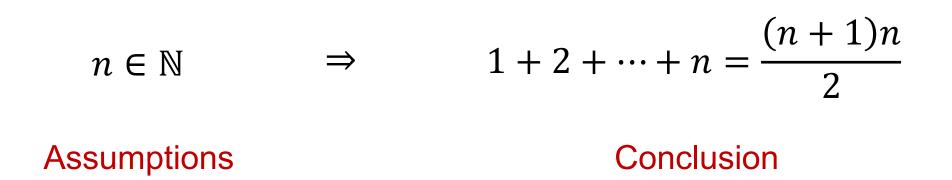
Learning to Prove Theorems via Interacting with Proof Assistants

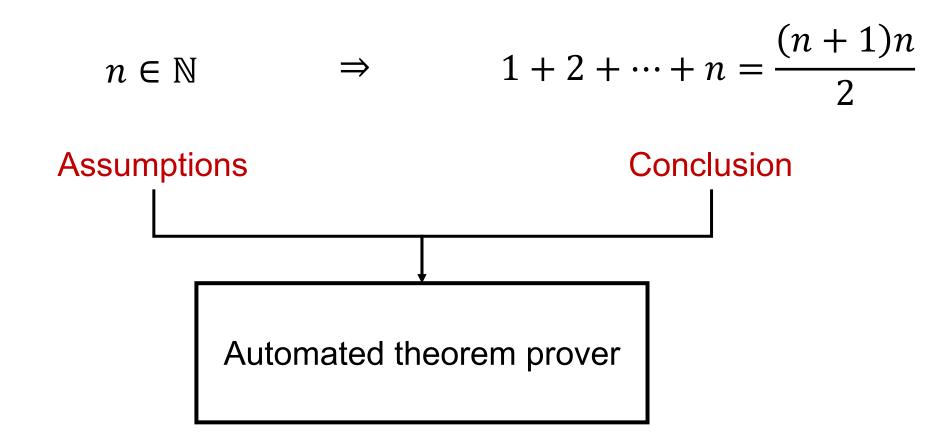
Kaiyu Yang, Jia Deng



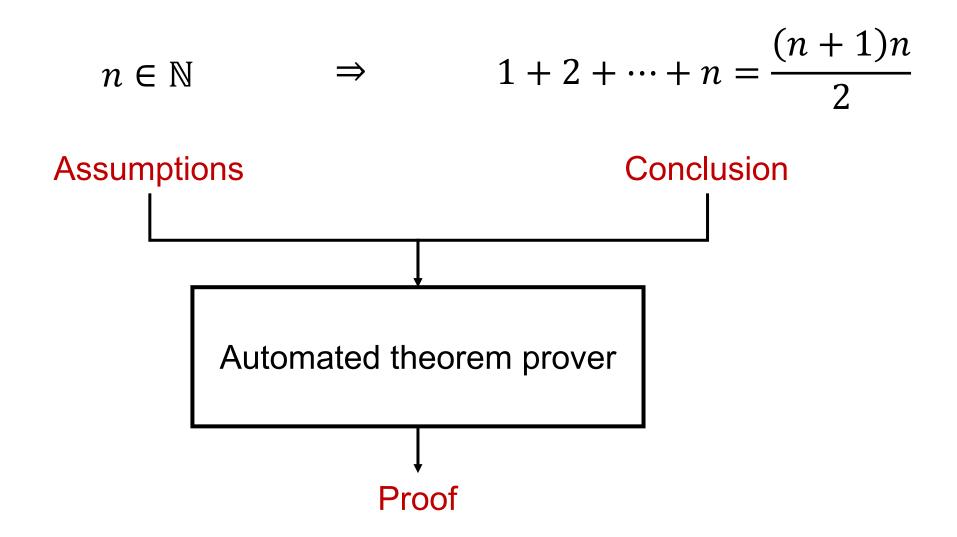
Automated Theorem Proving (ATP)

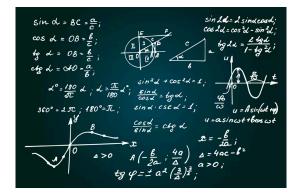


Automated Theorem Proving (ATP)

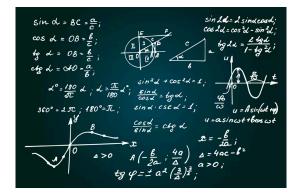


Automated Theorem Proving (ATP)





