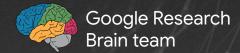
# Statistics and Samples in Distributional Reinforcement Learning

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**ICML 2019** 





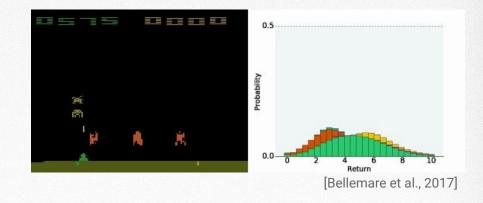
Distributional RL aims to learn full return distributions.

Return distribution:

$$Z^{\pi}(x,a) = \sum_{t=0}^{\infty} \gamma^t R_t \mid X_0 = x, A_0 = a$$

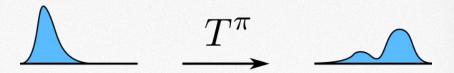
Distributional Bellman equation:

$$Z^{\pi} \stackrel{\mathcal{D}}{=} T^{\pi} Z^{\pi}$$



In practice, we often work with parametric approximate distributions.

Non-parametric



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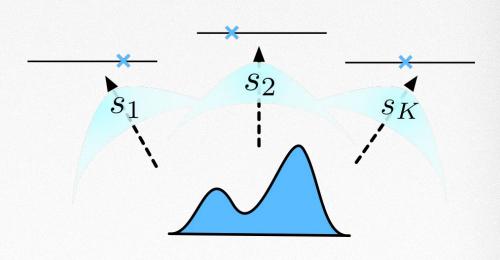
Non-parametric  $T^{\pi}$  Categorical [Bellemare et al., 2017]  $\widetilde{T}^{\pi}$ 

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#### Main Contribution: An Alternative Perspective

Distributional RL algorithms learn statistical functionals of the return distribution.

 Moments, tail probabilities, expectations, etc.



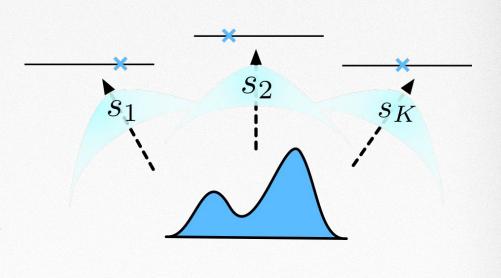
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 Moments, tail probabilities, expectations, etc.

**Theory:** What properties of return distributions can be learnt through dynamic programming?

**Algorithmic:** A general framework for approximate learning of statistics.





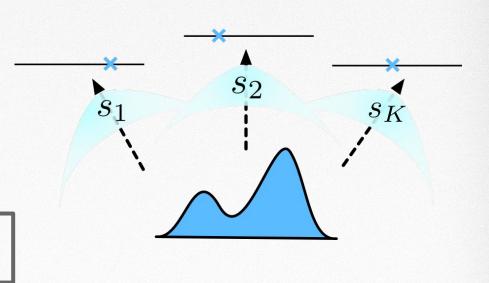
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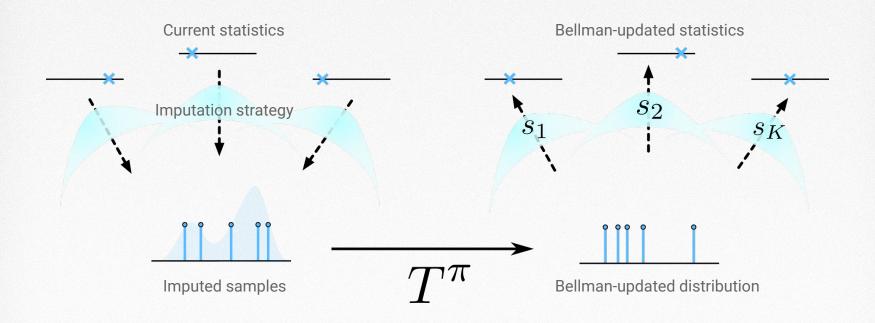
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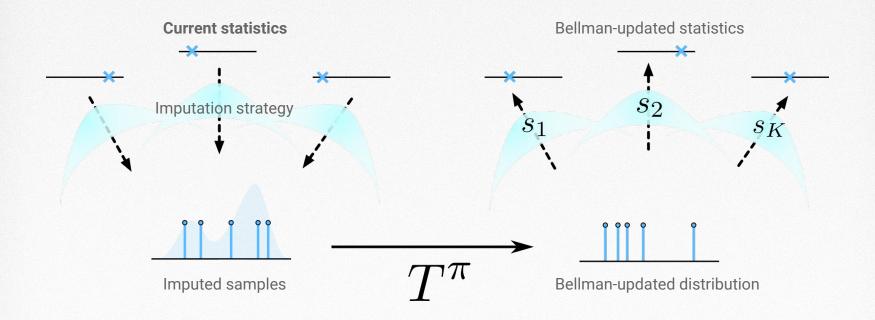
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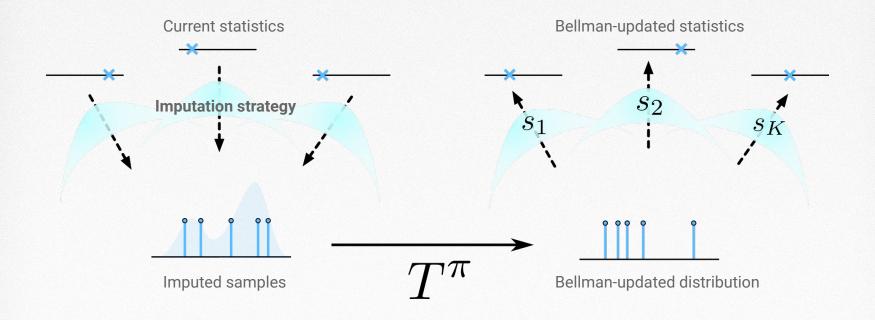




