

Test-Time Training with Self-Supervision for Generalization under Distribution Shifts

Yu Sun, Xiaolong Wang, Zhuang Liu, John Miller, Alexei Efros, Moritz Hardt
UC Berkeley

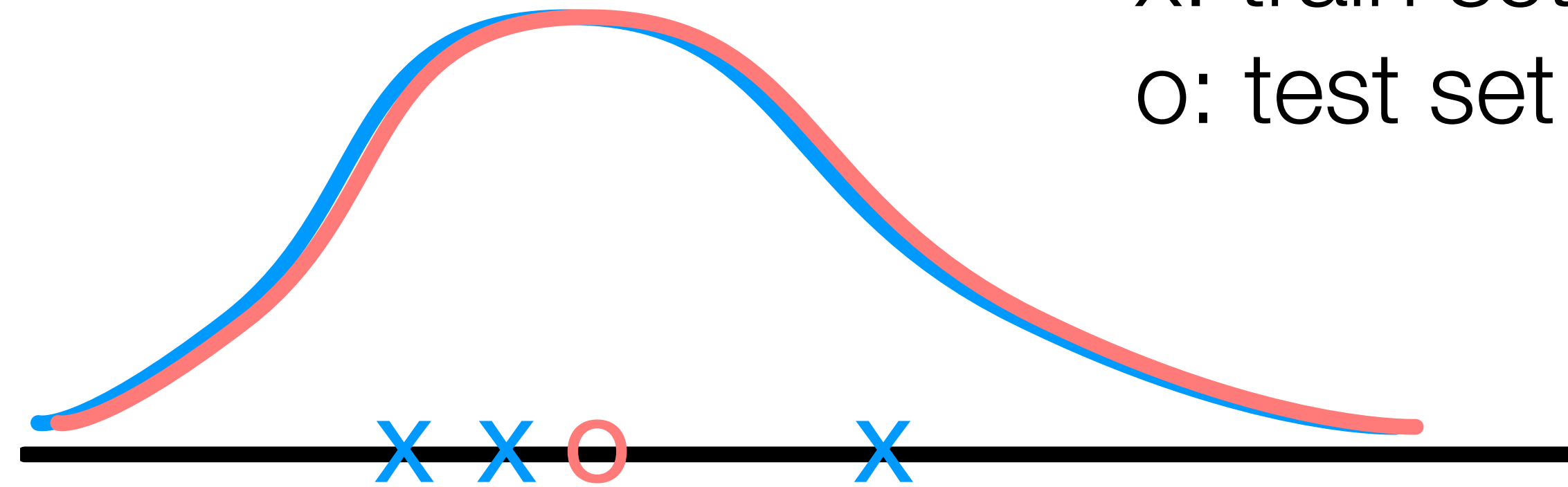
ICML 2020

same distribution

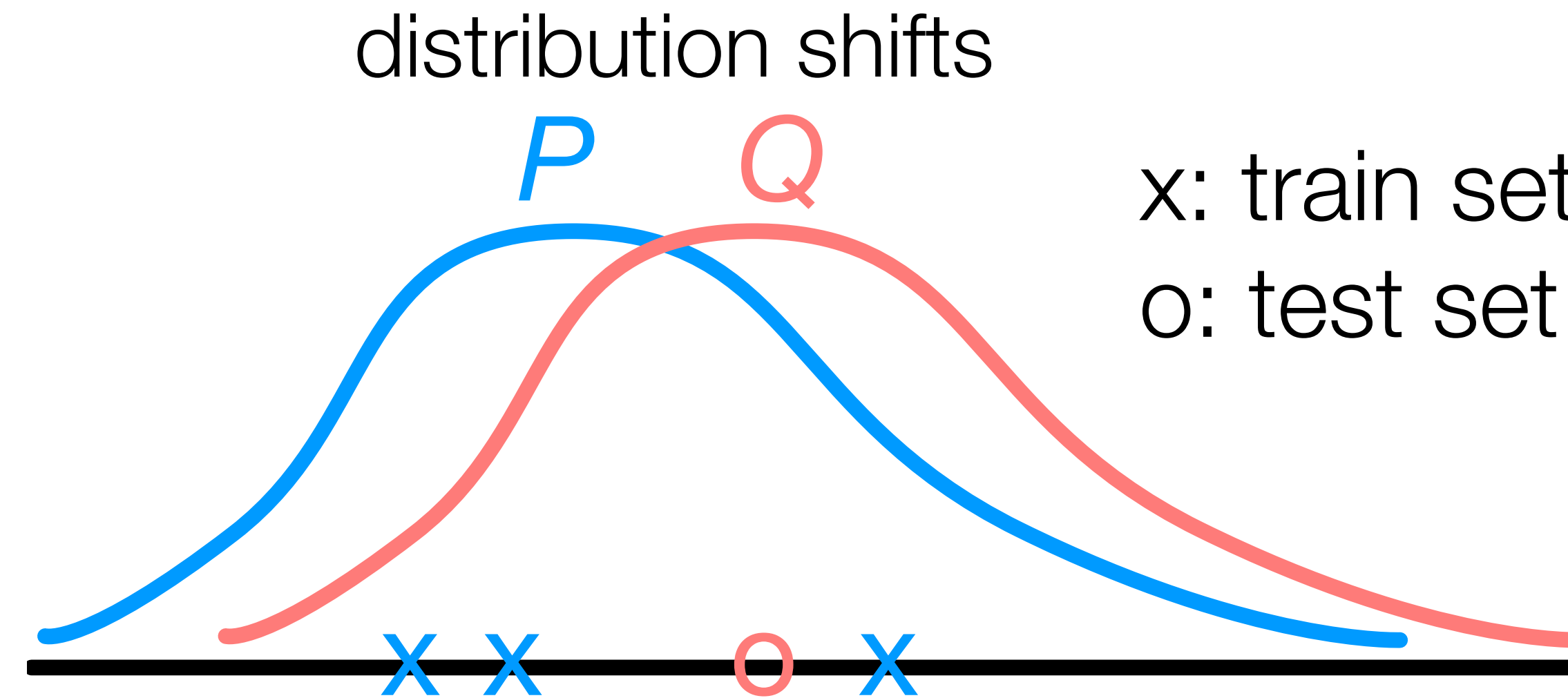
$$P = Q$$

x: train set

o: test set

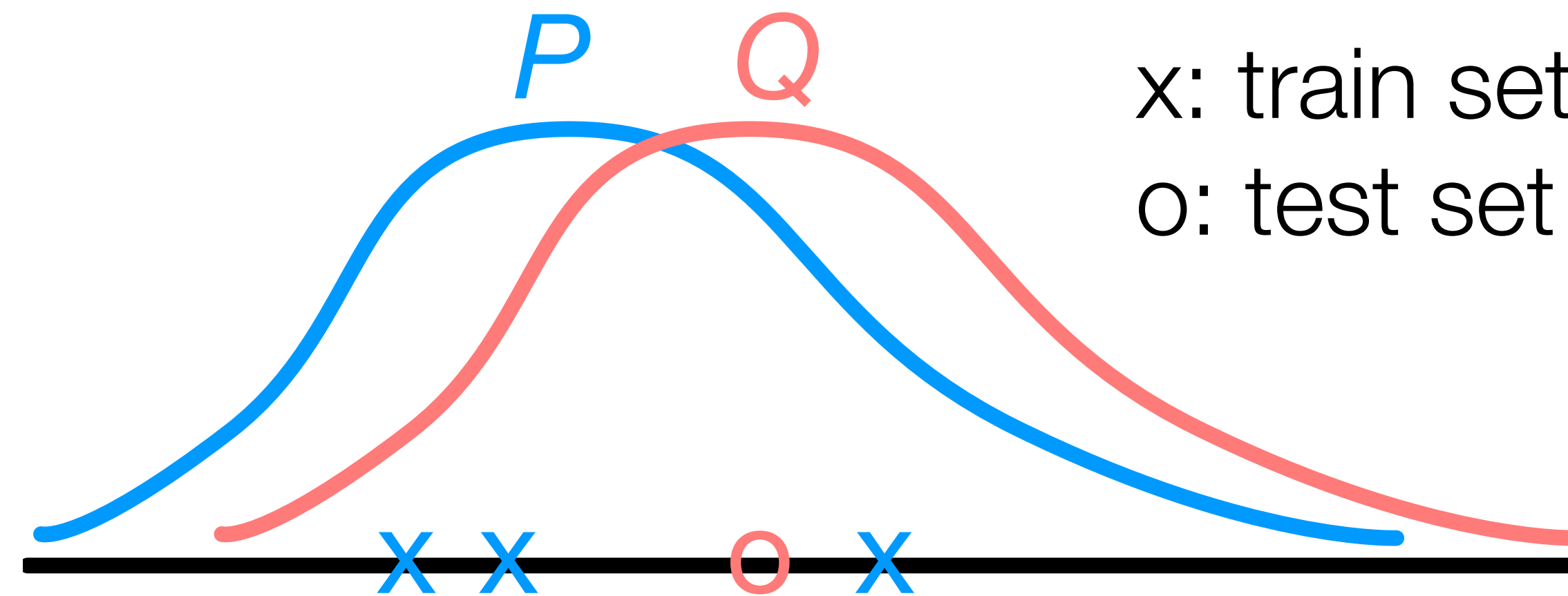


- **In theory:** same distribution for training and testing

