

Causal Conceptions of Fairness and their Consequences



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(* equal contribution)

[ACIC 2022 / ICML 2022]

Summary

- Unified taxonomy to understand *causal fairness* research field

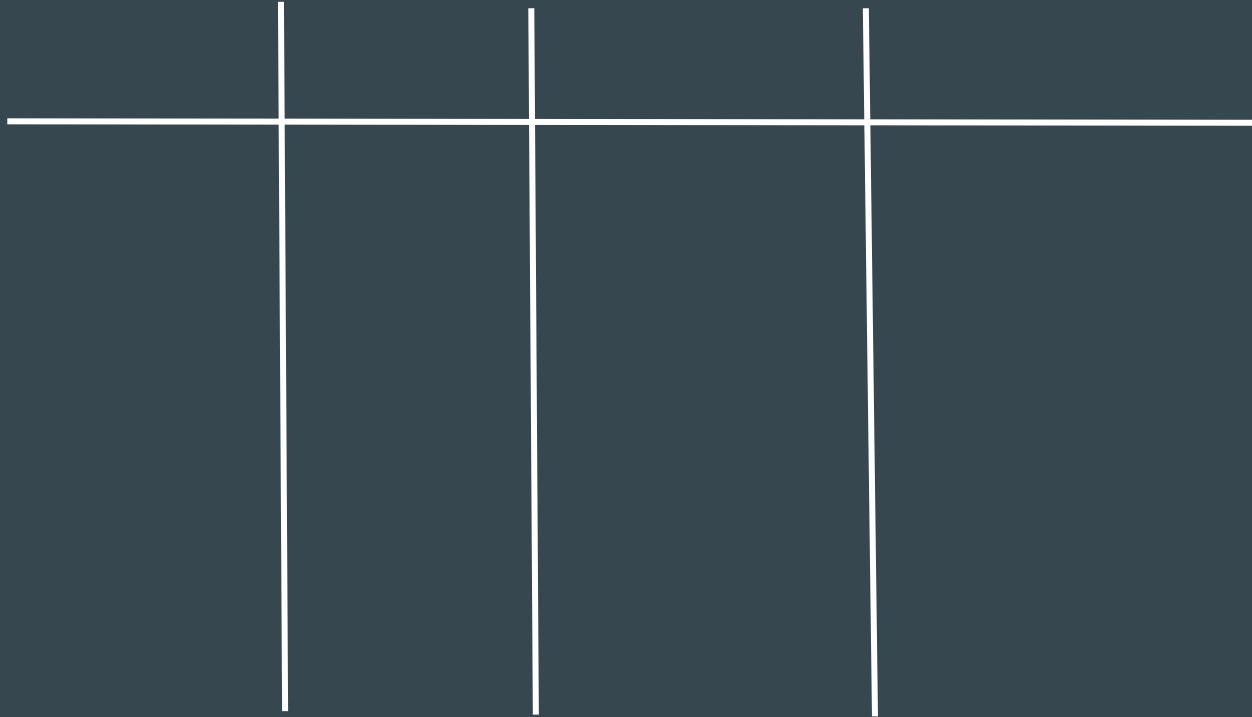
Summary

- Unified taxonomy to understand *causal fairness* research field
- Prominent causal conceptions of algorithmic fairness, if implemented, can harm the groups they were designed to protect


Stylized Example: College Admissions





Stylized Example: College Admissions









Stylized Example: College Admissions

 Test Score			
73			
65			
80			
...			











Stylized Example: College Admissions

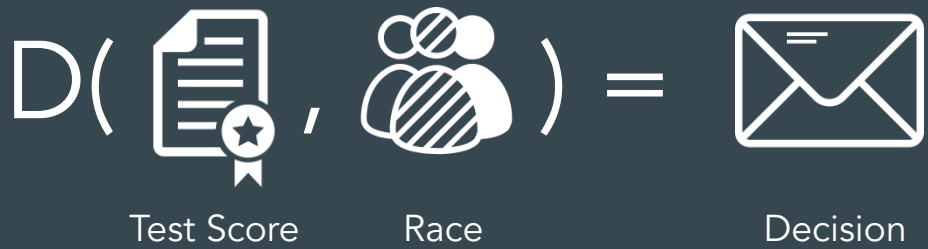
 Test Score	 Race Group		
73	Minority		
65	Majority		
80	Minority		
...	...		

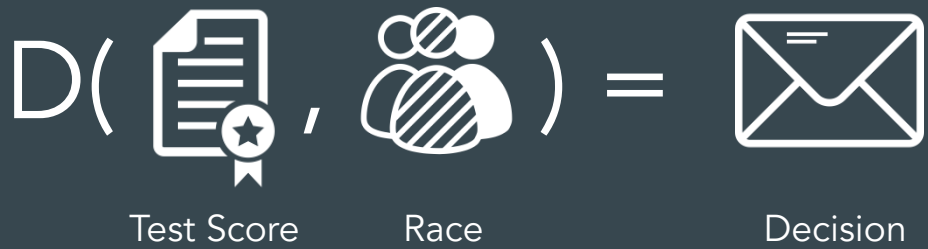
Stylized Example: College Admissions

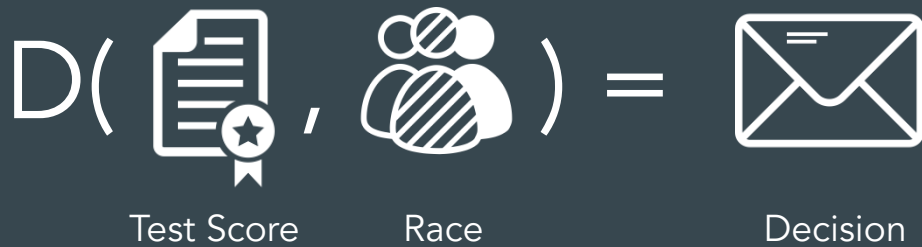
 Test Score	 Race Group	 Decision	
73	Minority		
65	Majority		
80	Minority		
...	

Stylized Example: College Admissions

 Test Score	 Race Group	 Decision	 Degree Attainment
73	Minority		
65	Majority		
80	Minority		
...








Degree
Attainment



Class Diversity





How to ensure that D is fair?



[Part 1: *causal fairness*
overview + taxonomy]

Traditional fairness definitions

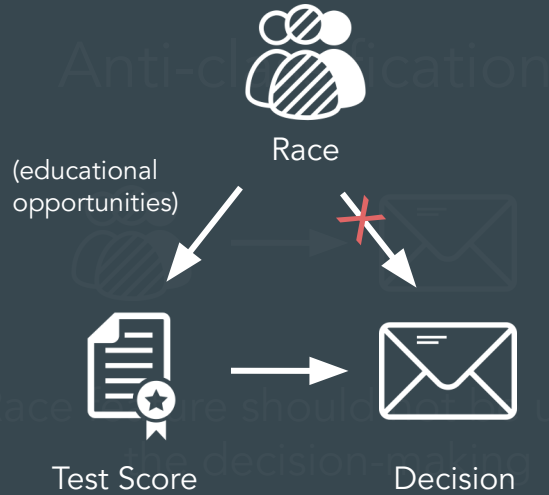
Anti-classification



Race feature should not be used in
the decision-making

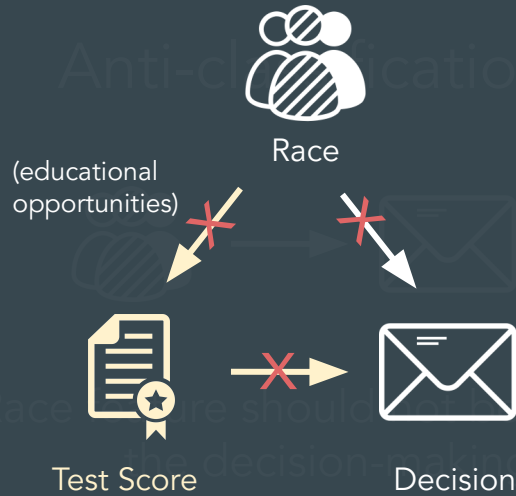
$$D(\text{Race}=95, \text{Minority}) =$$
$$D(\text{Race}=95, \text{Majority})$$

Causal Fairness Motivation



Race may still *indirectly* affect decisions

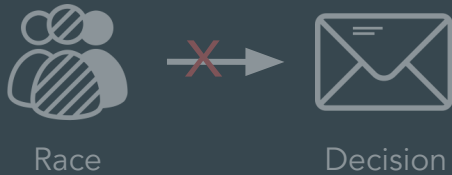
Causal Fairness Taxonomy



Family 1: Limit direct and indirect effects of race on decision

Traditional fairness definitions

Anti-classification



Race feature should not be used in the decision-making

$$D(\text{📄}=95, \text{👤}=Minority) = \\ D(\text{📄}=95, \text{👤}=Majority)$$

Classification parity

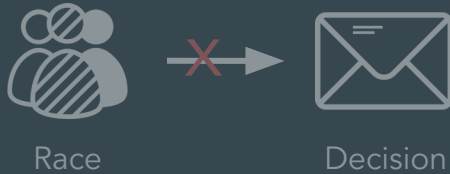


Model performance should be the same across groups

Precision = % of admits who successfully obtain a bachelor's degree

Traditional fairness definitions

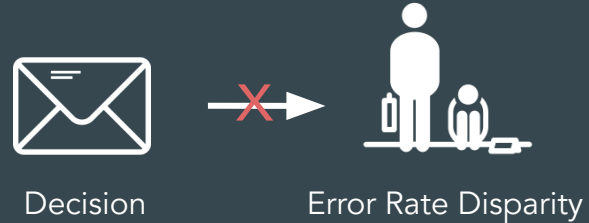
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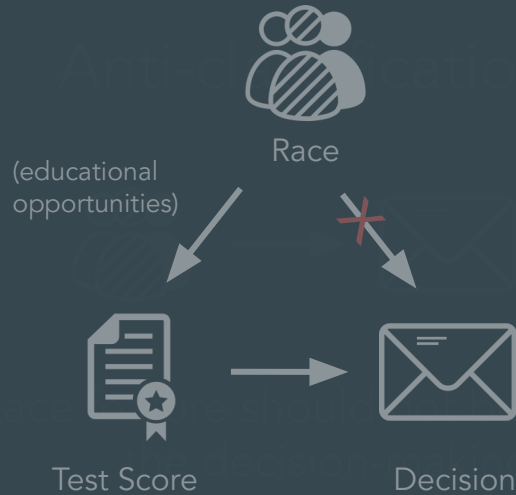
Classification parity



