

# Learning to Route in Similarity Graphs

**Dmitry Baranchuk**

joint work with Dmitry Persiyanov, Anton Sinitsin and Artem Babenko



# Overview

The Budgeted Nearest Neighbor Search Problem

Similarity Graphs

Learning to Route in Similarity Graphs

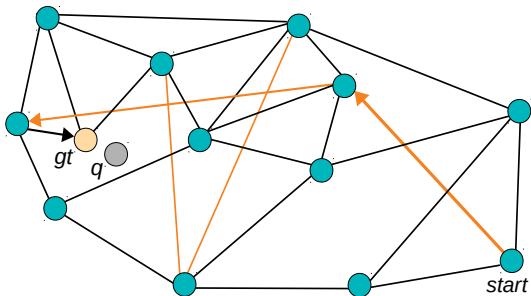
Evaluation

# The Budgeted Nearest Neighbor Search Problem

- $\{x_1, \dots, x_N\} \subset \mathbb{R}^D$  — search database
- $q \in \mathbb{R}^D$  — query
- *DCS* — maximal number of distance computations
- *Recall@1* — a rate of queries for which the actual nearest neighbor is successfully found

# Similarity Graphs

- **Vertices** correspond to the database items
- **Edges** connect (mostly) nearest neighbors



- Several state-of-the-art methods exist e.g. HNSW<sup>1</sup>, NSG<sup>2</sup>

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<sup>1</sup>Malkov, Y., Yashunin, D. Efficient and robust approximate nearest neighbor search using hierarchical navigable small world graphs. TPAMI 2018

<sup>2</sup>Cong Fu, Chao Xiang, Changxu Wang, and Deng Cai. Fast approximate nearest neighbor search with the navigating spreading-out graph. PVLDB 2019

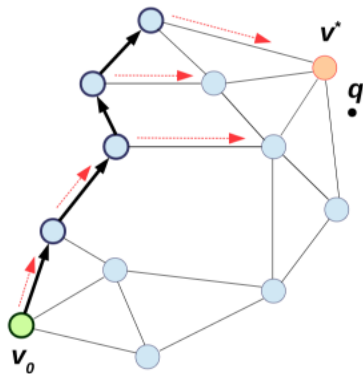
# Routing Algorithms

- **Greedy routing:** Pick the best neighbor of the current vertex
- **Beam search:** Expand the most promising vertex in the candidate pool
- **Our method:** Learn a routing algorithm directly from data



# Learning to Route in Similarity Graphs

1. **Imitation Learning:** Train the agent to imitate expert decisions
2. **Agent** is a beam search based on learned vertex representations
3. **Expert** encourages the agent to follow a shortest path to the actual nearest neighbor  $v^*$

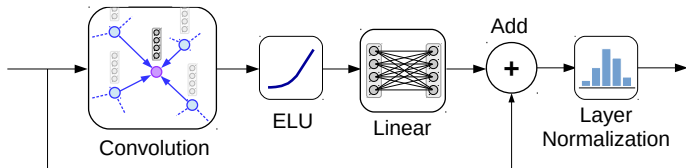


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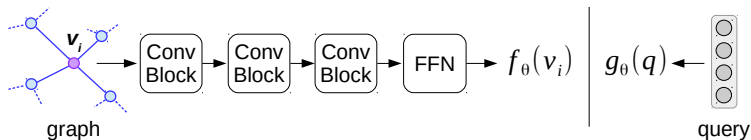
Ross, S., Gordon, G. J., and Bagnell, D. A reduction of imitation learning and structured prediction to no-regret online learning. AISTATS 2011

## Model Architecture

**Graph Convolutional Network** learns representations for vertices that account for the underlying structure of the similarity graph



### Graph Convolutional Block



Kipf, T. N. and Welling, M. Semi-supervised classification with graph convolutional networks. ICLR 2017

# Evaluation

- Datasets with  $10^5$  points
- No additional cost in run-time
- PyTorch implementation<sup>3</sup>

DCS budget	Vertex Representations	SIFT100K	DEEP100K	GloVe100K
		<i>Recall@1</i>	<i>Recall@1</i>	<i>Recall@1</i>
128	Original	0.239	0.386	0.198
	Learned	<b>0.371</b>	<b>0.474</b>	<b>0.305</b>
256	Original	0.672	0.795	0.400
	Learned	<b>0.799</b>	<b>0.811</b>	<b>0.526</b>
512	Original	0.936	0.940	0.582
	Learned	<b>0.949</b>	<b>0.945</b>	<b>0.676</b>

Search performance *Recall@1* for distance computation (DCS) budgets

<sup>3</sup><https://github.com/dbaranchuk/learning-to-route>