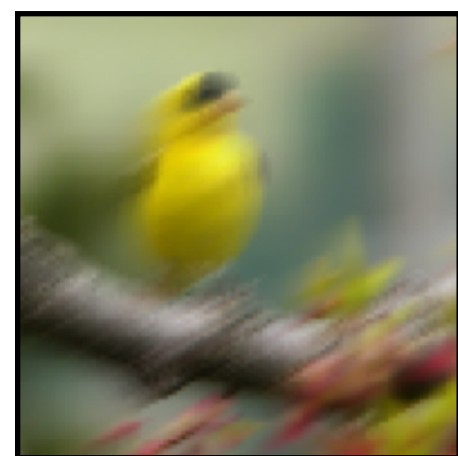
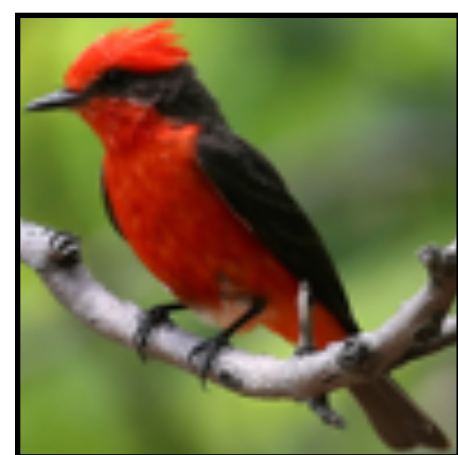


- **In theory:** same distribution for training and testing
- **In the real world:** distribution shifts are everywhere

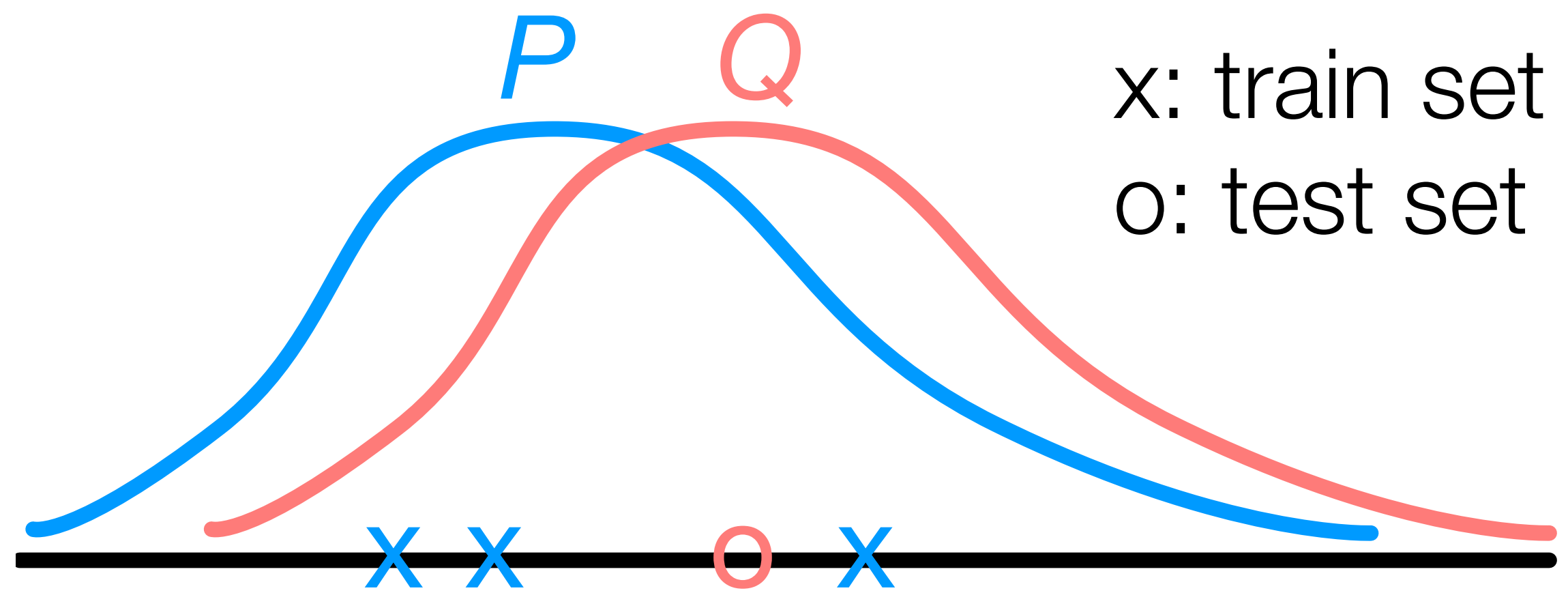
distribution shifts



- **In theory:** same distribution for training and testing
- **In the real world:** distribution shifts are everywhere