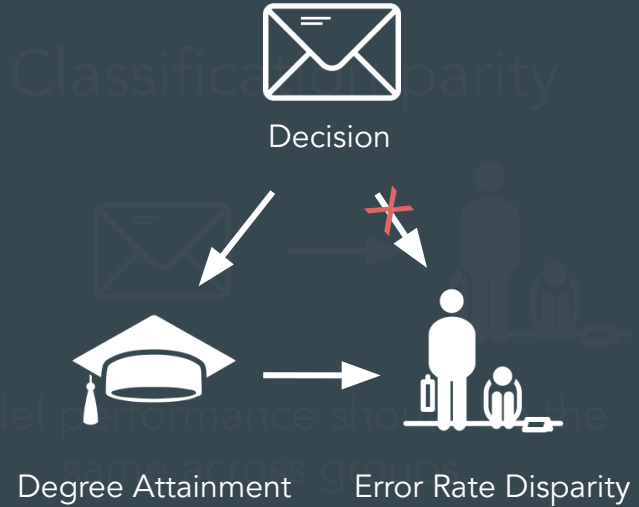
Model performance should be the same across groups

$$\text{Minority group precision} = \text{Majority group precision}$$

Causal Fairness Motivation

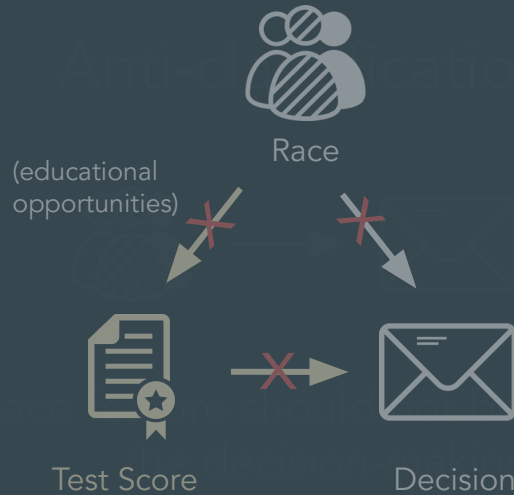


Race may still *indirectly* affect decisions

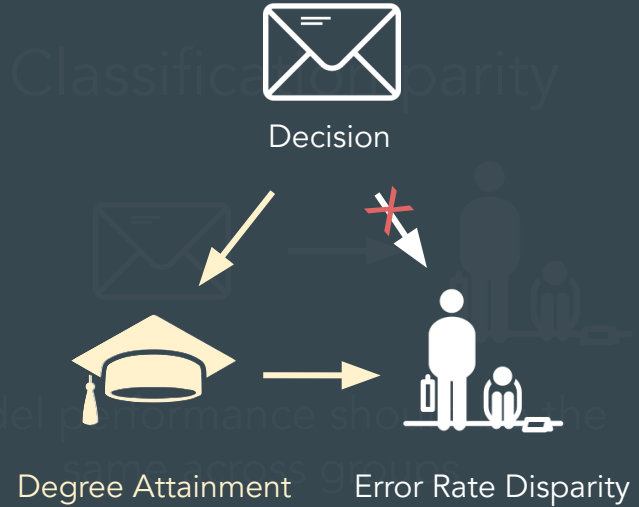


Decisions may affect graduation, altering error rates

Causal Fairness Taxonomy



Family 1: Limit direct and indirect effects of race on decision



Family 2: Model performance should be counterfactually equal between groups

Causal fairness taxonomy [see paper]

Family 1: Limit direct and indirect effects of race on decision

- Counterfactual fairness
- Path-specific fairness

Family 2: Limit counterfactual disparities between groups

- Counterfactual equalized odds
- Counterfactual predictive parity
- Principal fairness

Causal fairness taxonomy [see paper]

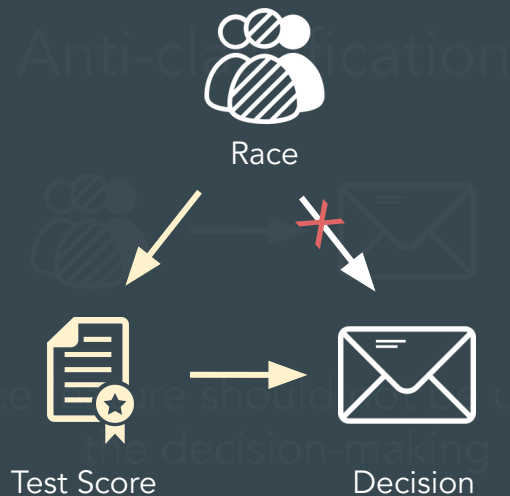
Family 1: Limit direct and indirect effects of race on decision

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Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

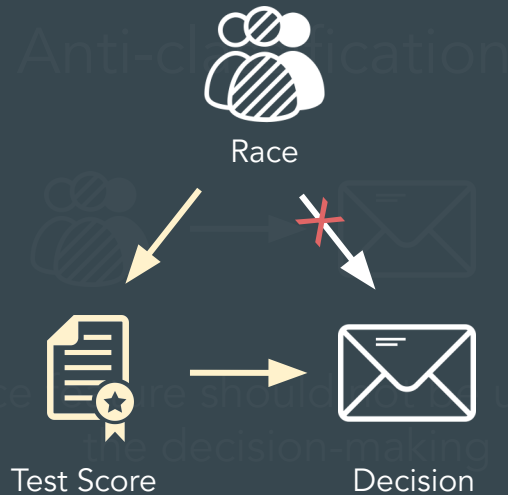
Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*

Model performance should be the same across groups

False positive rate (admits who did not graduate) should be equal between groups

Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

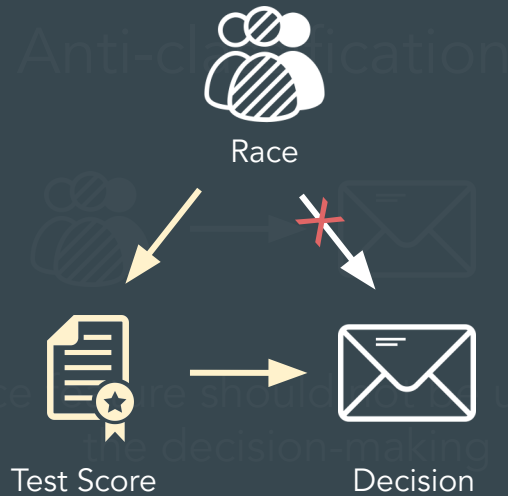
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Model performance should be the same across groups

[Important caveat: counterfactuals of race are epistemologically problematic]

(not graduate) should be equal between groups

Counterfactual Fairness



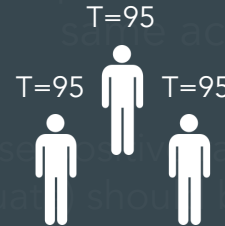
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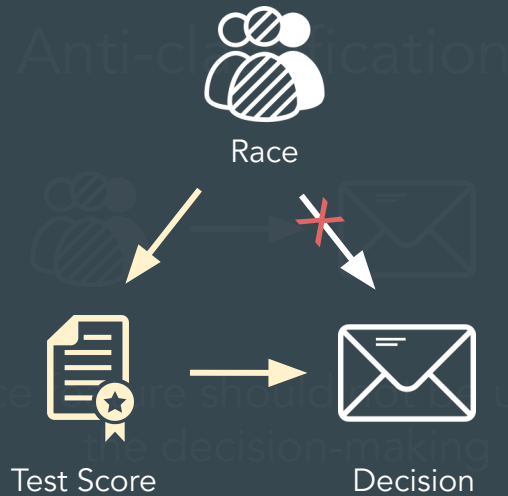
Model performance should be the same across groups

Fake (admits who did not graduate) should be equal between groups



Majority
(real world)

Counterfactual Fairness



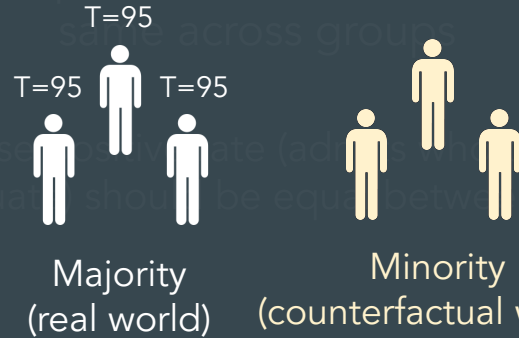
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Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*

Model performance should be the same across groups

Race should not be used in decision-making
False positive rate (and not-graduate rate) should be equal between groups



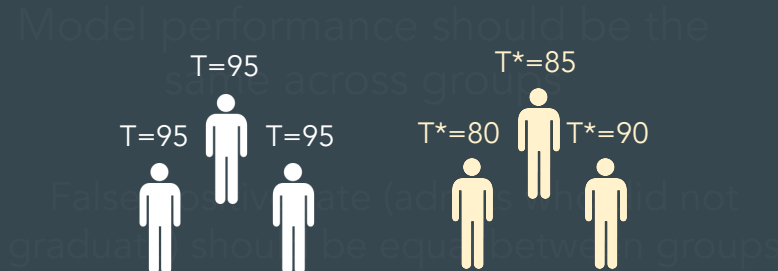
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