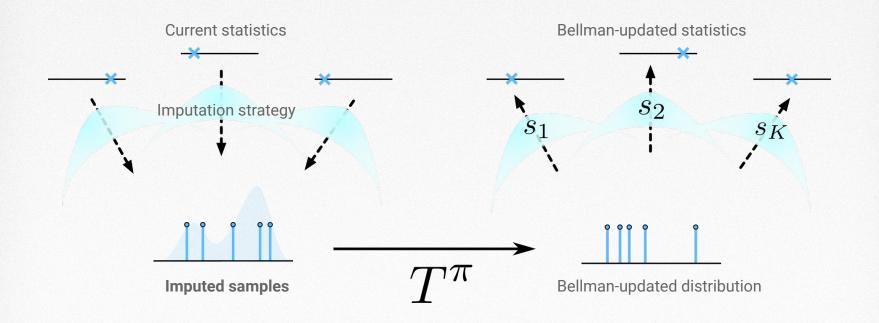




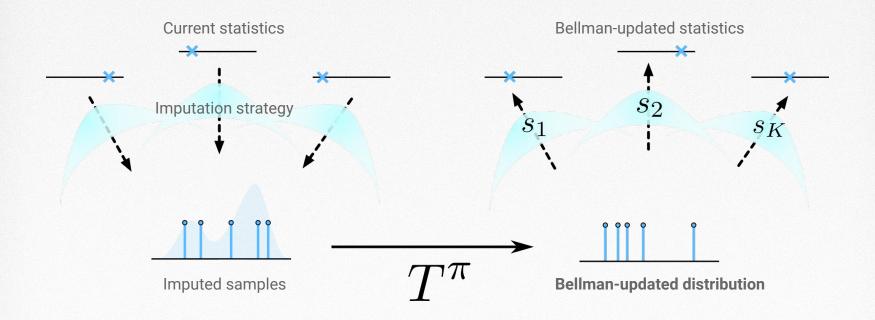




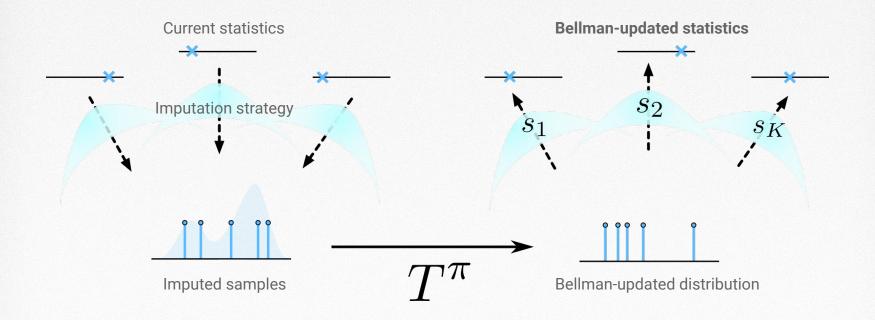










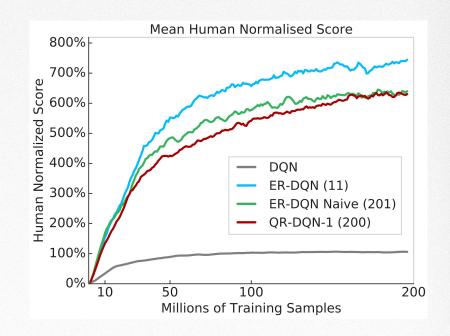




#### Application: Expectiles

We apply this framework to learn **expectiles** of return distributions.

New deep RL agent: Expectile Regression DQN (ER-DQN), with improved mean performance on Atari-57 relative to QR-DQN.





## Summary

A new perspective on distributional RL

Theoretical progress on what it is possible to learn