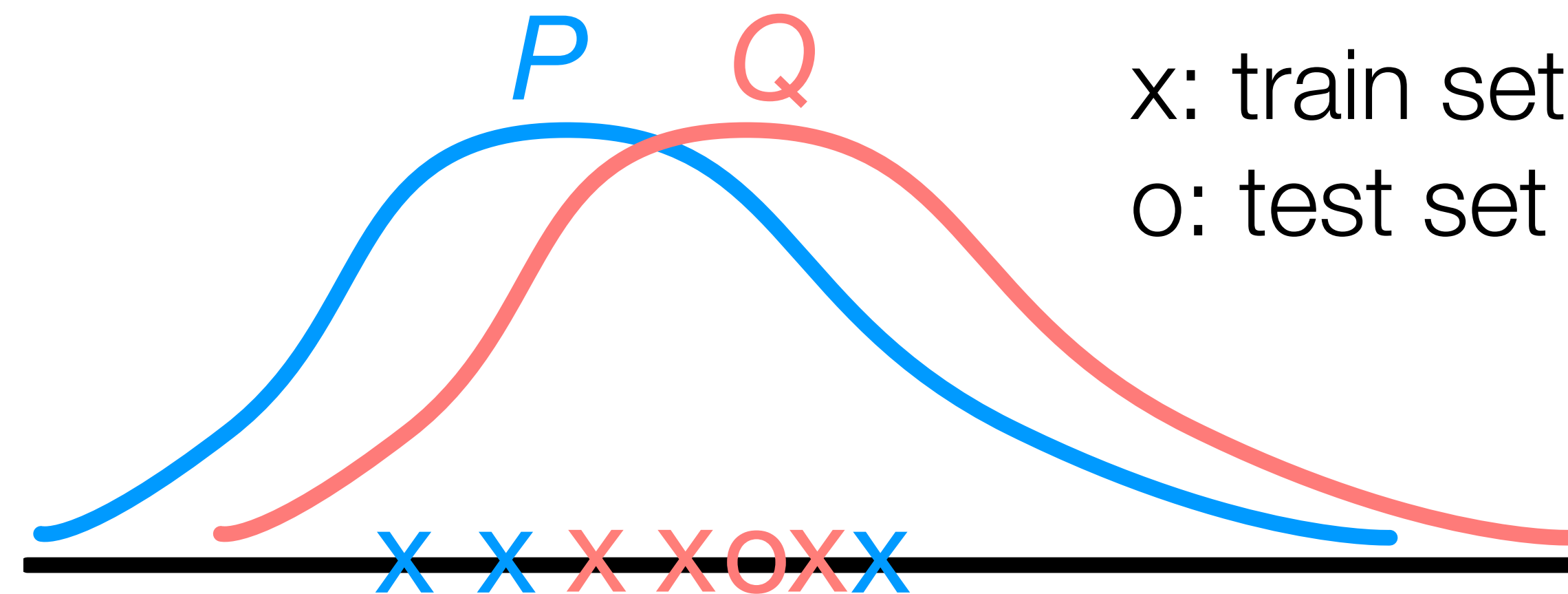


Existing paradigms



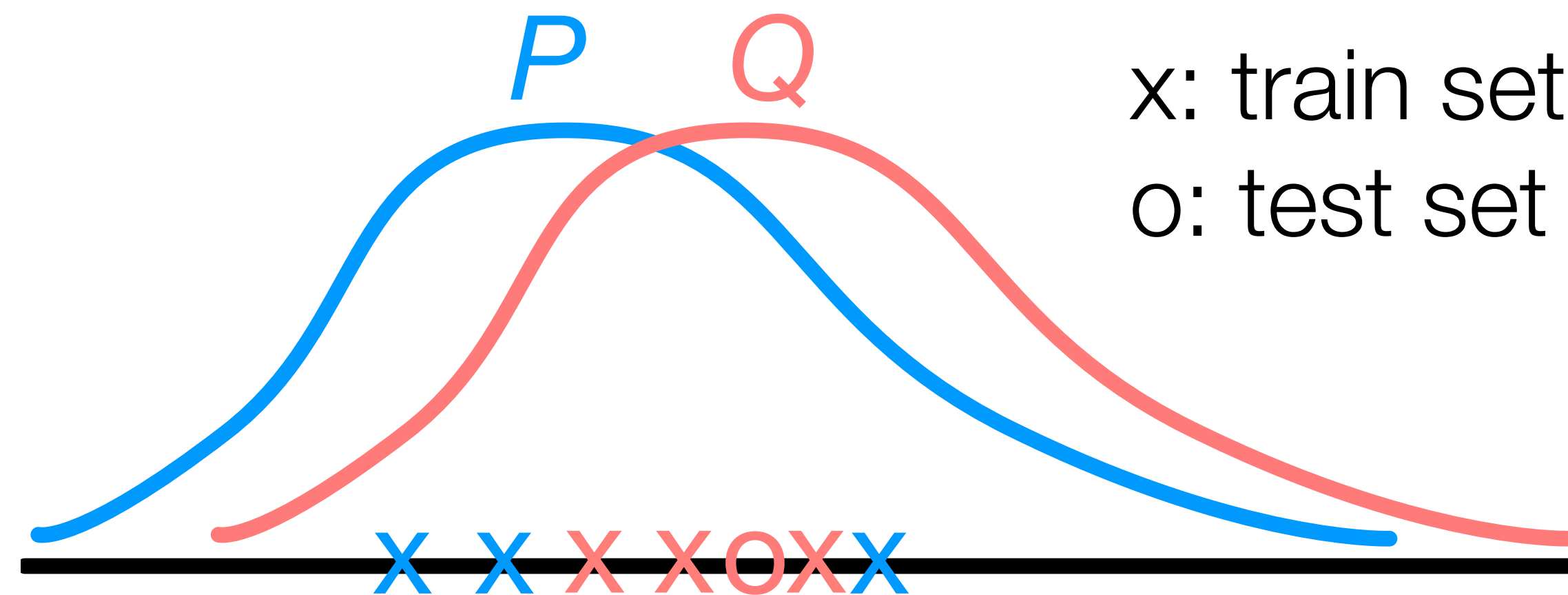
Existing paradigms

- **Domain adaptation**
 - Data from the test distribution



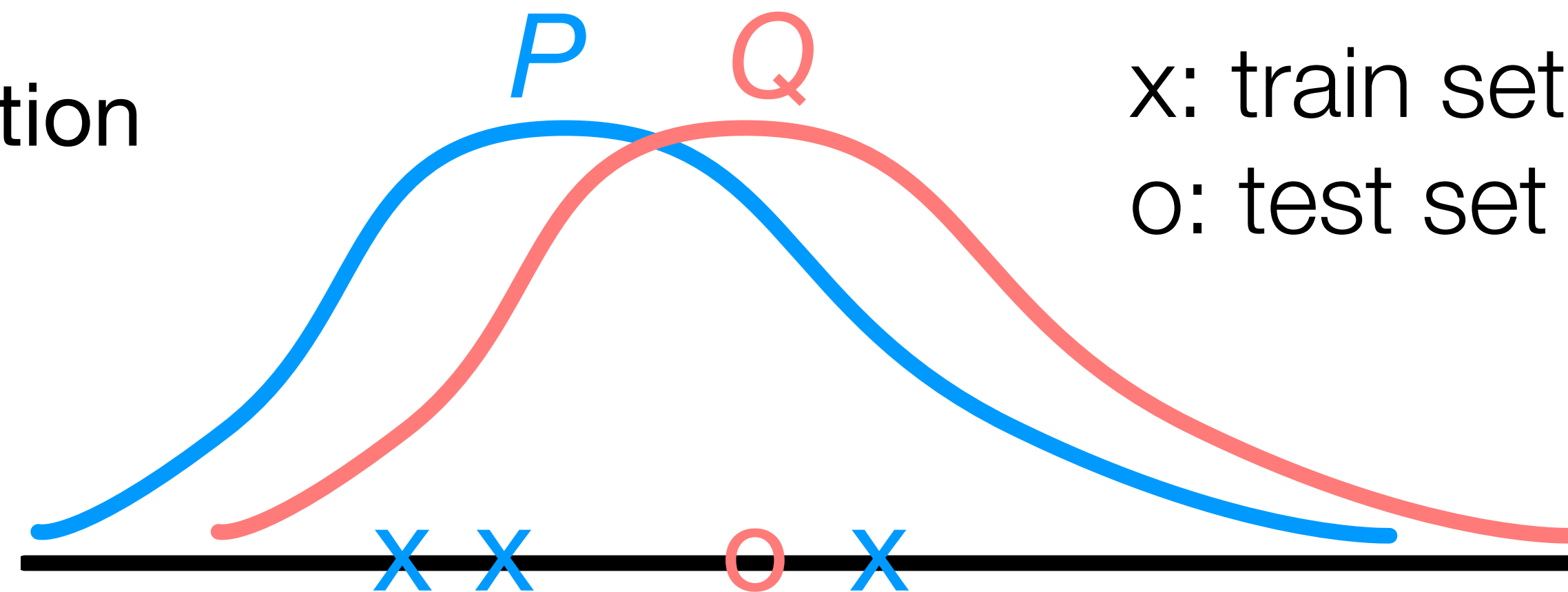
Existing paradigms

- **Domain adaptation**
 - Data from the test distribution (maybe unlabeled)
 - Hard to know the test distribution



Existing paradigms

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution