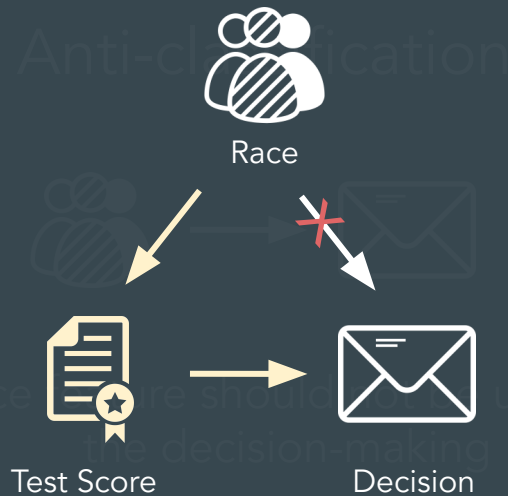
Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*



Majority (real world) Minority (counterfactual world)

[T* decreases due to reduced access to educational opportunities]

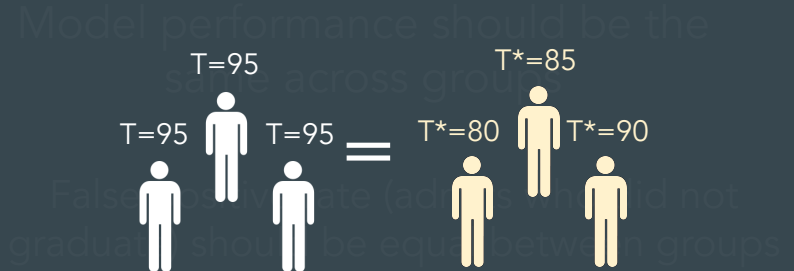
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

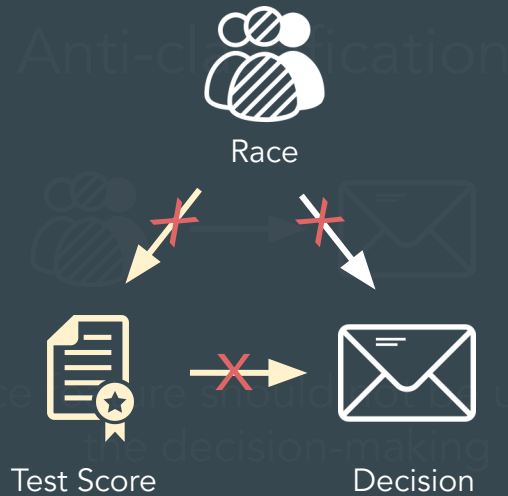
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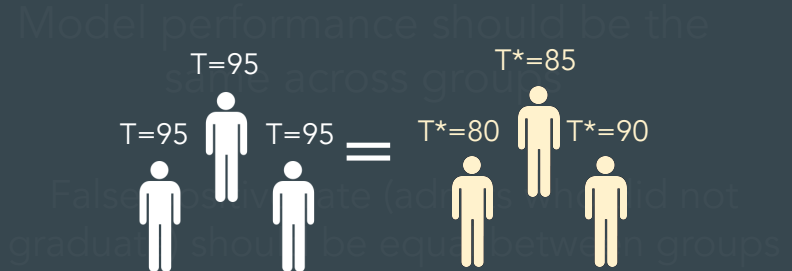
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*



[T* decreases due to reduced access to educational opportunities]

Part 2: What are the downstream consequences of causal fairness?