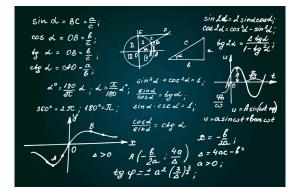
Computer-aided proofs in math



Computer-aided proofs in math



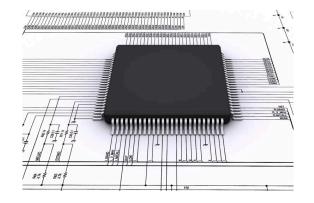
Software verification



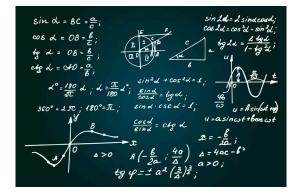
Computer-aided proofs in math



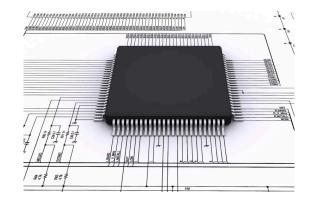
Software verification



Hardware design



Computer-aided proofs in math



Hardware design



Software verification



Cyber-physical systems

• Prove by resolution

Theorem

Prove by resolution

$$1 + 2 + \dots + n = \frac{(n+1)n}{2}$$

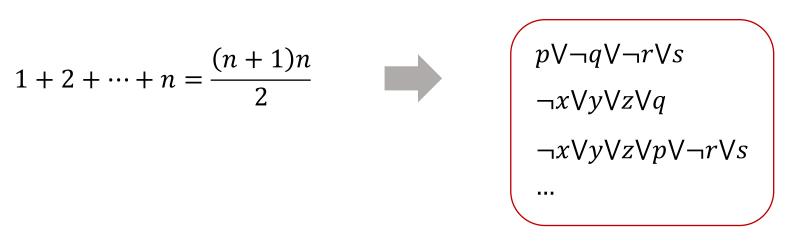
$$p \lor \neg q \lor \neg r \lor s$$

$$\neg x \lor y \lor z \lor q$$

$$\neg x \lor y \lor z \lor p \lor \neg r \lor s$$

Theorem

• Prove by resolution



Theorem

- The CNF representation
 - Long and incomprehensible even for simple math equations
 - Unsuitable for human-like high-level reasoning

$$1 + 2 + \dots + n = \frac{(n+1)n}{2}$$

$$p \lor \neg q \lor \neg r \lor s$$

$$\neg x \lor y \lor z \lor q$$

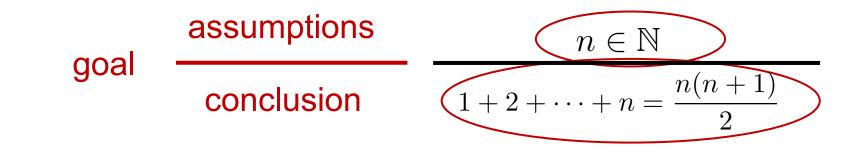
$$\neg x \lor y \lor z \lor p \lor \neg r \lor s$$