Domain generalization via invariant feature representation
Muandet, Balduzzi and Scholkopf, 2013

Domain generalization for object recognition with multi-task autoencoders
Ghifary, Bastiaan, Zhang and Balduzzi, 2015

Domain Generalization by Solving Jigsaw Puzzles
Carlucci, D'Innocente, Bucci, Caputo and Tommasi, 2019

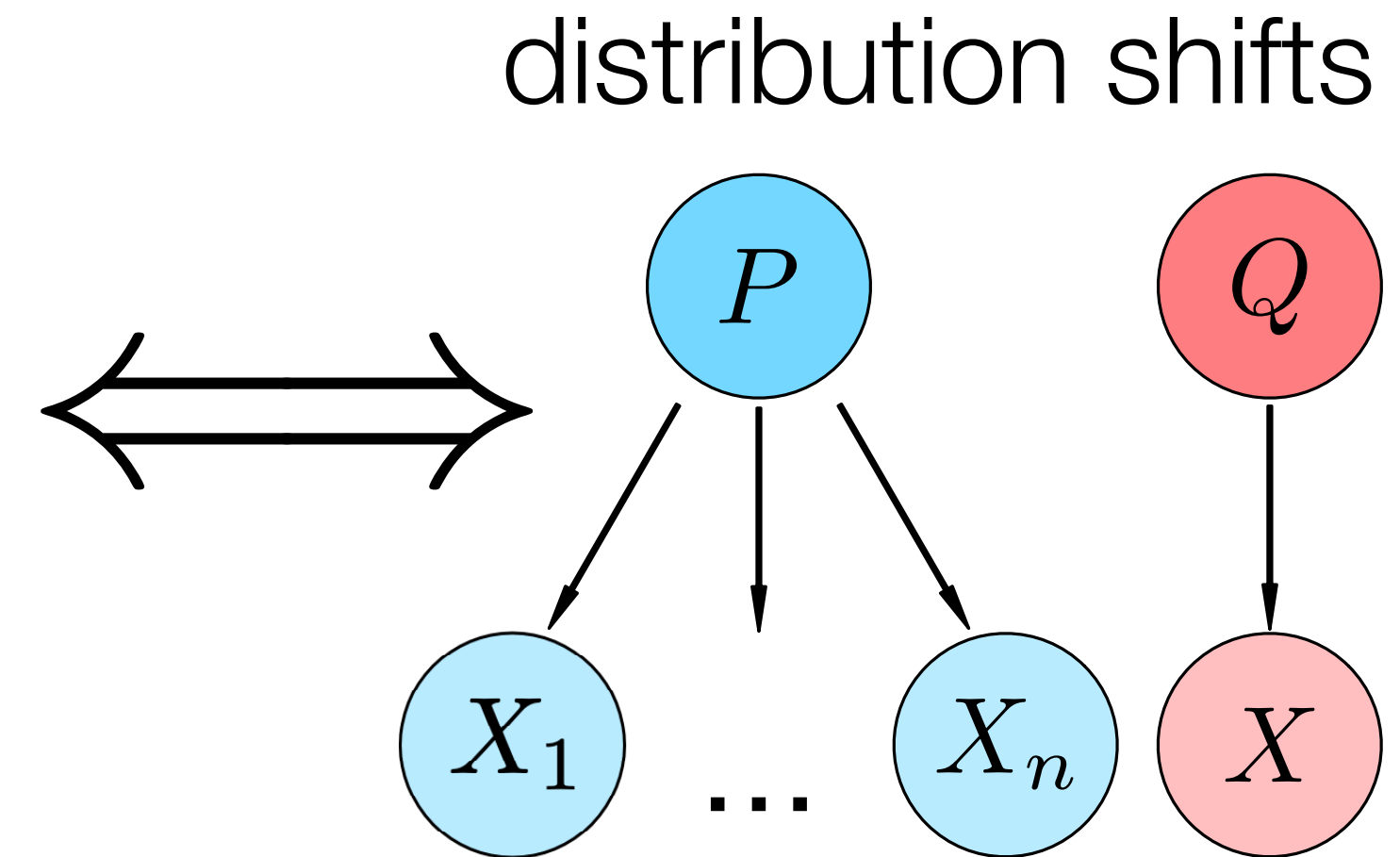
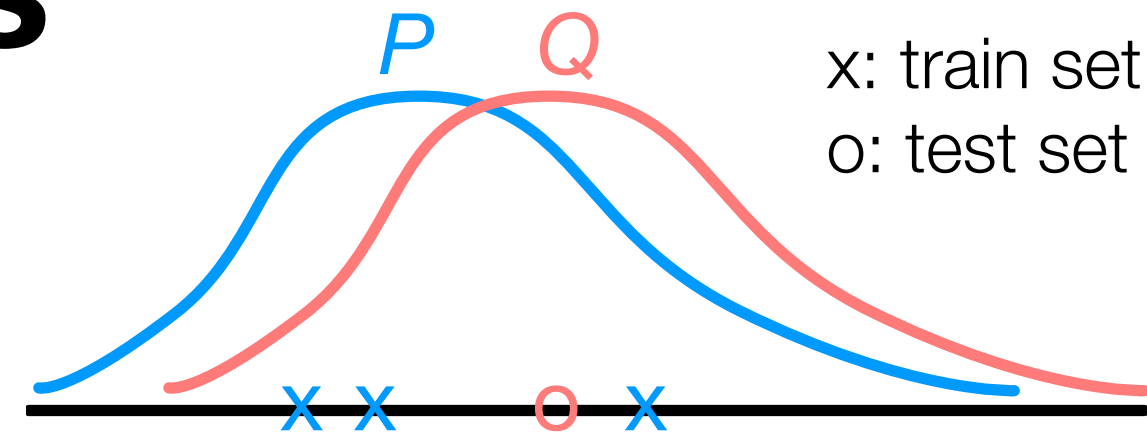
Existing paradigms