Counterfactual Fairness

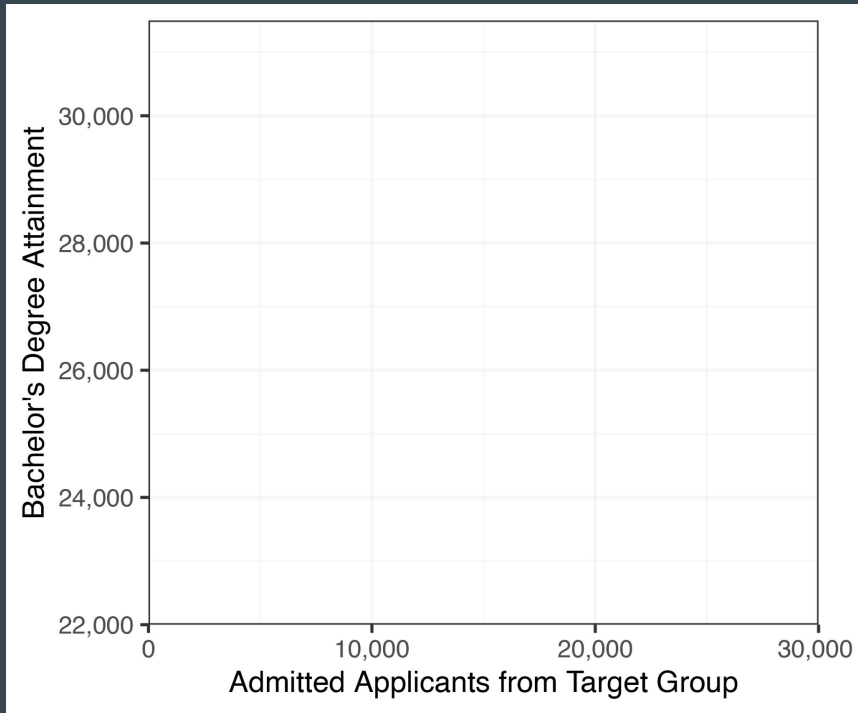


Diversity

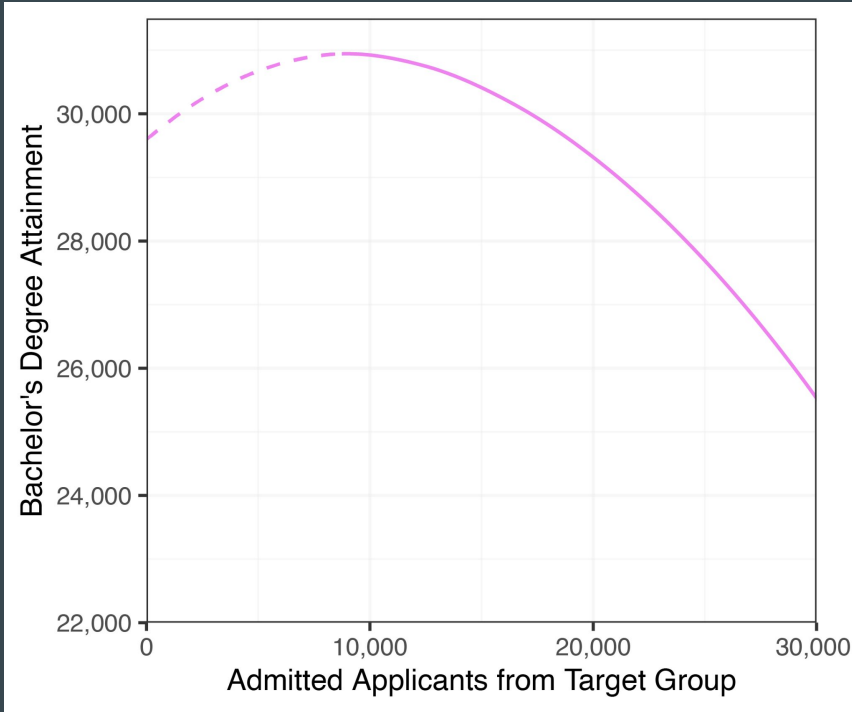


Degree Attainment

Illustrative example

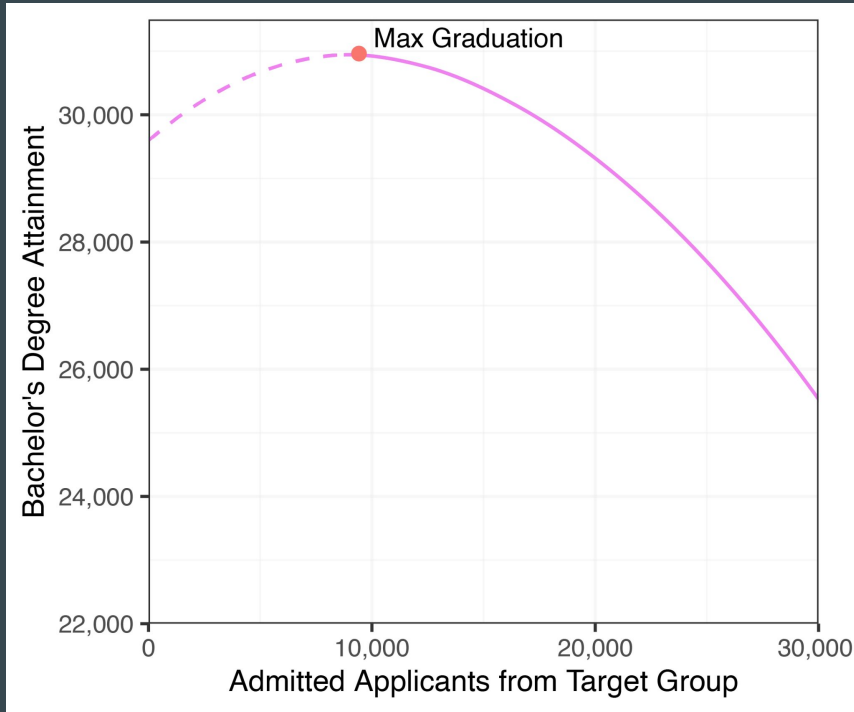


Illustrative example



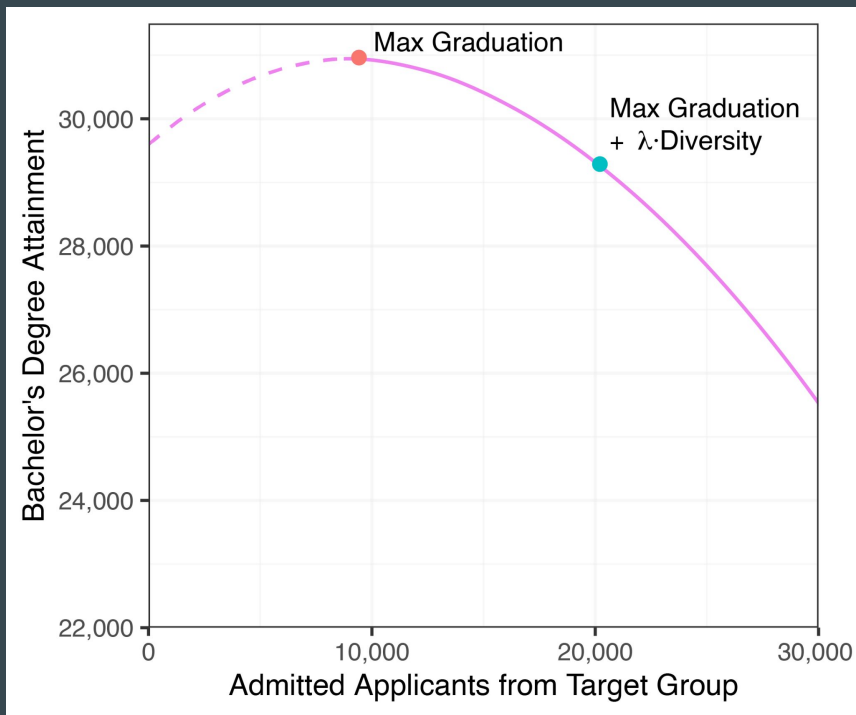
Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example



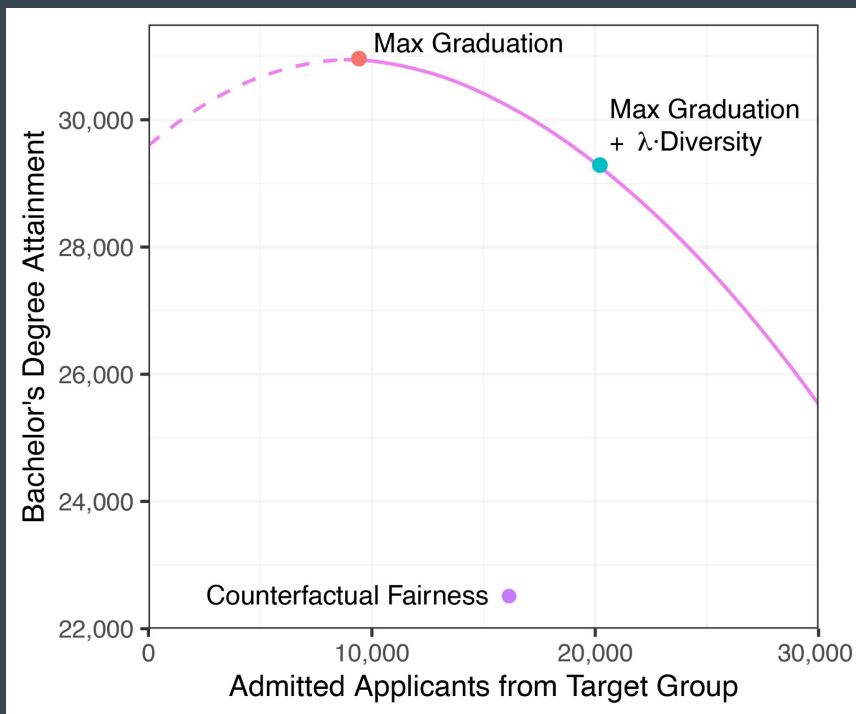
Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example

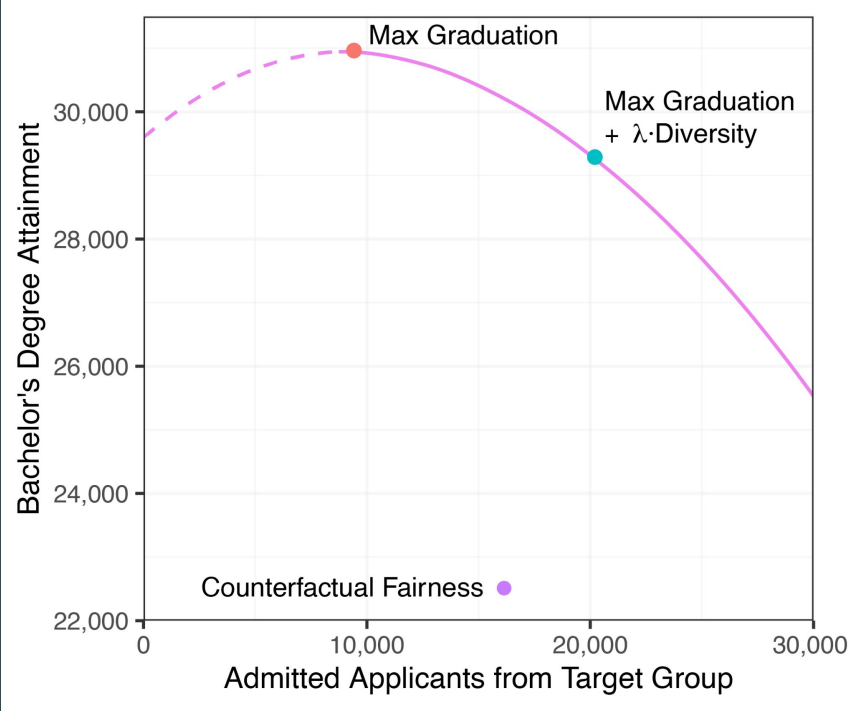


Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example



Illustrative example

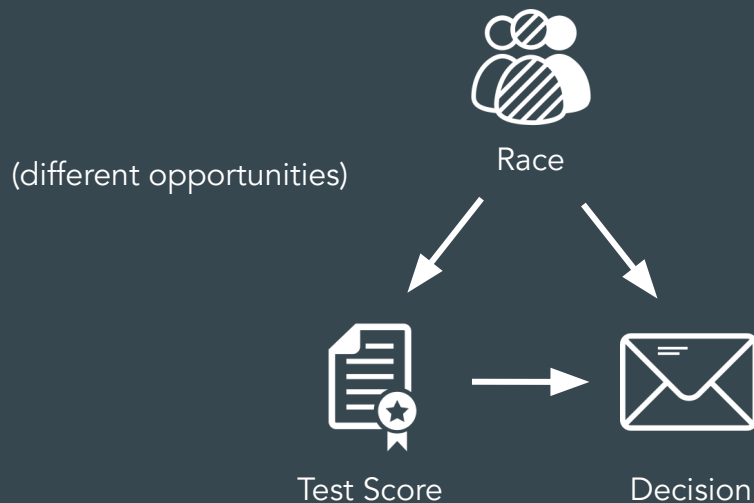


Counterfactual
Fairness

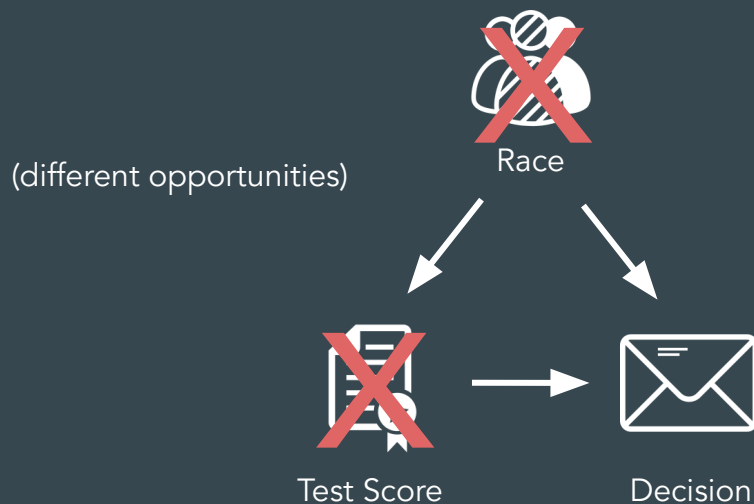


Randomized
Lottery

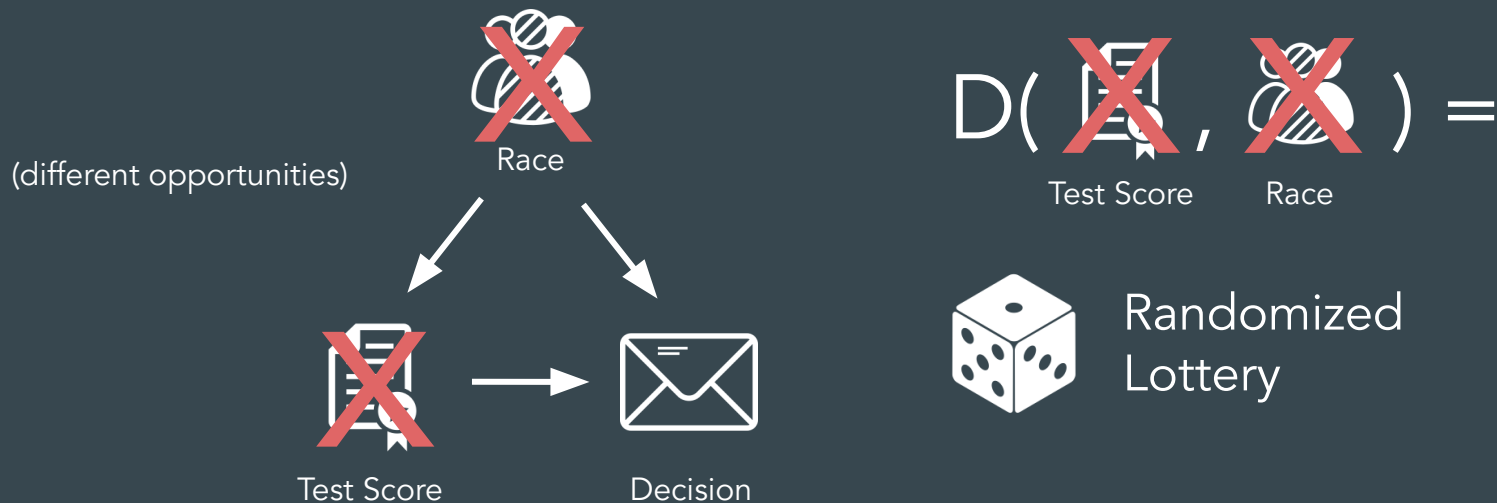
Theoretical result: Under mild assumptions, counterfactual fairness requires decisions to ignore race and all downstream covariates



