# Composing Entropic Policies using Divergence Correction

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# **Compositional Policies**

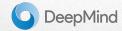






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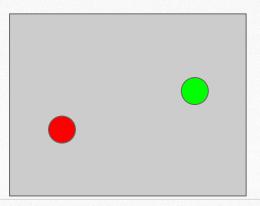
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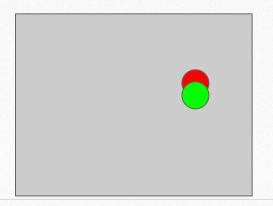


### Problem

Training tasks:  $r_1, r_2$ 

Transfer task:  $r_b = r_1 + r_2$ 





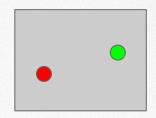




#### **Prior Work**

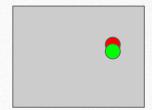
Generalized Policy Improvement (Barreto et al., 2017)

$$\left\{\pi_1,\pi_2,\ldots\right\} \qquad \qquad Q_b^{GPI}(s,a) = \max_i Q_b^{\pi_i}(s,a)$$



Compositional Optimism (Haarnoja et al., 2018) with Maximum Entropy RL

$$Q_b^{CO}(s,a) = Q^{\pi_1}(s,a) + Q^{\pi_2}(s,a)$$



# Maximum Entropy Generalized Policy Improvement

#### 1. Successor Features

$$\phi = (r_1, r_2)$$
  $\psi^{\pi}(s, a) = \mathop{\mathbb{E}}_{\pi} \left[ \sum_i \phi_i \right]$ 

$$Q_b^{\pi}(s, a) = \psi^{\pi}(s, a) \cdot (b, 1 - b)$$

2. Generalized Policy Improvement

$$Q_b^{GPI}(s, a) = \max_i Q_b^{\pi_i}(s, a)$$

$$\pi(a|s) \propto \exp(Q_b^{GPI}(s,a))$$

## **Divergence Correction**

Track the discounted, expected Rényi divergence between policies.

$$Q_b^{DC}(s,a) = Q^{\pi_1}(s,a) + Q^{\pi_2}(s,a) - C(s,a)$$

This information allows to recover the optimal compositional policy.

$$Q_b^{DC} = Q_b^*$$

# $r_1 = 1$ $r_2 = 1$

### Results