- **Domain adaptation**

- Data from the test distribution
- Hard to know the test distribution

- **Domain generalization**

- Data from the meta distribution



Domain generalization via invariant feature representation
Muandet, Balduzzi and Scholkopf, 2013

Domain generalization for object recognition with multi-task autoencoders
Ghifary, Bastiaan, Zhang and Balduzzi, 2015

Domain Generalization by Solving Jigsaw Puzzles
Carlucci, D'Innocente, Bucci, Caputo and Tommasi, 2019

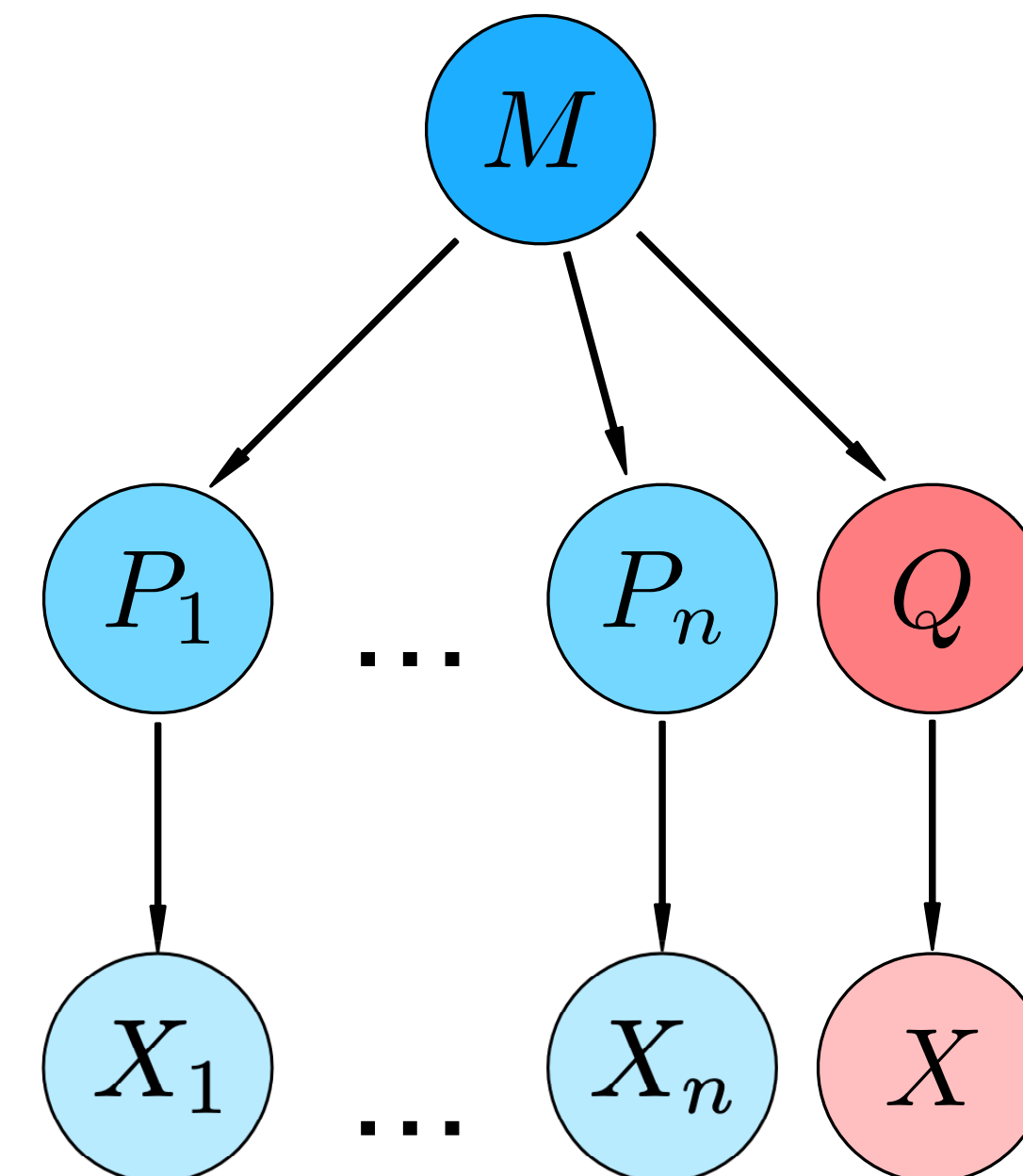
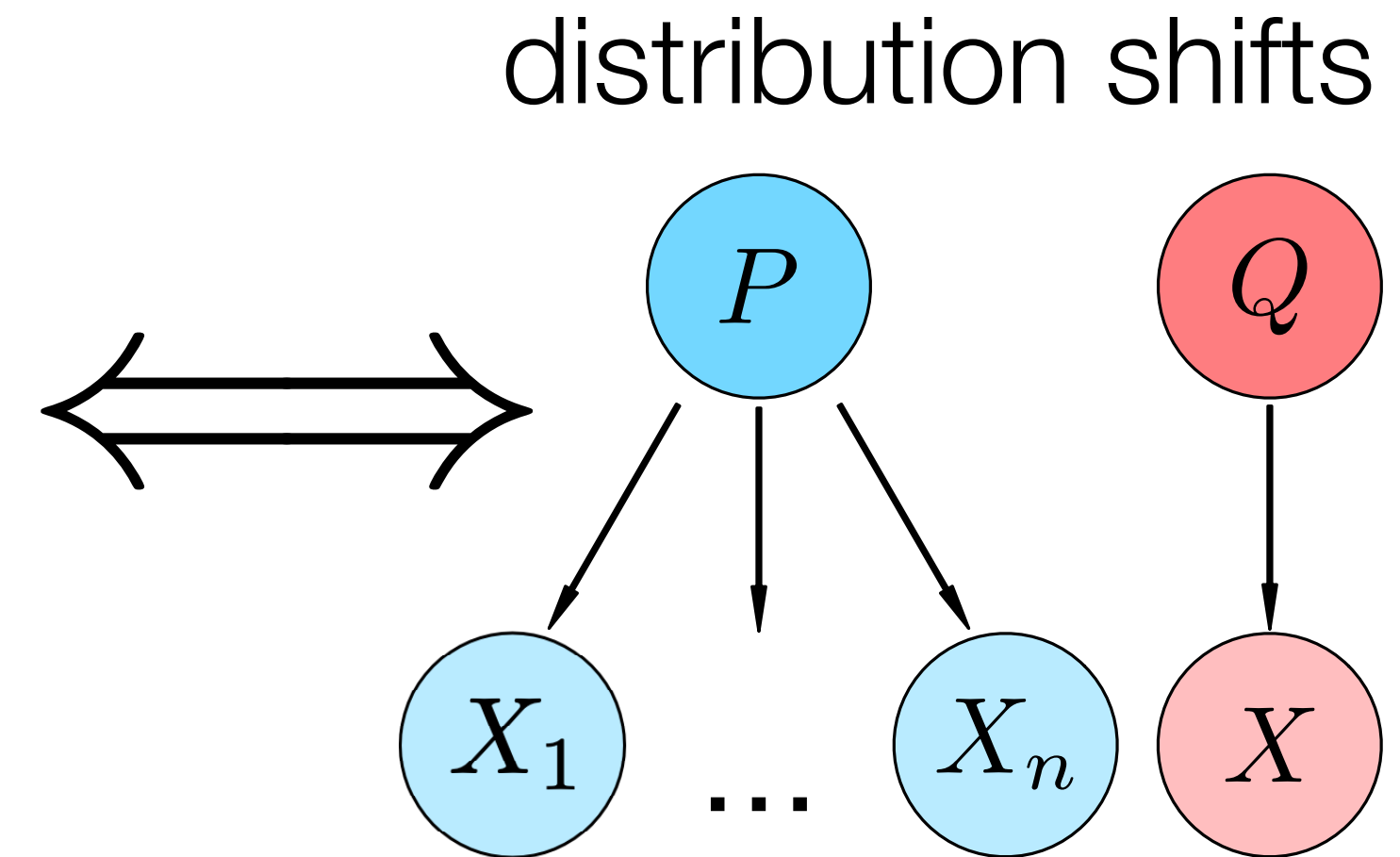
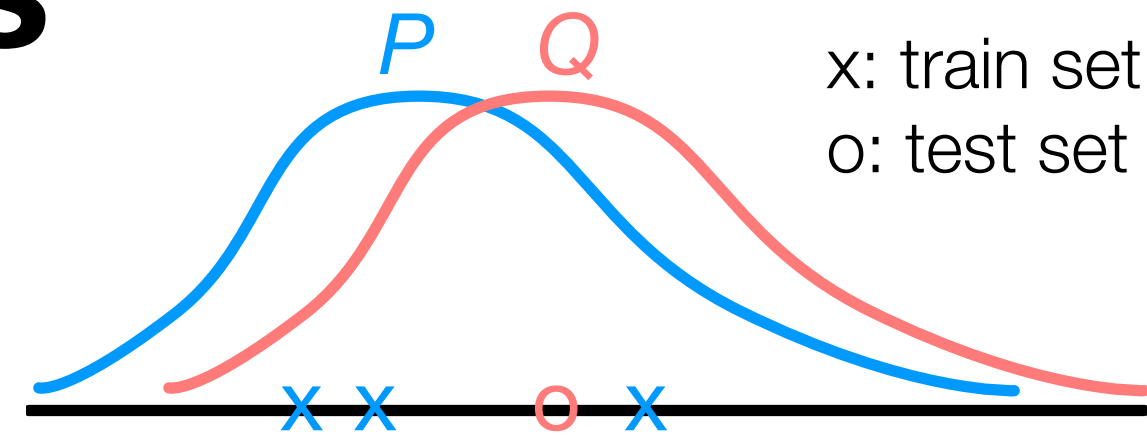
Existing paradigms

