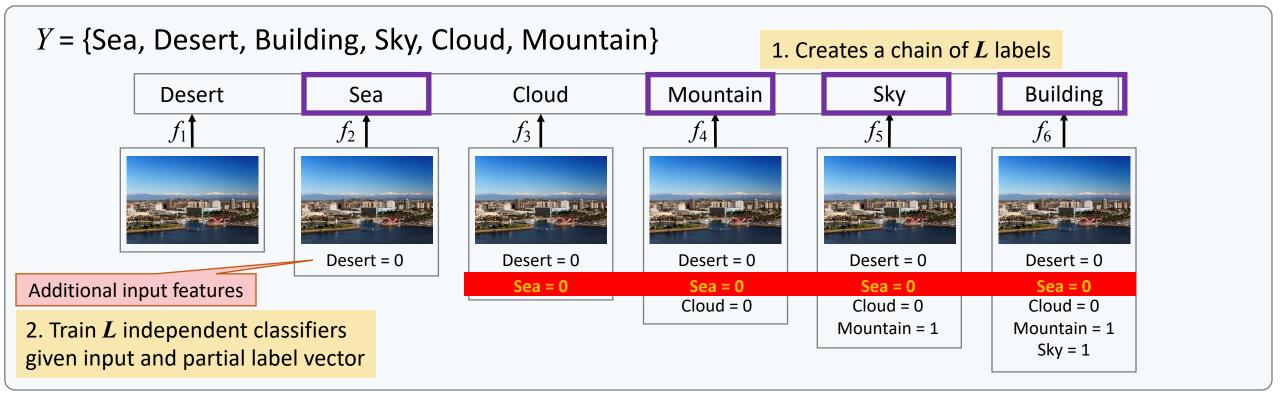
- Error-propagation at test time
- Effect of label orders in the chain

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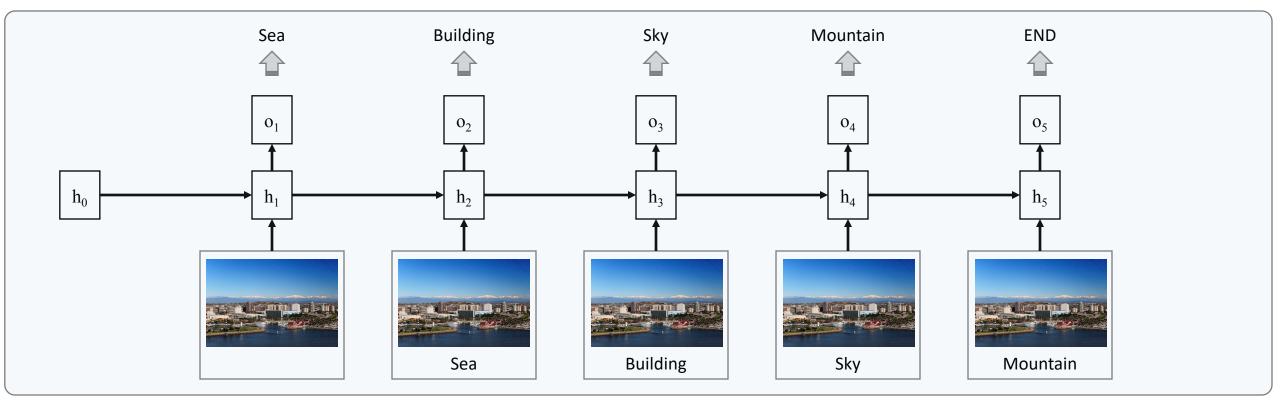
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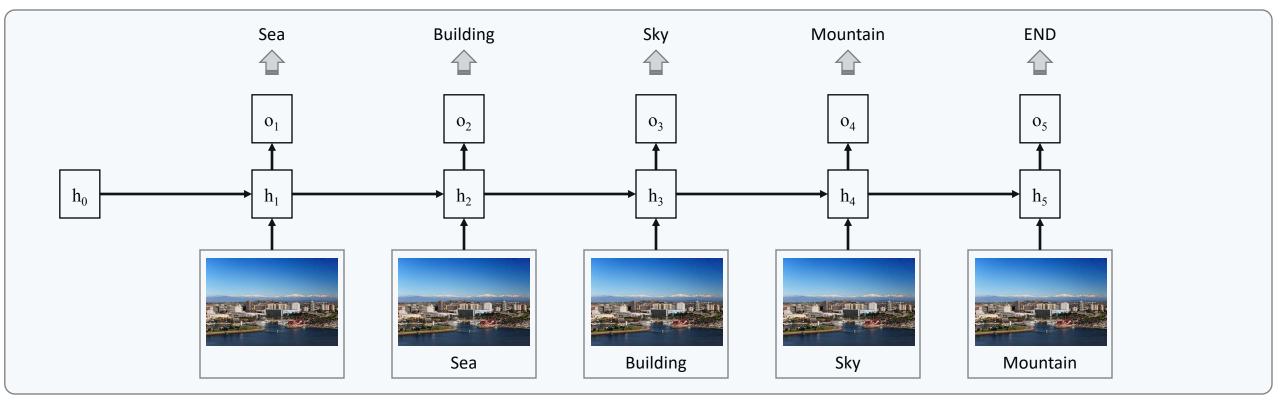
#### **Recurrent Neural Networks for MLC**

