

# Generative Causal Representation Learning for Out-of-Distribution Motion Forecasting

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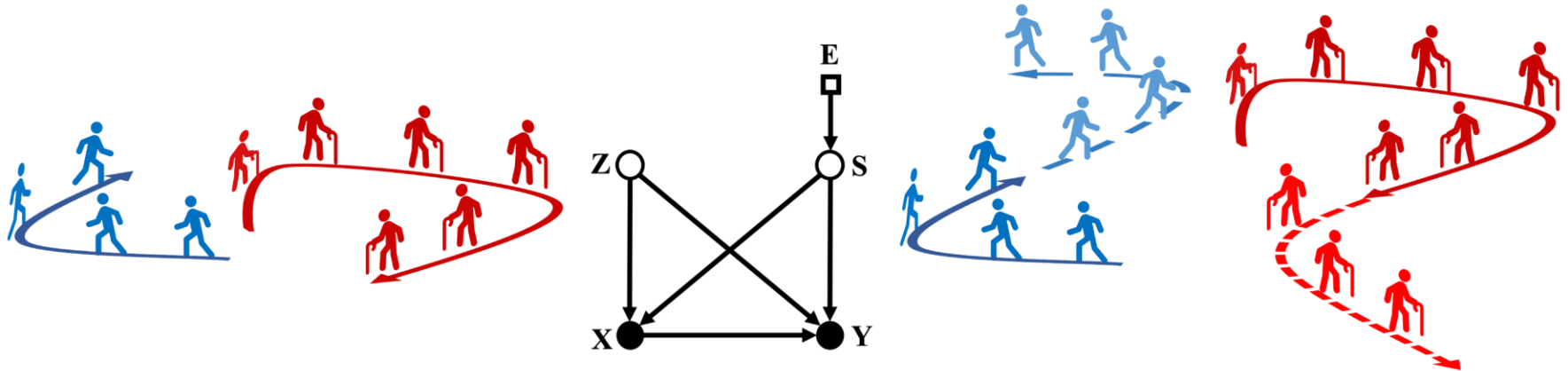
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# Robust Motion Forecasting

- Given past states of  $M$  agents in the scene, we predict the states of each agent in the next timesteps.
- Robustness comes into play when there are multiple domains/distributions in the data. These shifts are due to interventions in the generative/causal factors of the dataset.
- Statistical inference is only valid across environments with identical experimental conditions whereas learning about interventions trains robust models against environmental changes.



# Proposed Causal Model



Past trajectories

Future trajectories

- There are four endogenous variables:  $S$ ,  $Z$ ,  $X$ , and  $Y$  which represent variant features such as motion styles, invariant features such as physical laws, past trajectories, and future trajectories, respectively.
- There is one exogenous variables  $E$  i.e., the selection variable.
- We assume the model is causally sufficient i.e., it can explain the data without adding further causal variables.
- Only  $X$  and  $Y$  i.e., past and future trajectories, are observed.

# Loss Function

- The loss function of GCRL is given as:

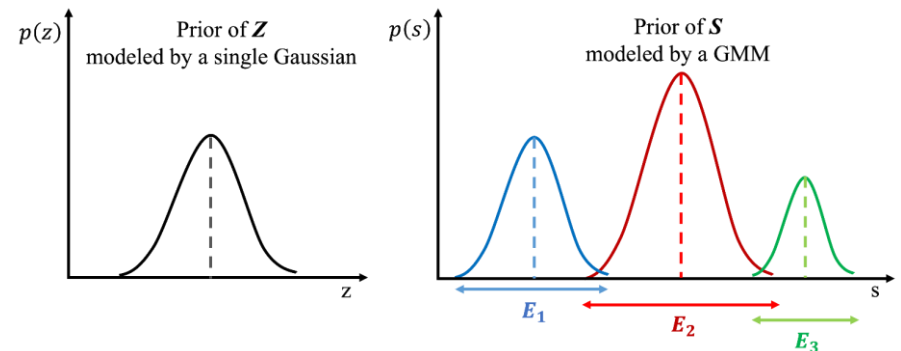
$$\max_{p,q} E_{p^*(x,y)} \left[ \log q(y|x) + \frac{1}{q(y|x)} E_{q(s|x),q(z|x)} \left[ p(y|x, s, z) \log \frac{p(x|s, z)p(s)p(z)}{q(s|x)q(z|x)} \right] \right]$$

- Through this loss function, GCRL learns to:
  1. To minimize the distance between groundtruth future trajectories and predicted future trajectories via maximizing  $\log q(y|x)$
  2. To eliminate the confounding effect by estimating the causal effect of X on Y via  $p(y|do(x))$
  3. To reconstruct past trajectories via maximizing  $\log p(x|s, z)$
  4. Invariant representations via maximizing  $\log \frac{p(z)}{q(z|x)}$
  5. Variant representations via maximizing  $\log \frac{p(s)}{q(s|x)}$
  6. Since GCRL learns to predict the future trajectories with a generative approach, it can tackle the multi-modality of trajectories