$$\dots$$

Theorem

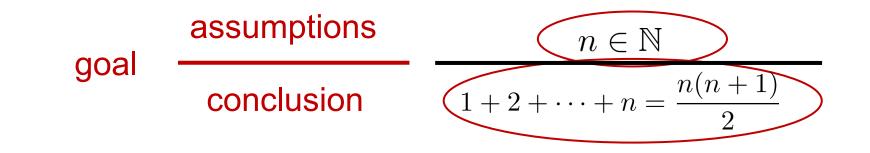


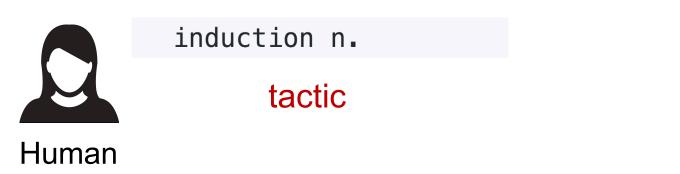




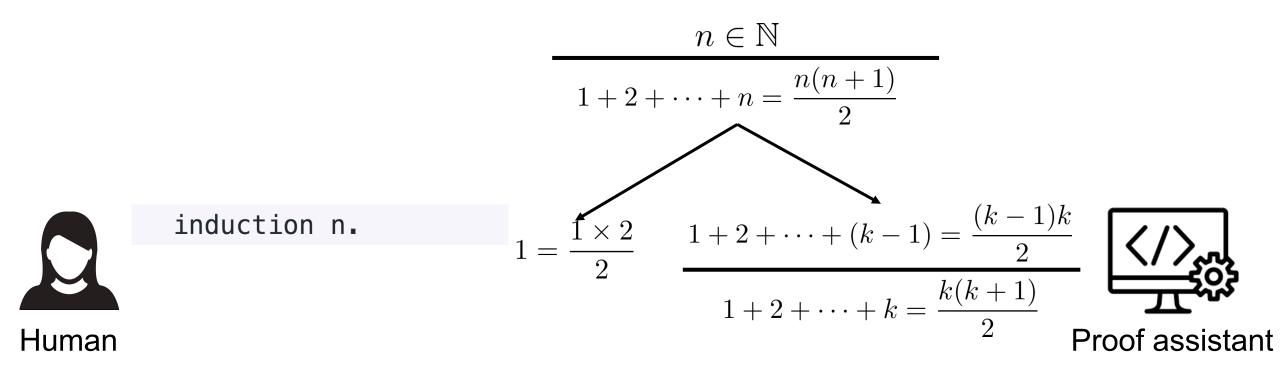


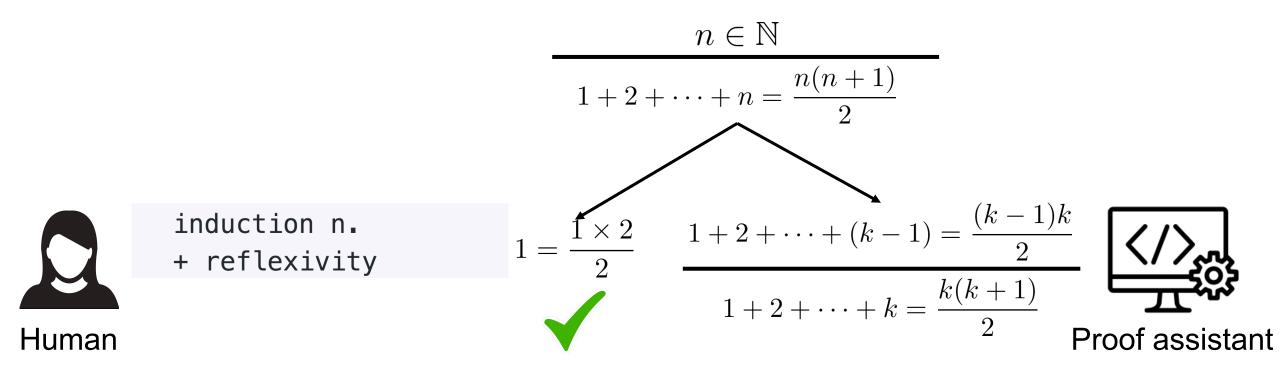


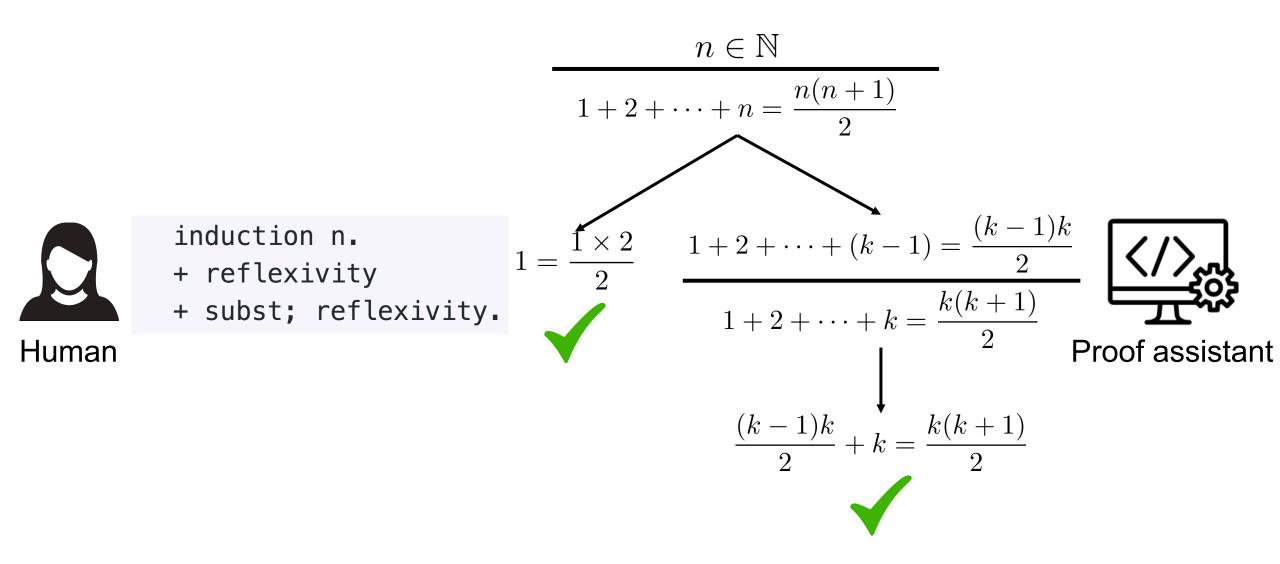


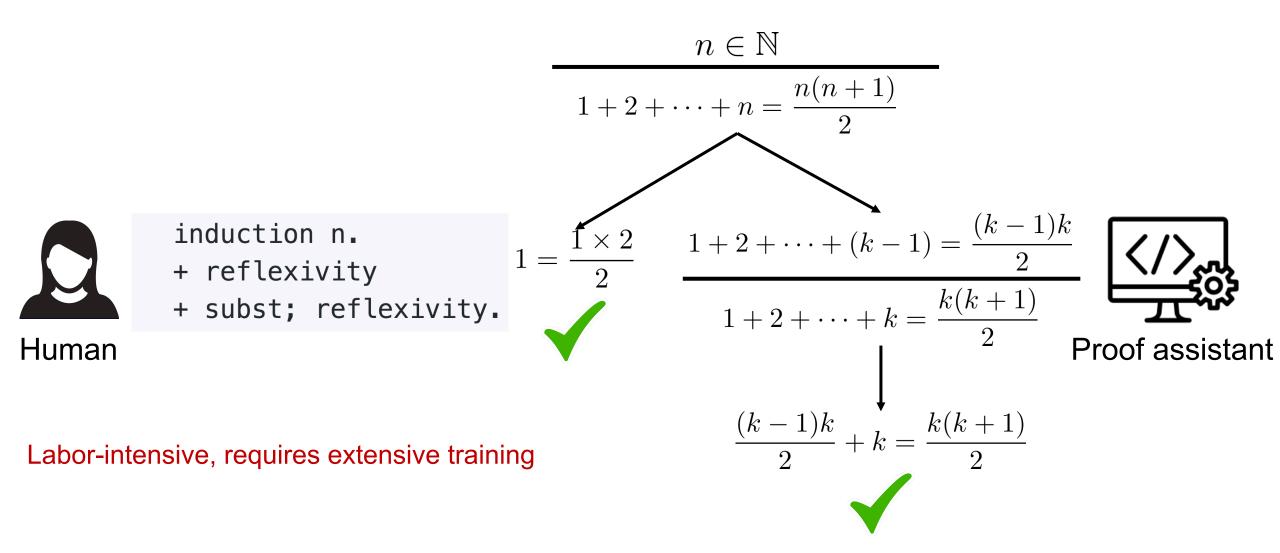