- **Domain adaptation**

- Data from the test distribution
- Hard to know the test distribution

- **Domain generalization**

- Data from the meta distribution

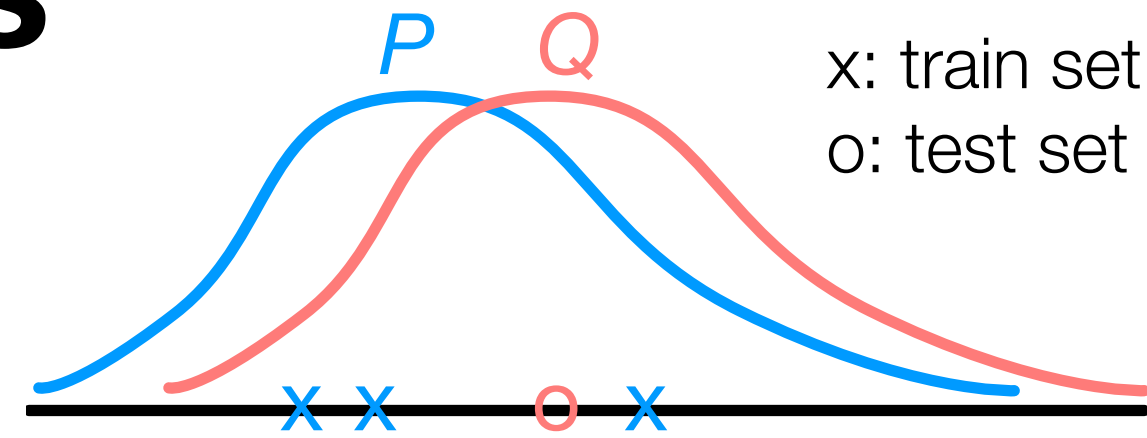


Domain generalization via invariant feature representation
Muandet, Balduzzi and Scholkopf, 2013

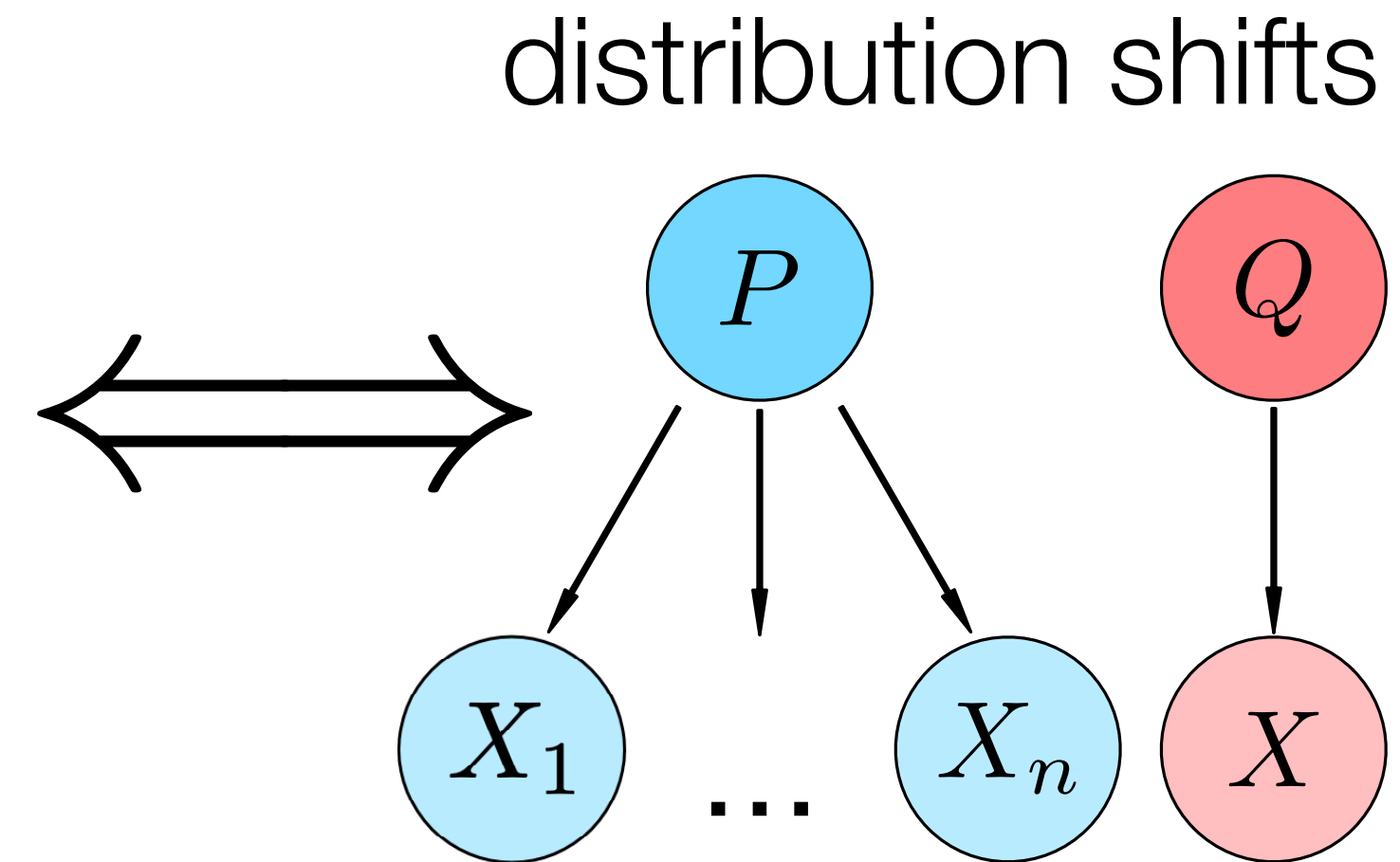
Domain generalization for object recognition with multi-task autoencoders
Ghifary, Bastiaan, Zhang and Balduzzi, 2015