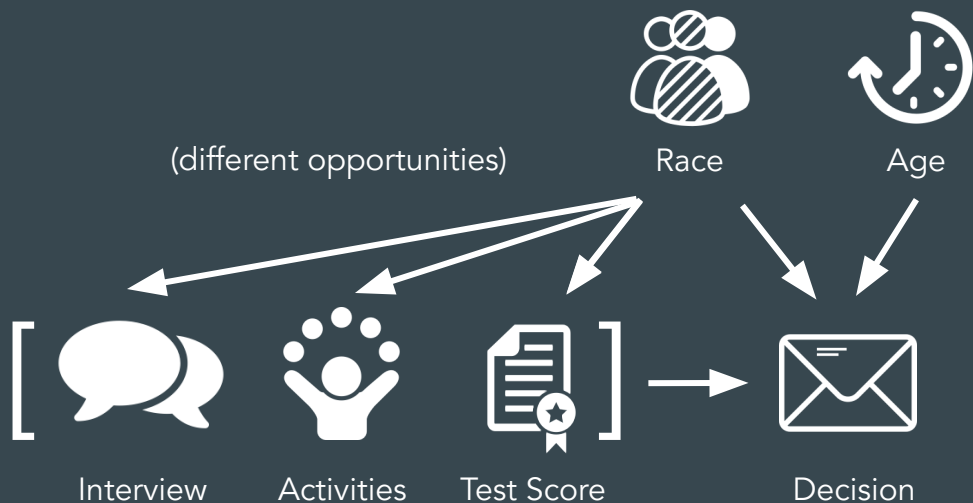
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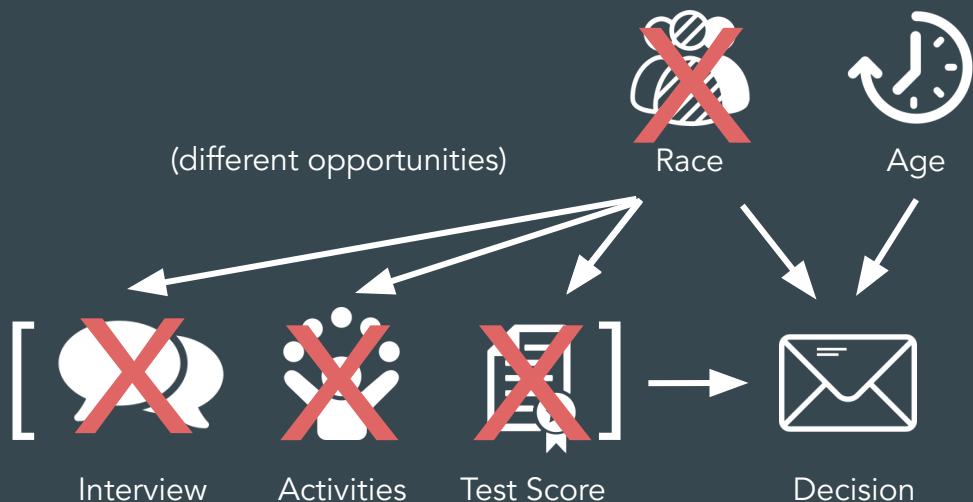
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Decisions based exclusively on age