- Learning from a set of relevant labels in a sequential manner (Nam et al., NIPS 2017)
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 Question: The effect of label permutation remain! How to determine the target label permutation?

# Target label permutations for RNN training

- Static label permutation for *all* instances
  - Arbitrary label sequence randomly chosen at the beginning
  - Label frequency distribution: *freq2rare*, *rare2freq*
  - Label structures (e.g., pairwise label dependencies)
- → *Suboptimal* choice; learn from only one permutation

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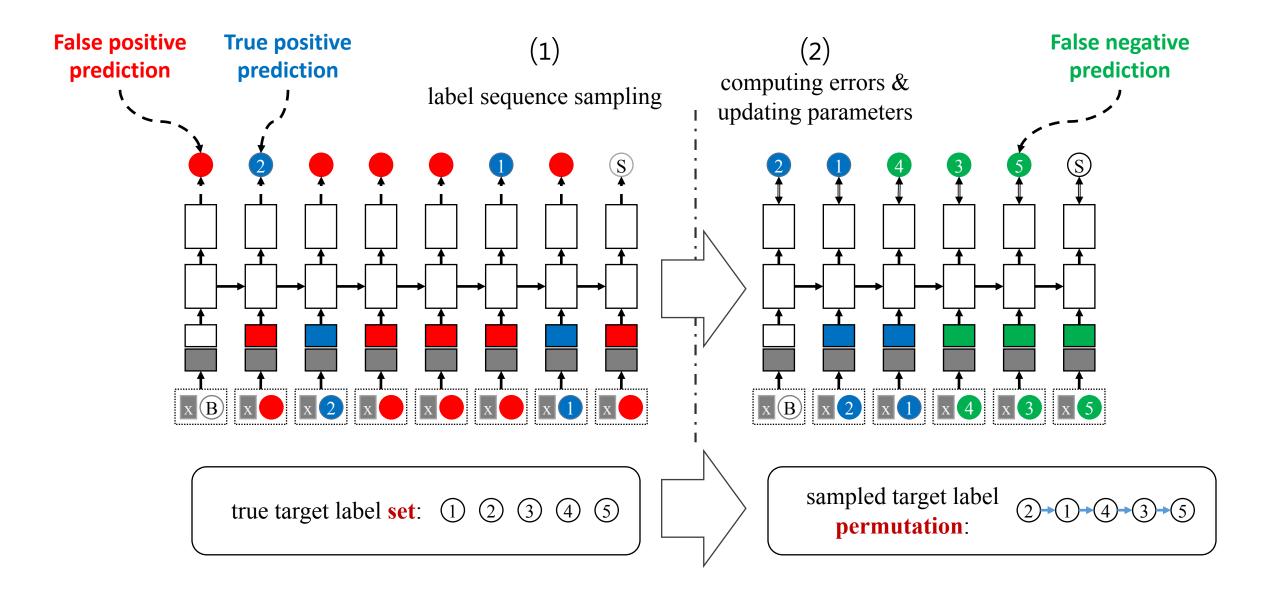
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- Different label permutations for *individual* instances
  - Choosing randomly every time
  - Learning from all possible label permutations
- → More robust to the effect of label permutation; *Computational complexity*

