





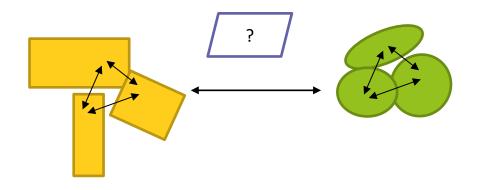
#### Setting & problem statement

- Supervised learning, clustering, retrieval: distances are useful!
- Deformations in the wild: perspective, rotation, translation, ...





Find a distance between images which is **invariant to smooth diffeomorphisms** and **computable in practice.** 

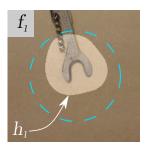


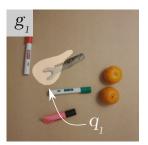
#### **How? Enforce inductive bias.**

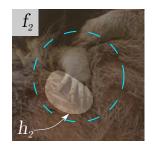
- Labeled data is expensive
- Data augmentation is computationally intensive.



## Applied to our examples

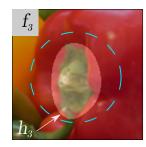


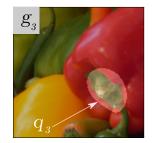






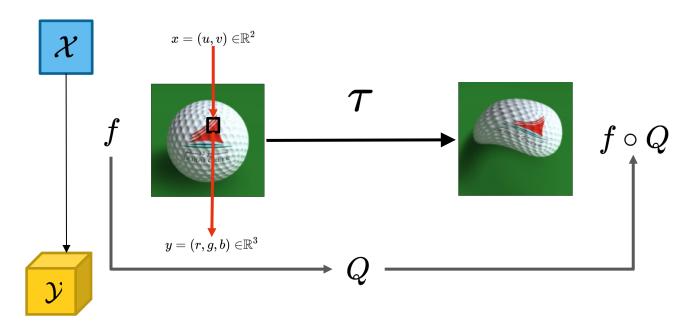








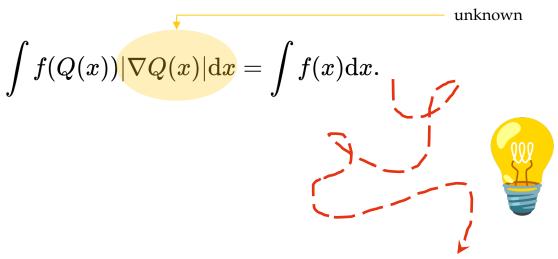
## ▼ Key idea #1: Seeing images as functions







#### **Key idea #2:** change of variable



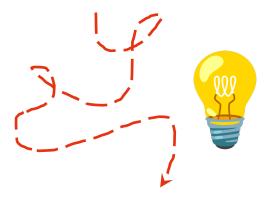
$$D_{\lambda}(f,g) := \max_{\|h\|_{\mathcal{H}} \leq 1} \min_{q \in \mathcal{H}} \max_{\|v\|_{\mathcal{F}} \leq 1} \Big| \int_X v(g(x)) q(x) \mathrm{d}x - \int_X v(f(x)) \mu(x) h(x) \mathrm{d}x \Big|^2 + \lambda \|q\|_{\mathcal{H}}^2$$





#### **Key idea #3:** Nyström approximations

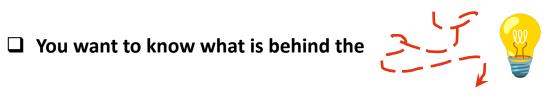
Kernel methods are expressive but expensive when used naïvely!



Efficient time complexity thanks to Nyström approximations.



# Come talk to me **Hall E #517 (6-8pm)**



You work on invariances in ML.

☐ You are interested in kernel methods, Nyström approximations, ...

☐ You like (bad) ML memes...