Proof sketch



$D(T = \text{Low}, \text{Race} = \text{Majority})$



$D(T = \text{Med.}, \text{Race} = \text{Majority})$



$D(T = \text{High}, \text{Race} = \text{Majority})$



$D(T = \text{Low}, \text{Race} = \text{Minority})$

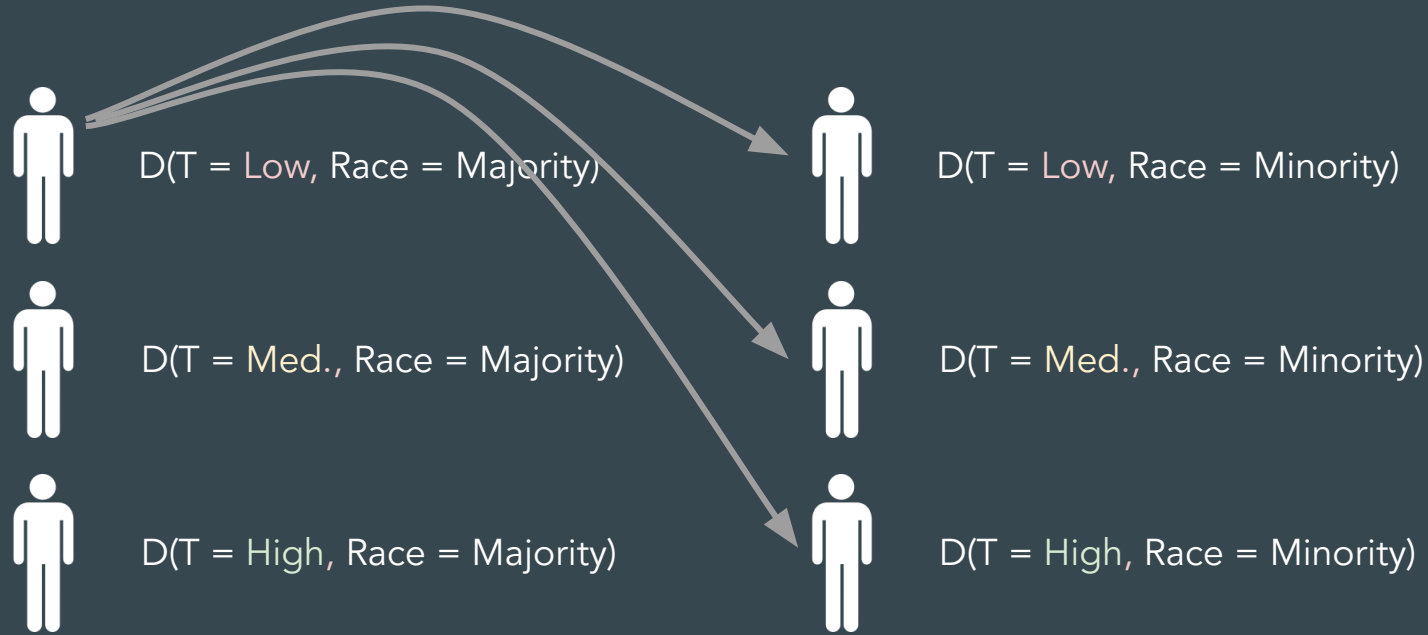


$D(T = \text{Med.}, \text{Race} = \text{Minority})$

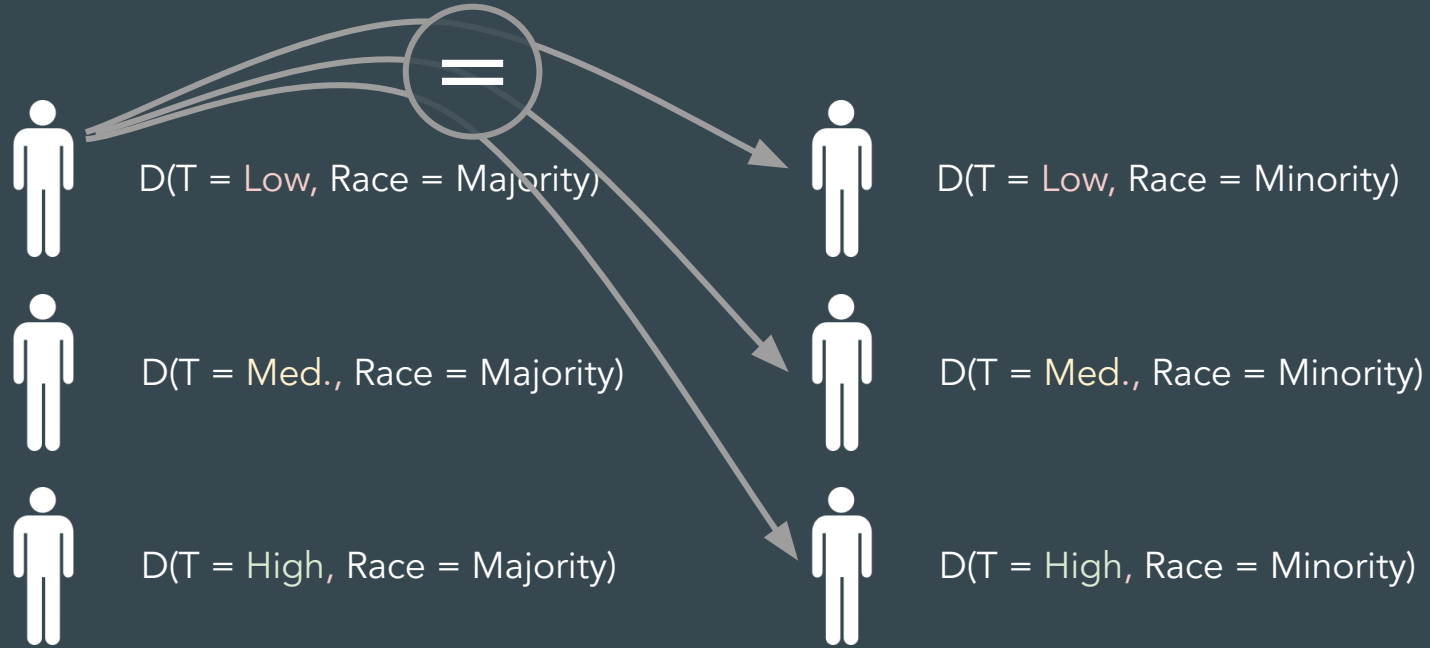


$D(T = \text{High}, \text{Race} = \text{Minority})$

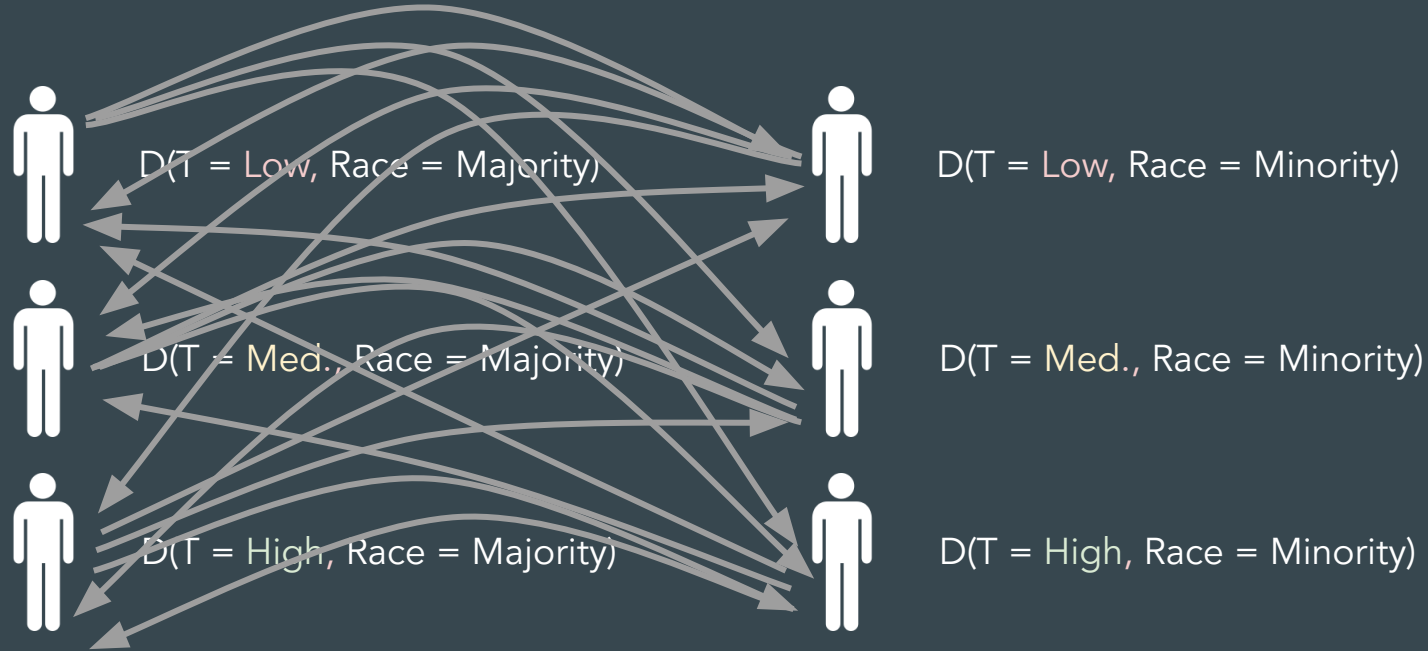
Proof sketch



Proof sketch



Proof sketch



Causal fairness taxonomy [see paper]

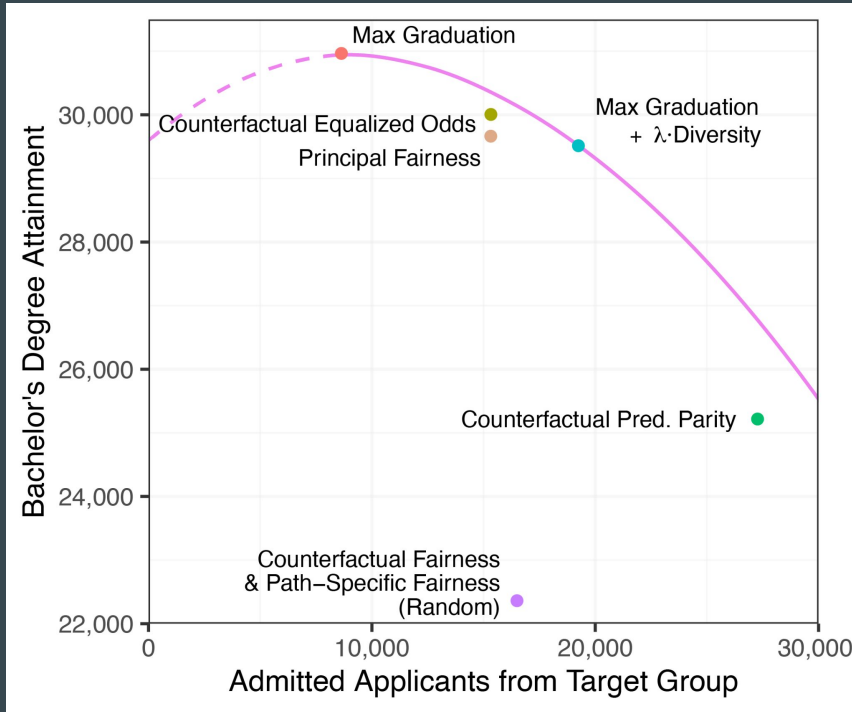
Family 1: Limit direct and indirect effects of race on decision

- Counterfactual fairness
- Path-specific fairness

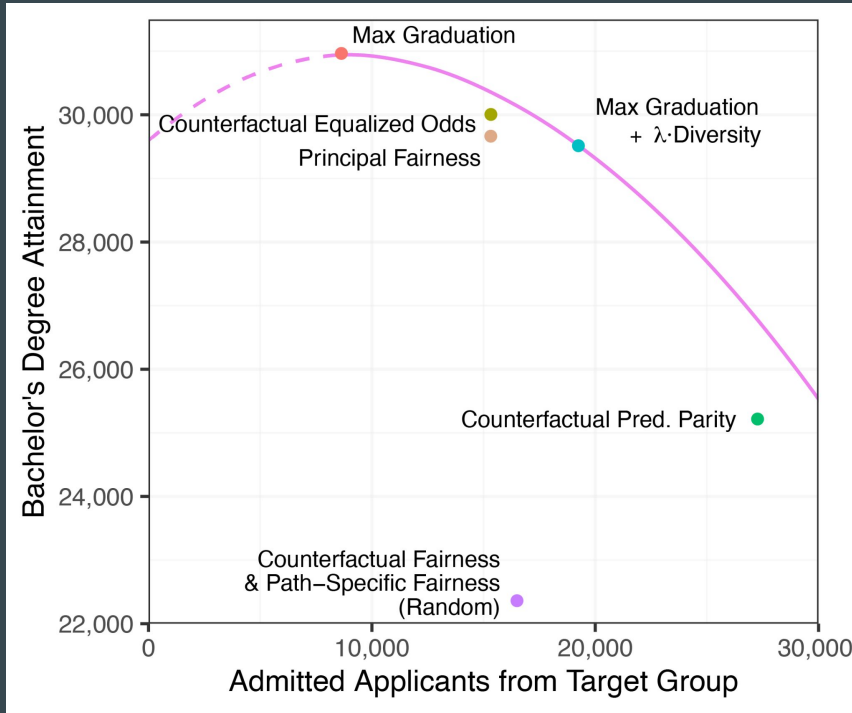
Family 2: Limit counterfactual disparities between groups

- Counterfactual equalized odds
- Counterfactual predictive parity
- Principal fairness

Key theoretical result #2



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Causal Fairness
(Family 1 and 2)



Decreased Degree Attainment



Decreased Class Diversity



Key theoretical result #2

In *almost every* case (in a measure theoretic sense) it is impossible to satisfy prominent causal fairness definitions and be Pareto optimal



Causal Fairness
(Family 1 and 2)



Decreased
Degree
Attainment



Decreased
Class Diversity



Summary

- Causal fairness definitions lead to Pareto inefficient decisions, perversely harming the groups they were designed to protect
- Directly optimizing for desired outcomes (e.g. degree attainment, diversity) may be preferable

Thank You!



Full Paper

H. Nilforoshan*, J. Gaebler*, R. Shroff, & S. Goel. "Causal Conceptions of Fairness and their Consequences." *International Conference on Machine Learning (ICML 2022)*.