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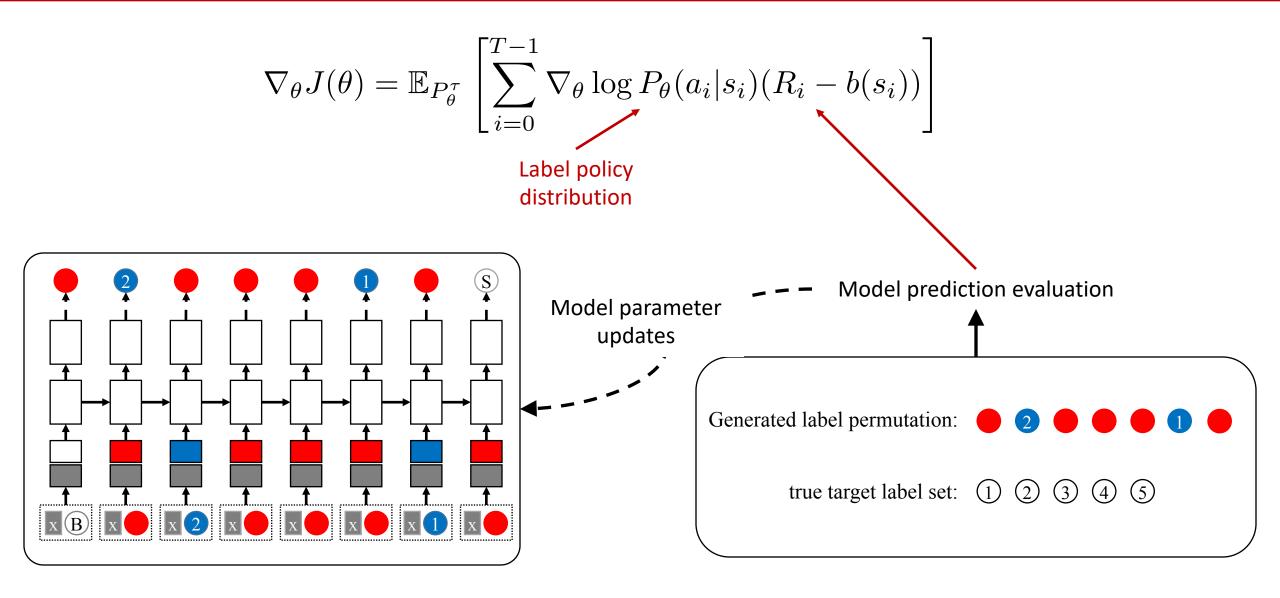
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We need MLC algorithms that learn context-dependent label permutations *efficiently*!