# Domain Adaptation

- All representations generated by  $q(z|x)$  will be in the **same range**, whereas the representations of  $q(s|x)$  will form **clusters**, each modeled by a component of the GMM.
- Since  $Z$  is **invariant**, we can **directly transfer** it to the new domain without any fine-tuning.
- However,  $S$  can be interpreted as a **weighted sum of the representations** learnt from different environments of the training domains, which may be used in the test domains as well.
- Depending on how related the test domains are to the training domains, we may need to fine-tune the components of the GMM and obtain a new prior for  $S$ .

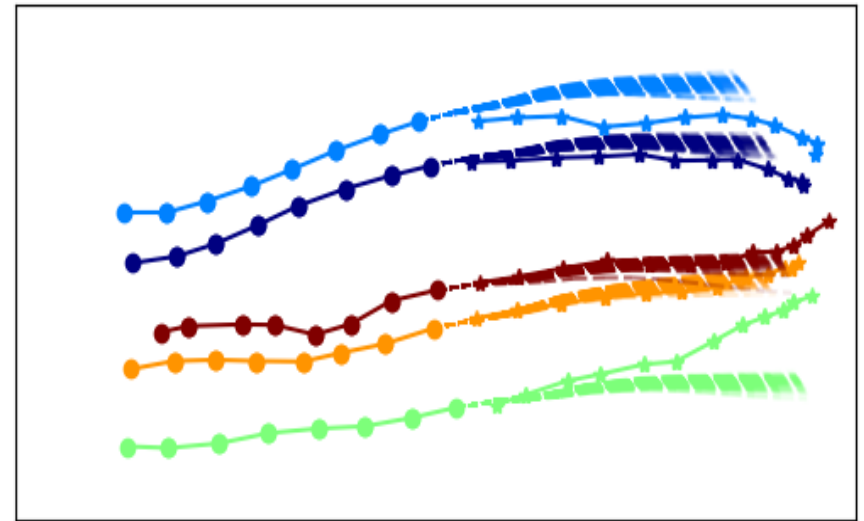
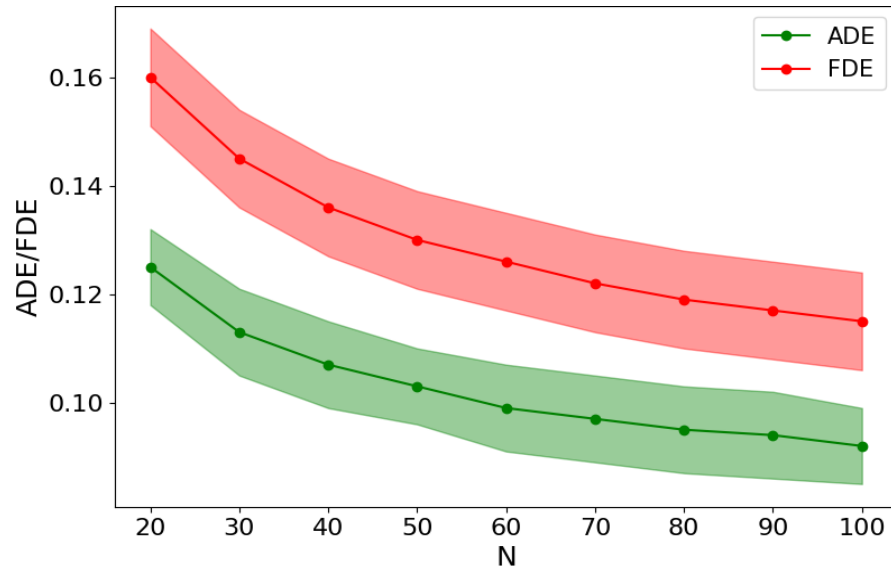