Technical Blog Post

jgaeb.com/2022/07/18/prevalence.html

[jgaeb.com]

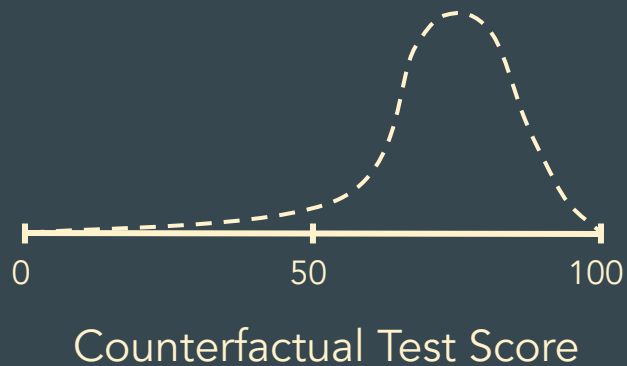
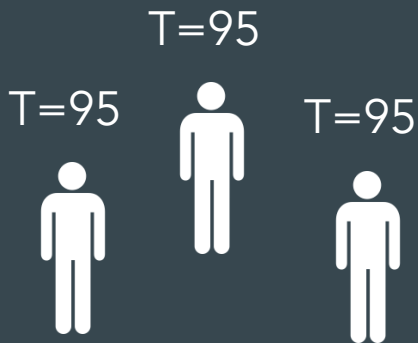
[jgaeb@stanford.edu]

[hamedn.com]

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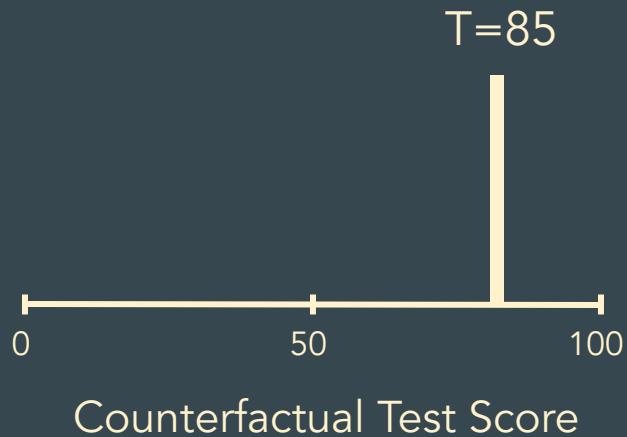
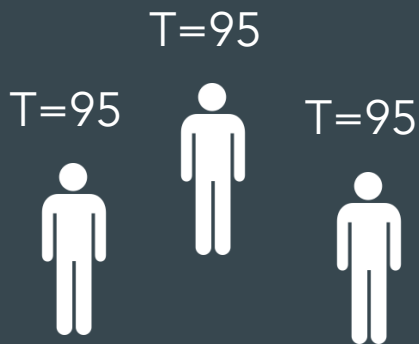
Assumptions

There is variance in the counterfactual distribution of covariates

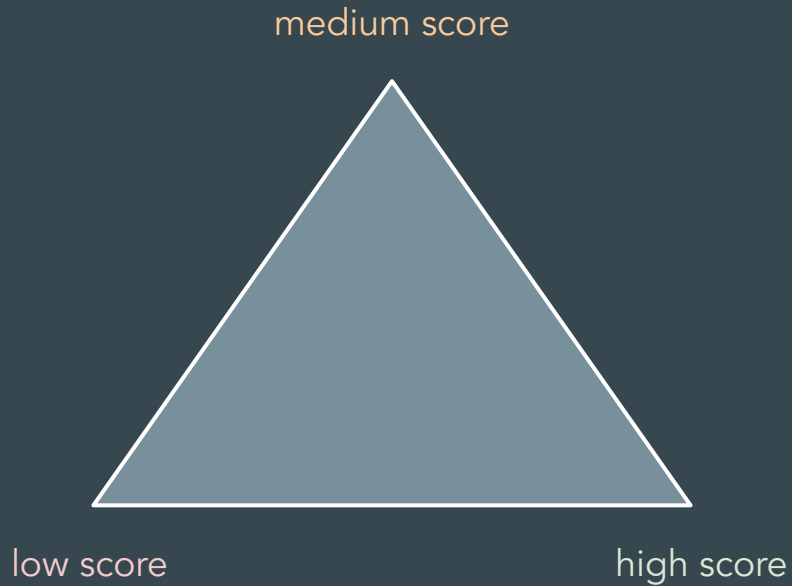


Assumptions

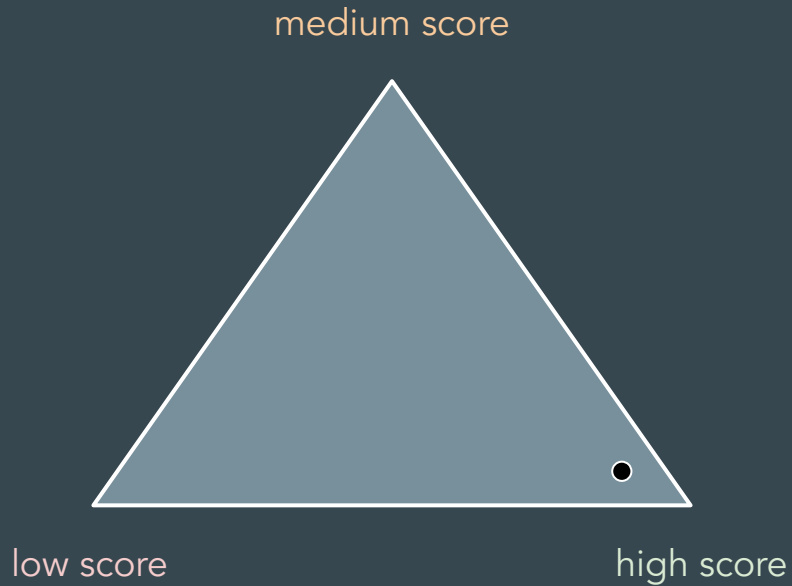
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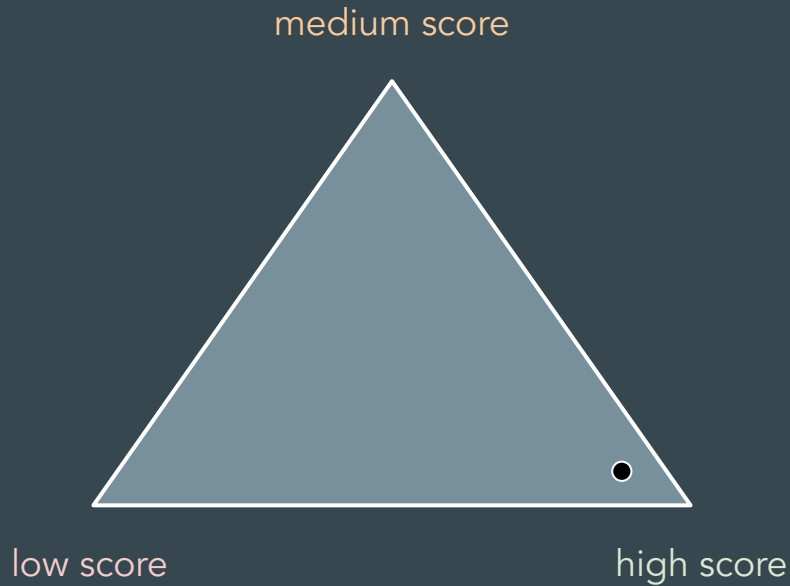
What do we mean by "almost every"?



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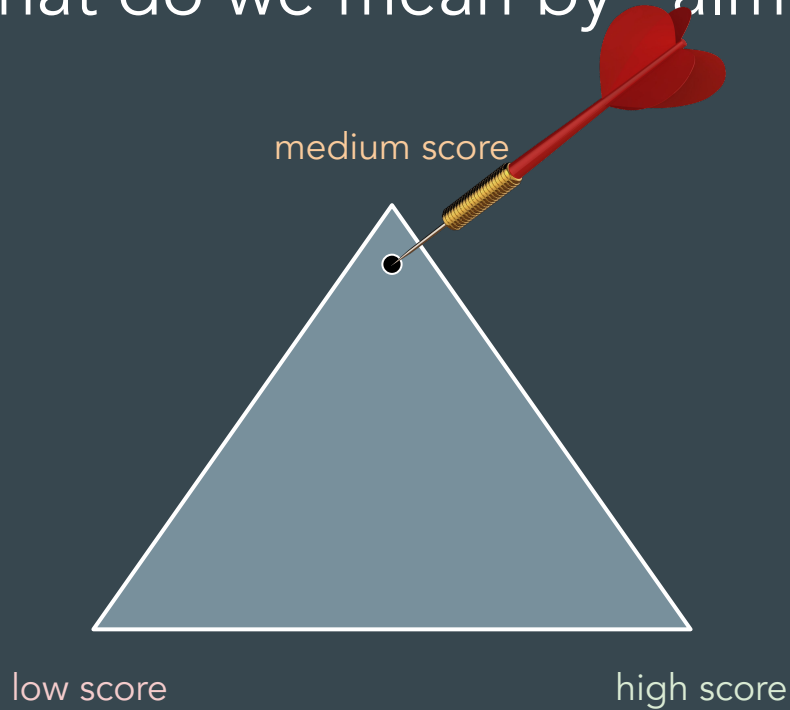


$$P(\text{📄} = \text{low}) = 0.05$$

$$P(\text{📄} = \text{medium}) = 0.05$$

$$P(\text{📄} = \text{high}) = 0.90$$

What do we mean by "almost every"?

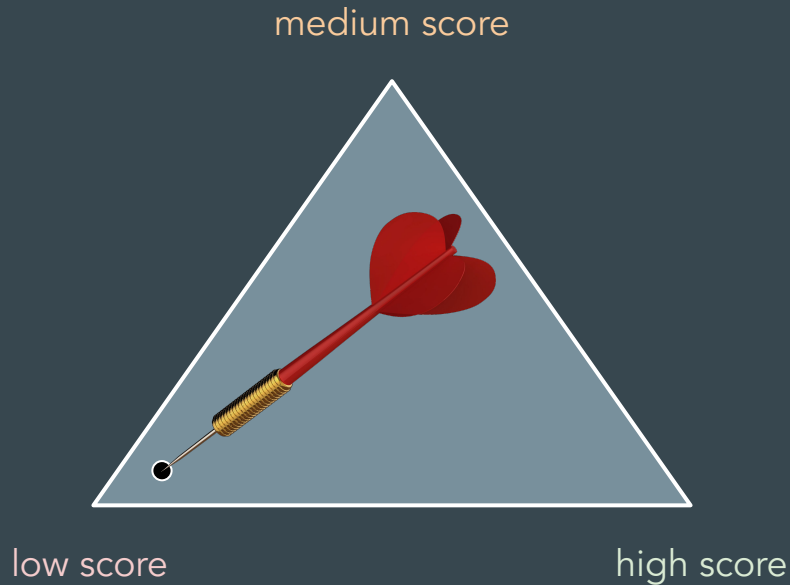


$$P(\text{📄} = \text{low}) = 0.05$$

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What do we mean by "almost every"?