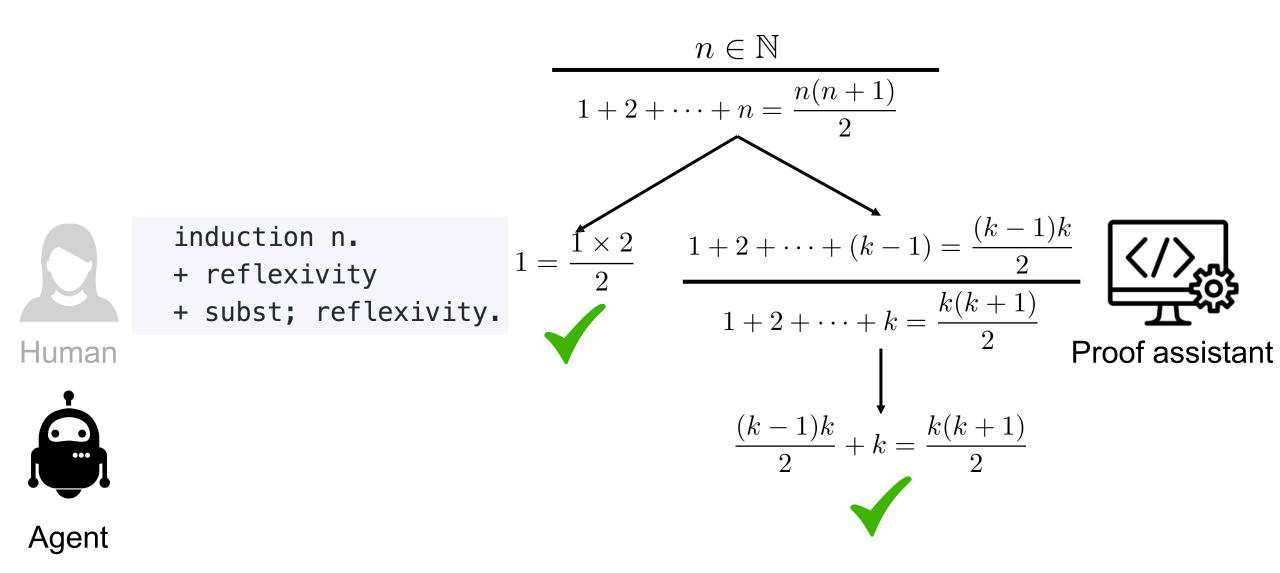










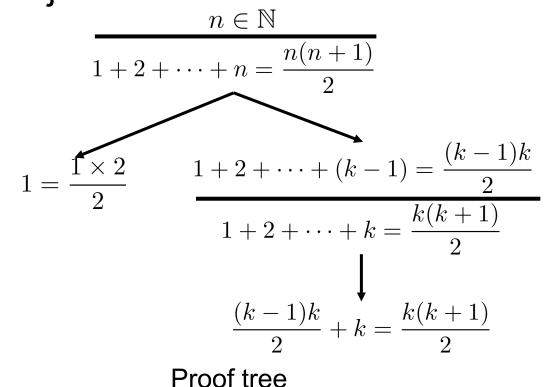


CoqGym: Dataset and Learning Environment

- Tool for interacting with the Coq proof assistant [Barras et al. 1997]
- 71K human-written proofs, 123 Coq projects
- Diverse domains
 - math, software, hardware, etc.