# Robustness of GCRL

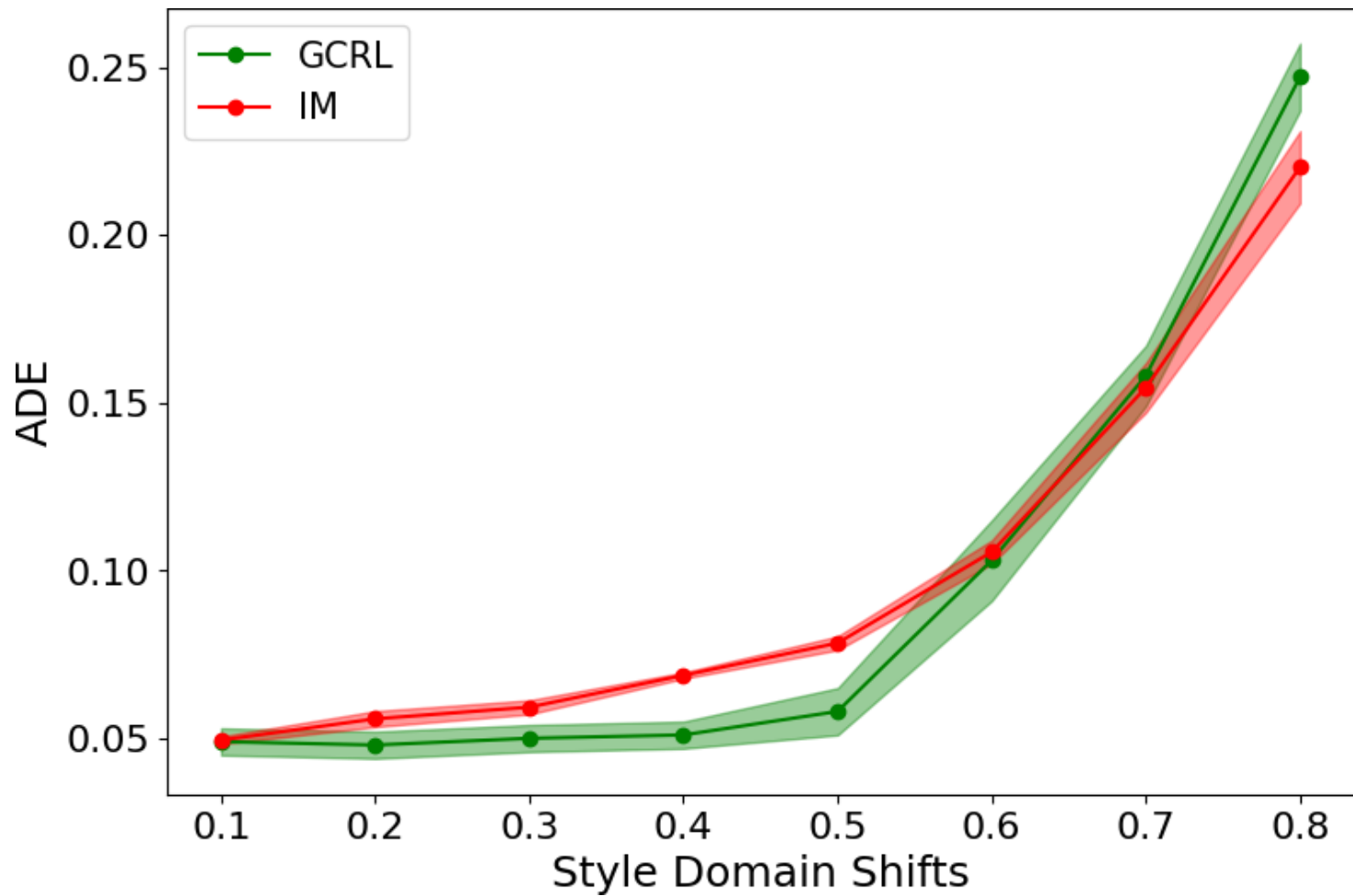
Method	ADE/FDE $\alpha = 8$	ADE/FDE $\alpha = 16$	ADE/FDE $\alpha = 32$	ADE/FDE $\alpha = 64$
Baseline (Huang et al., 2019)	<b>0.80/1.37</b>	2.15/3.80	2.64/4.44	2.68/4.48
Counterfactual (Chen et al., 2021)	0.80/1.59	1.62/2.68	2.32/3.90	2.68/4.52
Invariant $\lambda = 1.0$ (Liu et al., 2022)	0.94/1.65	1.04/1.76	1.52/2.55	1.96/3.35
Invariant $\lambda = 1.0$ (Liu et al., 2022)	0.91/1.67	0.99/1.87	1.18/2.20	1.27/2.33
Invariant $\lambda = 1.0$ (Liu et al., 2022)	0.98/1.79	1.00/1.83	1.06/1.90	1.56/2.58
GCRL (ours)	0.97/1.8	<b>0.97/1.8</b>	<b>0.97/1.8</b>	<b>0.97/1.8</b>