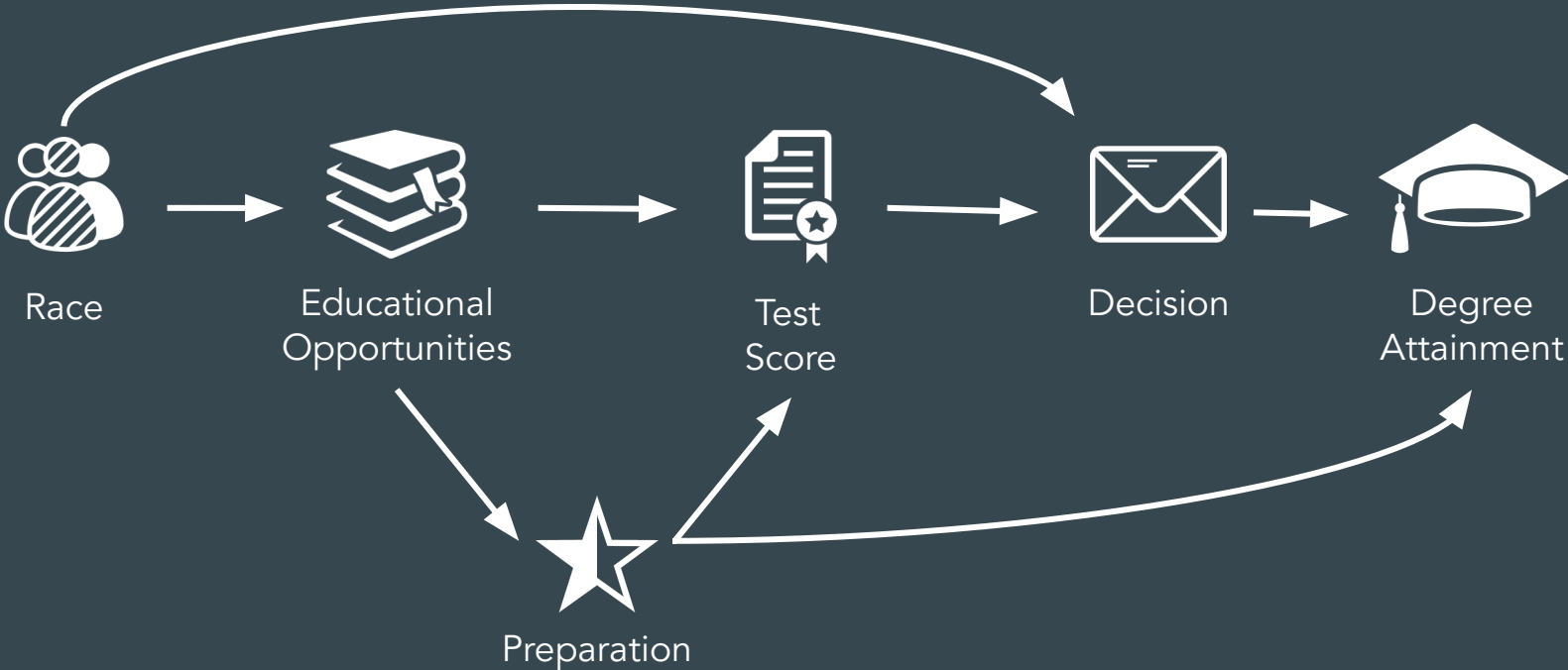
$$P(\text{📄} = \text{low}) = 0.90$$

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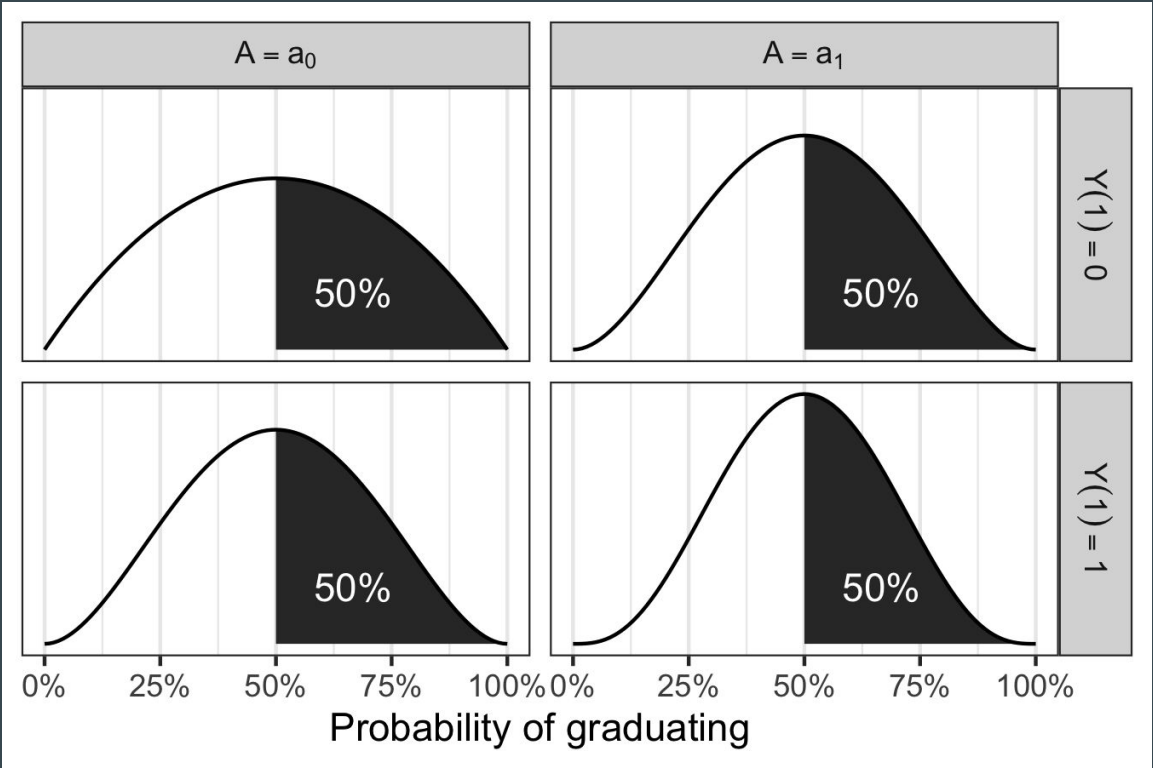
$$P(\text{📄} = \text{high}) = 0.05$$

$P(\downarrow \text{👤} \downarrow \text{🎓} \text{ Pareto Inefficient} \mid \text{🎯 Randomly Chosen Distribution}) = 1.0$

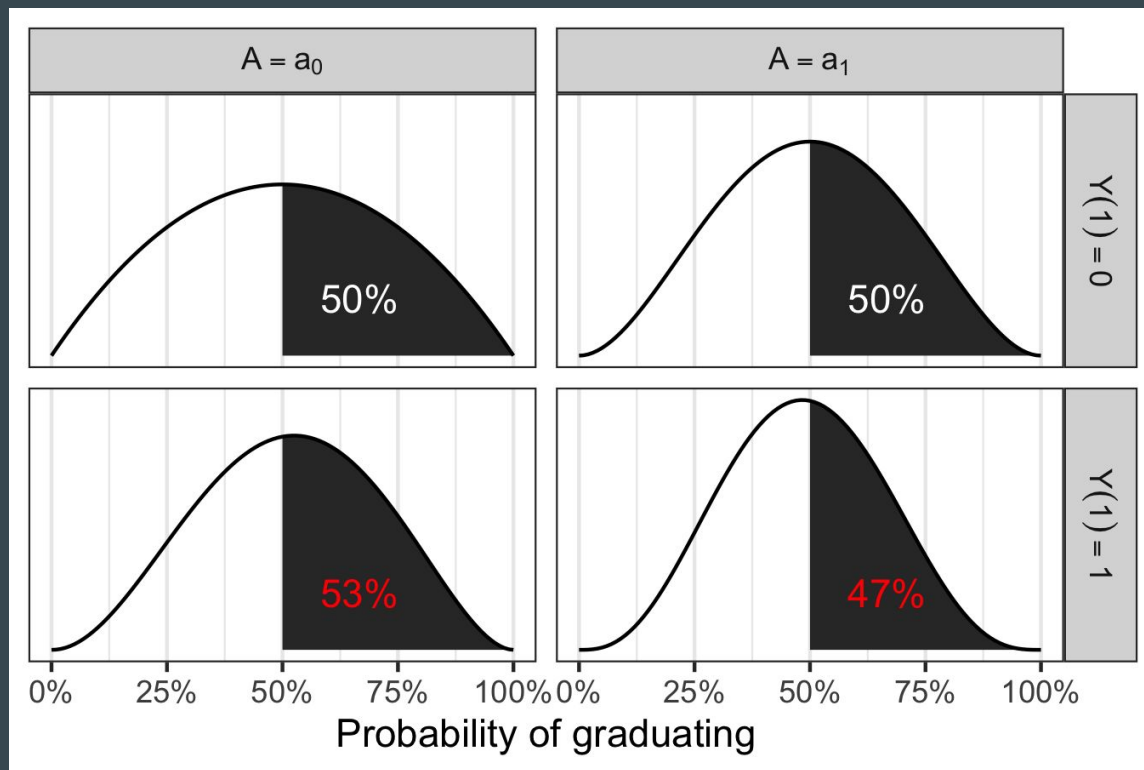
Simulation variables



Key idea



Key idea



Key idea