CoqGym: Dataset and Learning Environment

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- Structured data
 - Proof trees
 - Abstract syntax trees



ASTactic: Tactic Generation with Deep Learning

 $n, k \in \mathbb{N}$ n = 2k $n \ge k$

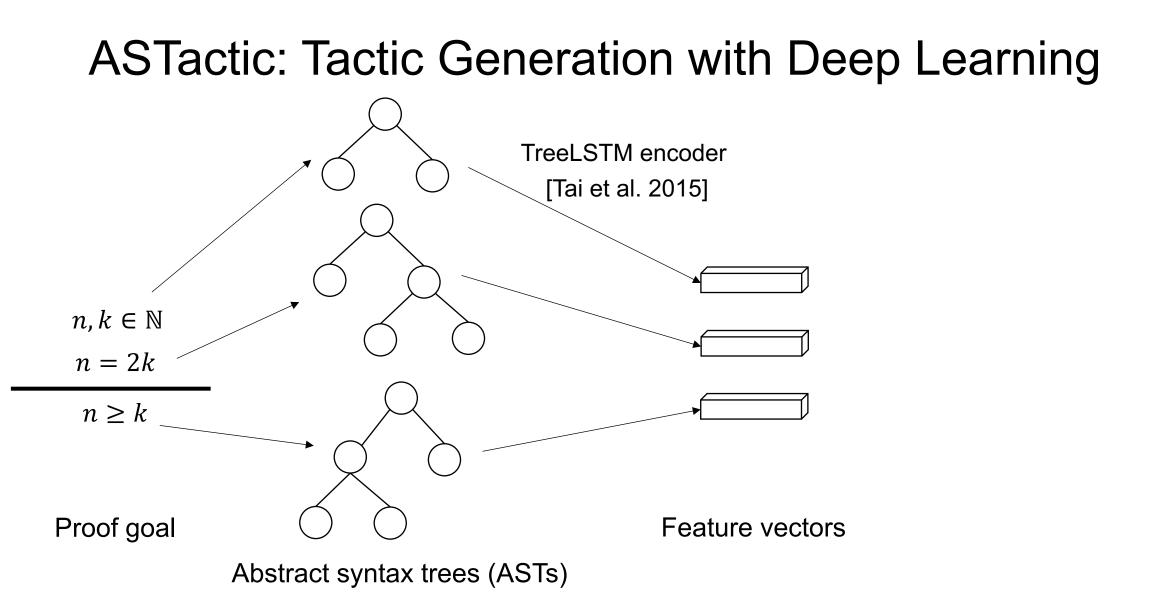
induction n.