# Multimodal Trajectories in GCRL

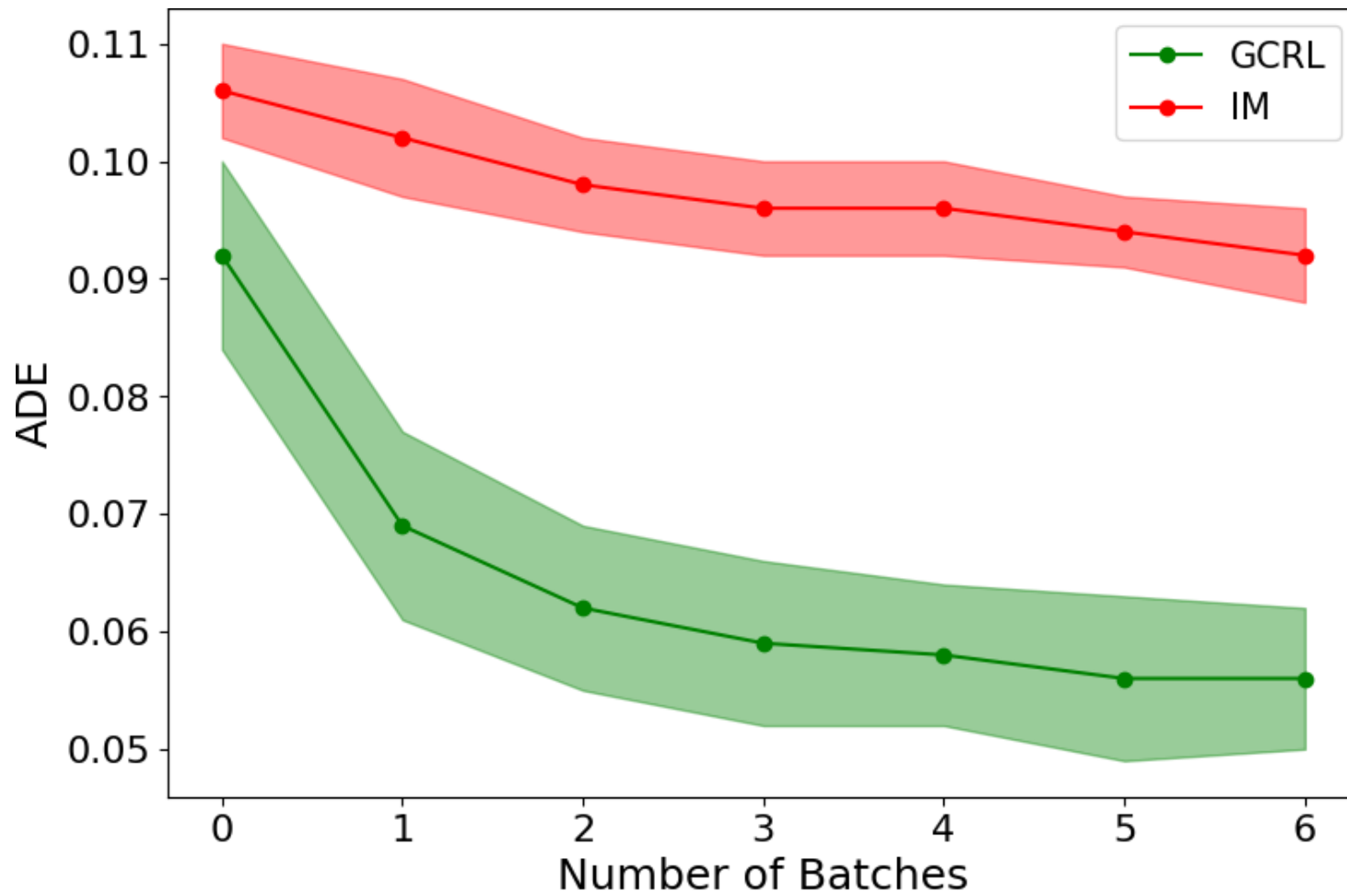


# Domain Generalization





# Domain Adaptation



# Identifiability

Weak MCC of S	Weak MCC of Z	Strong MCC of S	Strong MCC of Z
0.956	0.049	-0.16	-0.025

Method	ADE	FDE
Z Only	0.1054	0.1347
S Only	0.2188	0.2418



# Contact

- You can always reach to me via my email [sshirahm@uwaterloo.ca](mailto:sshirahm@uwaterloo.ca). 😊



# References

1. Huang, Y., Bi, H., Li, Z., Mao, T., and Wang, Z. Stgat: Modeling spatial-temporal interactions for human trajectory prediction. In 2019 IEEE/CVF International Conference on Computer Vision (ICCV), pp. 6271–6280, 2019. doi: 10.1109/ICCV.2019.00637.
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3. Liu, Y., Cadei, R., Schweizer, J., Bahmani, S., and Alahi, A. Towards robust and adaptive motion forecasting: A causal representation perspective. In IEEE/CVF Conference on Computer Vision and Pattern Recognition, CVPR 2022, New Orleans, LA, USA, June 18-24, 2022, pp. 17060–17071. IEEE, 2022. doi: 10.1109/CVPR52688.2022.01657.