Domain Generalization by Solving Jigsaw Puzzles
Carlucci, D'Innocente, Bucci, Caputo and Tommasi, 2019

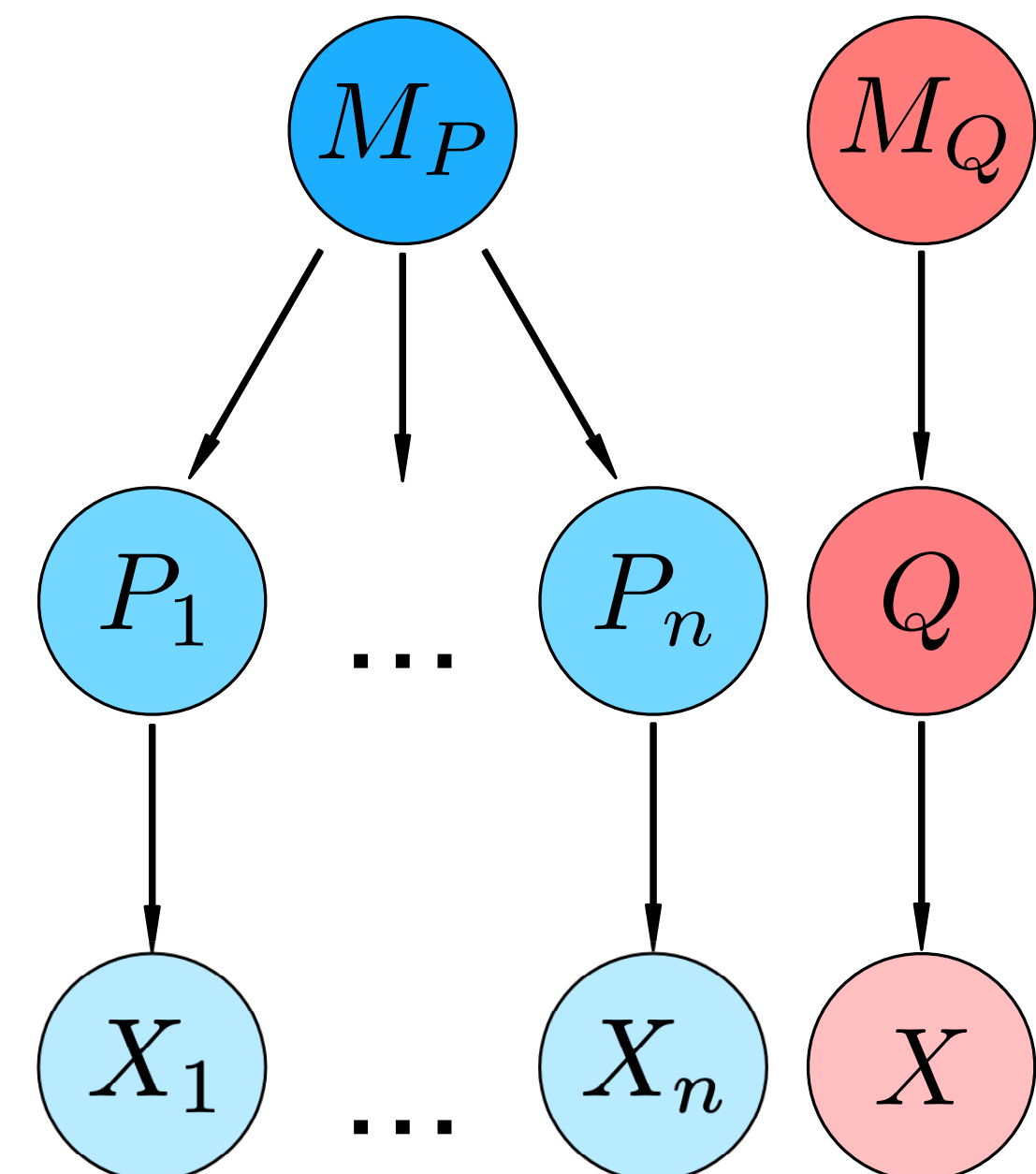
Existing paradigms



- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution



meta distribution shifts



Domain generalization via invariant feature representation
Muandet, Balduzzi and Scholkopf, 2013

Domain generalization for object recognition with multi-task autoencoders
Ghifary, Bastiaan, Zhang and Balduzzi, 2015

Domain Generalization by Solving Jigsaw Puzzles
Carlucci, D'Innocente, Bucci, Caputo and Tommasi, 2019

Existing paradigms

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution
- **Adversarial robustness**
 - Topological structure of the test distribution

Certifying some distributional robustness with principled adversarial training
Sinha, Namkoong and Duchi, 2017

Towards deep learning models resistant to adversarial attacks
Madry, Makelov, Schmidt, Tsipras and Vladu, 2017

Adversarially robust generalization requires more data
Schmidt, Santurkar, Tsipras, Talwar and Madry, 2018