#### Model based label permutation

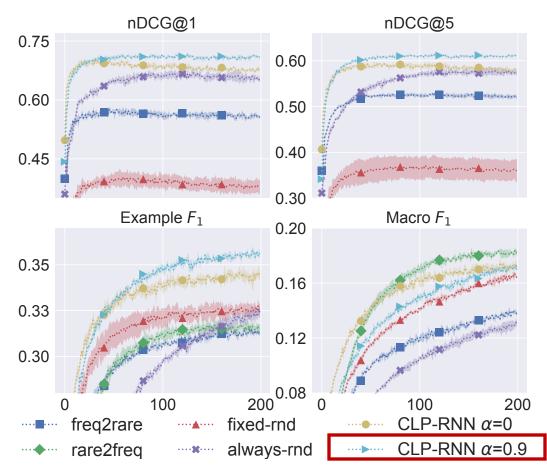


#### Policy gradient



#### Experiments

• We combined two approaches! Context-dependent label permutation learning clearly outperforms static label permutation approaches



	Methods	Example $F_1$	Macro $F_1$	Prec@1	Prec@3	Prec@5
Mediamill	SLEEC	-	-	87.82	73.45	59.17
	FastXML	-	-	84.22	67.33	53.04
	Parabel	-	-	83.91	67.12	52.99
	freq2rare	$66.63 \pm 0.33$	$39.68 {\pm} 0.69$	$90.05{\scriptstyle\pm0.31}$	$74.20{\scriptstyle\pm0.18}$	$58.39 {\pm} 0.29$
	rare2freq	$66.95 {\pm} 0.26$	$43.33 {\pm} 0.62$	$53.67 {\pm} 1.31$	$59.57 {\pm} 0.78$	$52.49 {\pm} 0.37$
	fixed-rnd	$67.21 {\pm} 0.25$	$41.85 {\pm} 0.90$	$73.95 {\pm} 5.20$	$65.58 {\pm} 2.31$	$55.55 {\pm} 0.83$
	always-rnd	$66.25 {\pm} 0.25$	$34.03 {\pm} 0.58$	$89.08 {\pm} 0.18$	$73.90 {\pm} 0.24$	$59.45 {\pm} 0.31$
	CLP-RNN ( $\alpha$ =0)	$67.22 {\pm} 0.15$	$38.75 {\pm} 0.88$	$89.40 {\pm} 0.42$	$73.84 {\pm} 0.30$	$59.29 {\pm} 0.17$
_ C	CLP-RNN ( $\alpha$ =0.6)	$67.27 \pm 0.30$	$36.49 {\pm} 0.74$	$91.27 {\pm} 0.28$	$75.25 \pm 0.32$	$59.75 {\scriptstyle \pm 0.30}$
Delicious	SLEEC	-	-	67.59	61.38	56.56
	FastXML	-	-	69.61	64.12	59.27
	Parabel	-	-	67.44	61.83	56.75
	freq2rare	$31.36 \pm 0.17$	$13.94 {\pm} 0.29$	$57.21 {\pm} 0.38$	$54.28 {\pm} 0.31$	$51.16 {\pm} 0.36$
	rare2freq	$31.60 {\pm} 0.15$	$18.00 \pm 0.31$	$17.46 {\pm} 0.38$	$18.49 {\pm} 0.51$	$20.31 {\pm} 0.72$
	fixed-rnd	$32.74 {\pm} 0.27$	$16.48 {\pm} 0.31$	$40.59 {\pm} 1.31$	$37.21 {\pm} 3.06$	$35.74 {\pm} 2.60$
	always-rnd	$32.45 {\pm} 0.05$	$13.00 {\pm} 0.25$	$66.58 {\pm} 0.90$	$60.46 {\pm} 0.54$	$54.95 {\pm} 0.55$
	CLP-RNN ( $\alpha$ =0)	$34.43 {\pm} 0.54$	$17.33 {\pm} 0.17$	$69.57 {\pm} 0.43$	$61.57 {\pm} 0.69$	$55.73 {\pm} 0.56$
– C	CLP-RNN ( $\alpha$ =0.9)	$35.80 {\scriptstyle \pm 0.35}$	$18.00{\scriptstyle \pm 0.51}$	$70.54 \pm 0.77$	$63.39 {\scriptstyle \pm 0.65}$	$57.72 {\scriptstyle \pm 0.58}$

Poster #233