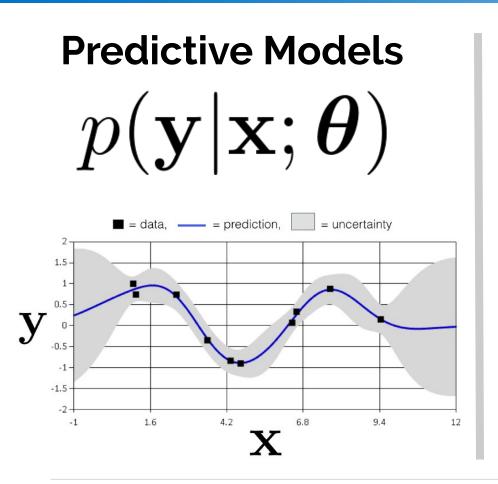
Hybrid Models with Deep and Invertible Features

Eric Nalisnick*, Akihiro Matsukawa*, Yee Whye Teh, Dilan Gorur, Balaji Lakshminarayanan

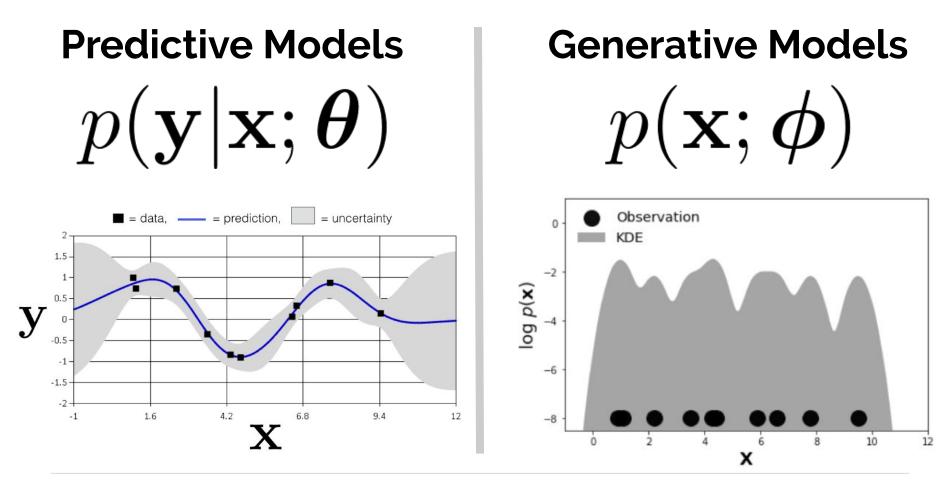


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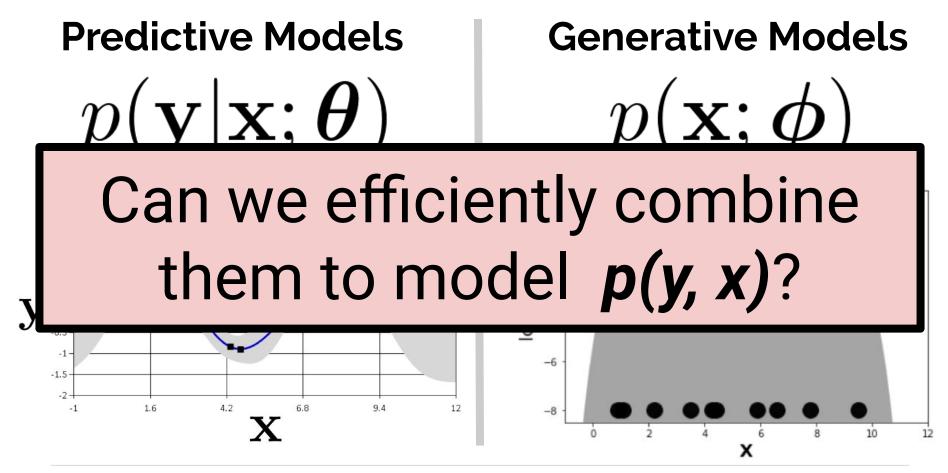
*equal contribution





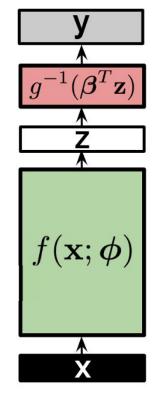


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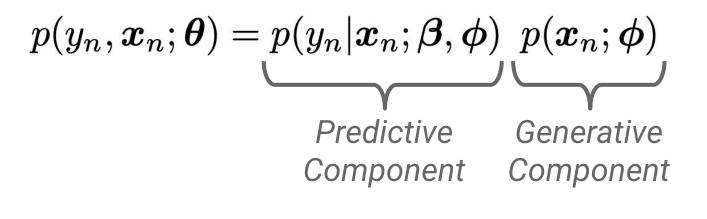
We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).