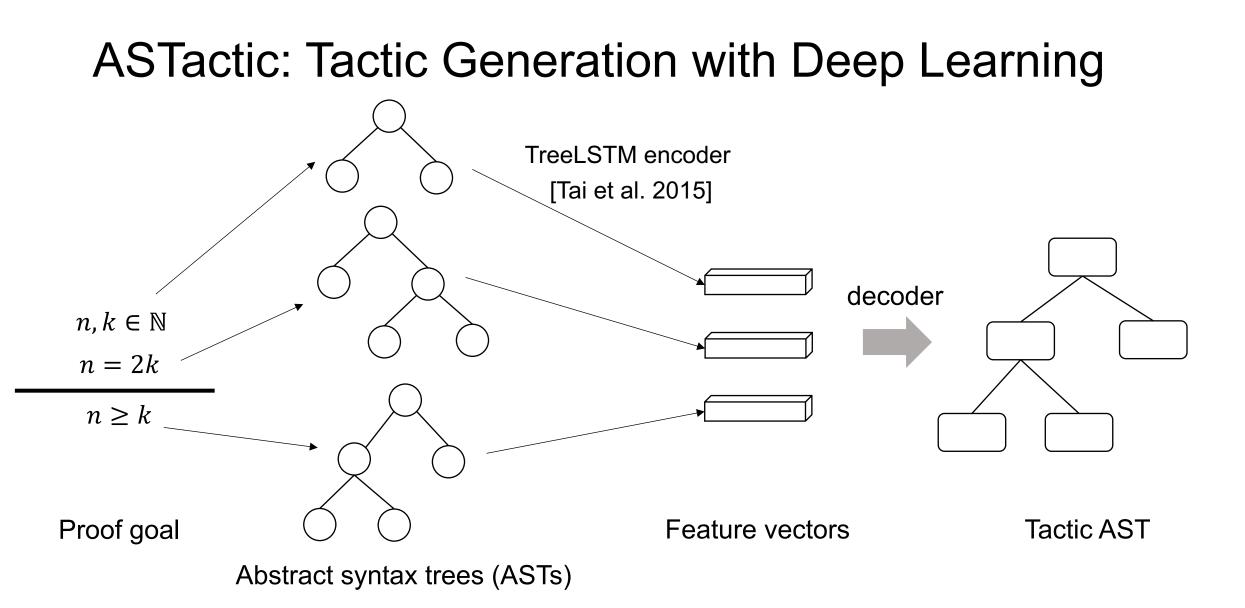
Proof goal

Tactic

ASTactic: Tactic Generation with Deep Learning $n, k \in \mathbb{N}$ n = 2k $n \ge k$ Proof goal

Abstract syntax trees (ASTs)





ASTactic can augment state-of-the-art ATP systems [Czajka and Kaliszyk, 2018] to prove more theorems

Related Work

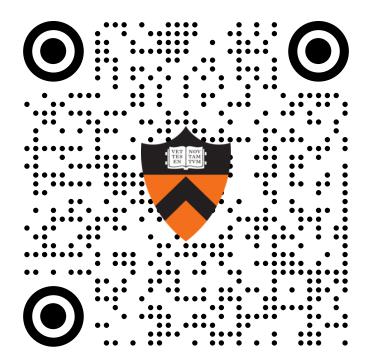
- CoqHammer [Czajka and Kaliszyk, 2018]
- SEPIA [Gransden et al. 2015]
- TacticToe [Gauthier et al. 2018]
- FastSMT [Balunovic et al. 2018]
- GamePad [Huang et al. 2019]
- HOList [Bansal et al. 2019] (concurrent work at ICML19)

Main differences:

- Our dataset is larger covers more diverse domains.
- Our model is more flexible, generating tactics in the form of ASTs.

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Poster today @ Pacific Ballroom #247

Code: https://github.com/princeton-vl/CoqGym