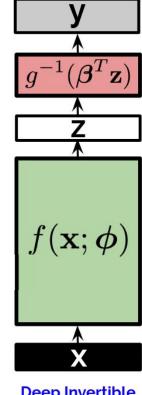


Deep Invertible Generalized Linear Model (DIGLM)



We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).



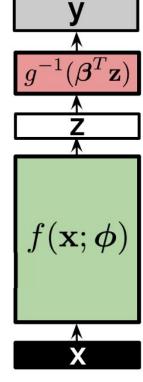


Deep Invertible Generalized Linear Model (DIGLM)



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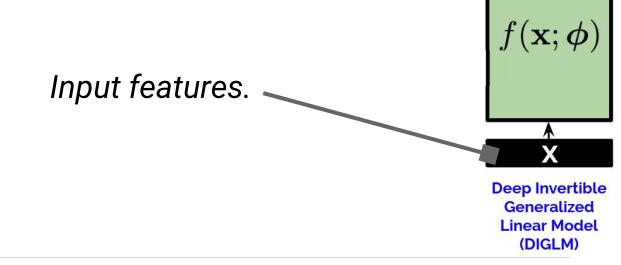
$$p(y_n, \boldsymbol{x}_n; \boldsymbol{\theta}) = p(y_n | \boldsymbol{x}_n; \boldsymbol{\beta}, \boldsymbol{\phi}) \quad p(\boldsymbol{x}_n; \boldsymbol{\phi})$$
$$= \begin{bmatrix} p(y_n | f(\boldsymbol{x}_n; \boldsymbol{\phi}); \boldsymbol{\beta}) & p_z(f(\boldsymbol{x}_n; \boldsymbol{\phi})) & \frac{\partial f_{\boldsymbol{\phi}}}{\partial \boldsymbol{x}_n} \end{bmatrix}$$
Linear Model Normalizing Flow



Deep Invertible Generalized Linear Model (DIGLM)



We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).





We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).

Normalizing flow acts as a deep neural feature extractor.

Deep Invertible Generalized Linear Model (DIGLM)



We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).

> Flow's output and params. are used to compute **p(x)** via change-of-variables.

Deep Invertible Generalized Linear Model (DIGLM)



We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).

Flow's output is used as the feature vector in a (generalized) linear model, which computes **p(y|x)**.

Deep Invertible Generalized Linear Model (DIGLM)

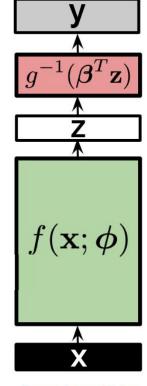


We define a computationally efficient **hybrid model** by combining *normalizing flows* with *generalized linear models* (GLMs).

Optimization objective:

Weight to trade-off predictive and generative performance.

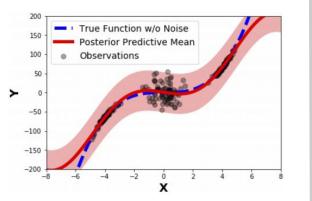
$$\mathcal{J}_{\lambda}(oldsymbol{ heta}) = \sum_{n=1}^{N} \Bigl(\log p(y_n | oldsymbol{x}_n; oldsymbol{eta}, oldsymbol{\phi}) + \lambda \log p(oldsymbol{x}_n; oldsymbol{\phi}) \Bigr)$$



Deep Invertible Generalized Linear Model (DIGLM)



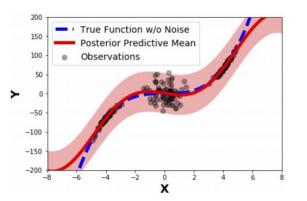
Simulation: Heteroscedastic Regression



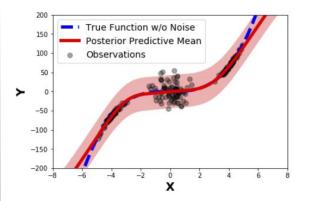
Gaussian process fitted to simulated data.

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Simulation: Heteroscedastic Regression



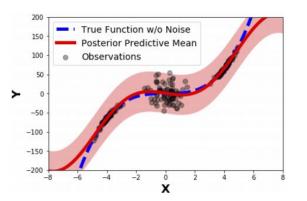
Gaussian process fitted to simulated data.



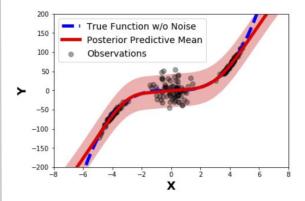
Our model's predictive component.

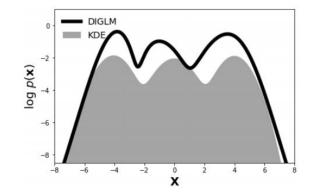


Simulation: Heteroscedastic Regression



Gaussian process fitted to simulated data.





Our model's predictive component.

Our model's generative component.



For more details, please visit our poster.

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