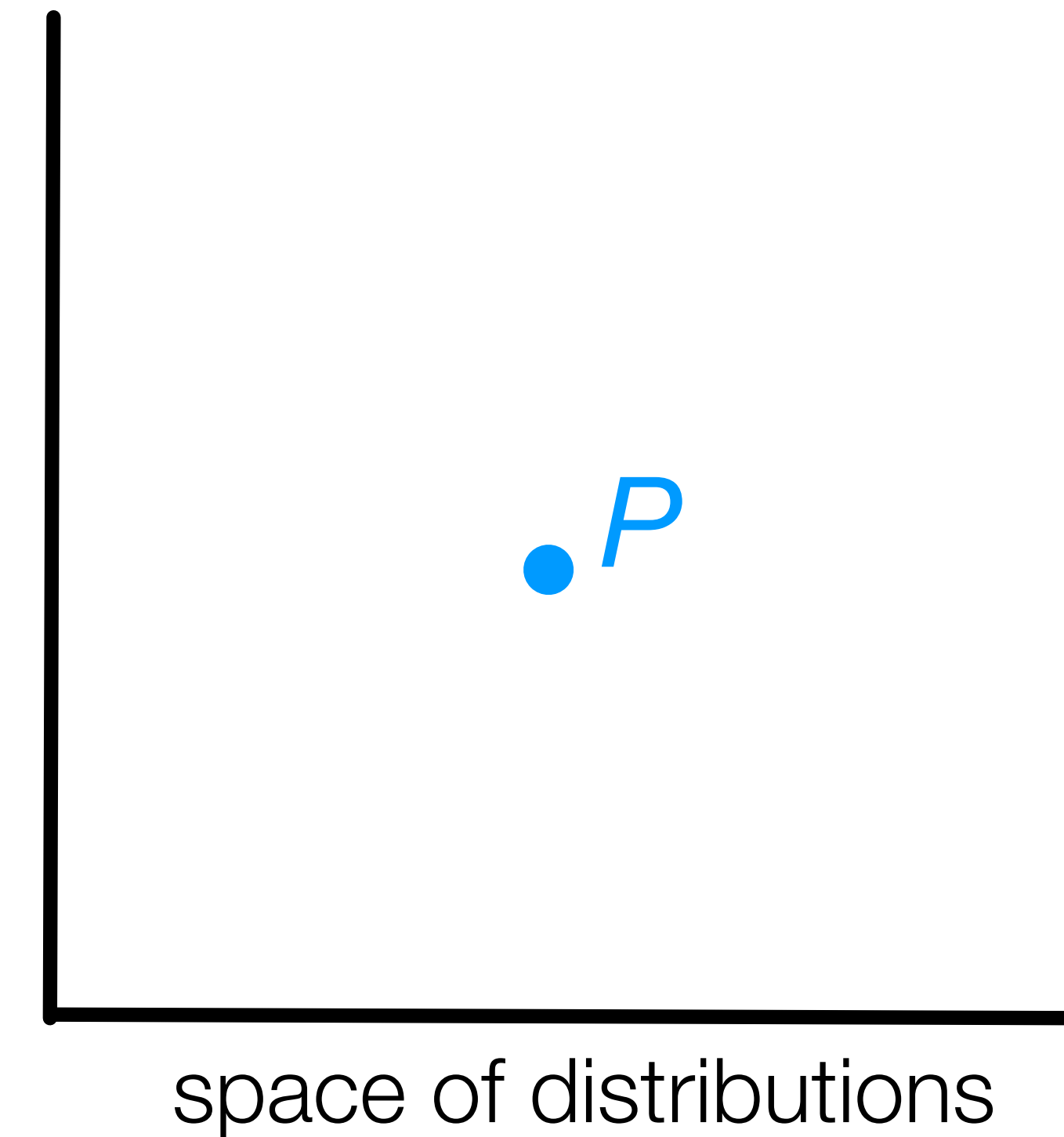
Existing paradigms

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution
- **Adversarial robustness**
 - Topological structure of the test distribution

Certifying some distributional robustness with principled adversarial training
Sinha, Namkoong and Duchi, 2017

Towards deep learning models resistant to adversarial attacks
Madry, Makelov, Schmidt, Tsipras and Vladu, 2017

Adversarially robust generalization requires more data
Schmidt, Santurkar, Tsipras, Talwar and Madry, 2018



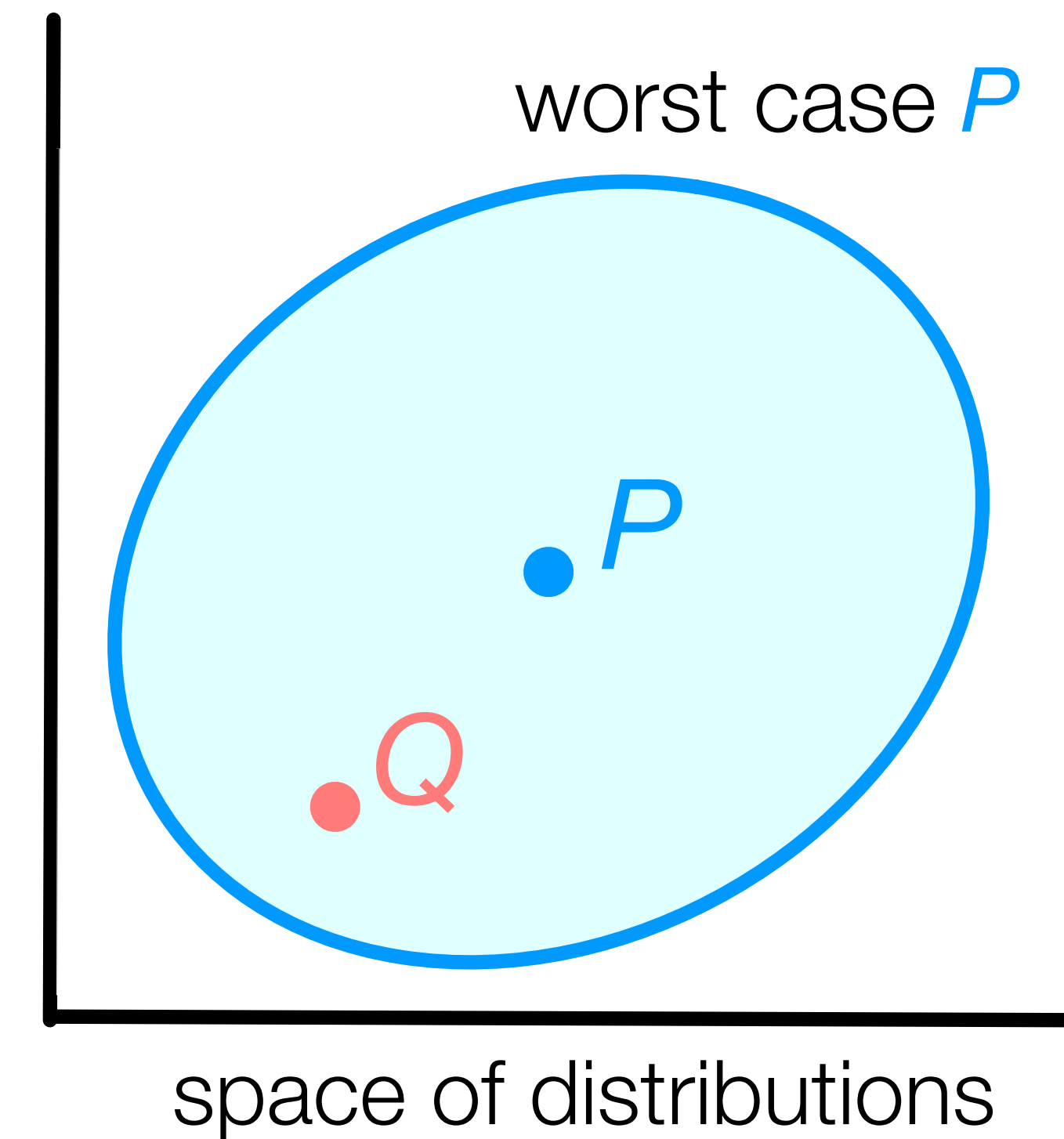
Existing paradigms

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution
- **Adversarial robustness**
 - Topological structure of the test distribution

Certifying some distributional robustness with principled adversarial training
Sinha, Namkoong and Duchi, 2017

Towards deep learning models resistant to adversarial attacks
Madry, Makelov, Schmidt, Tsipras and Vladu, 2017

Adversarially robust generalization requires more data
Schmidt, Santurkar, Tsipras, Talwar and Madry, 2018



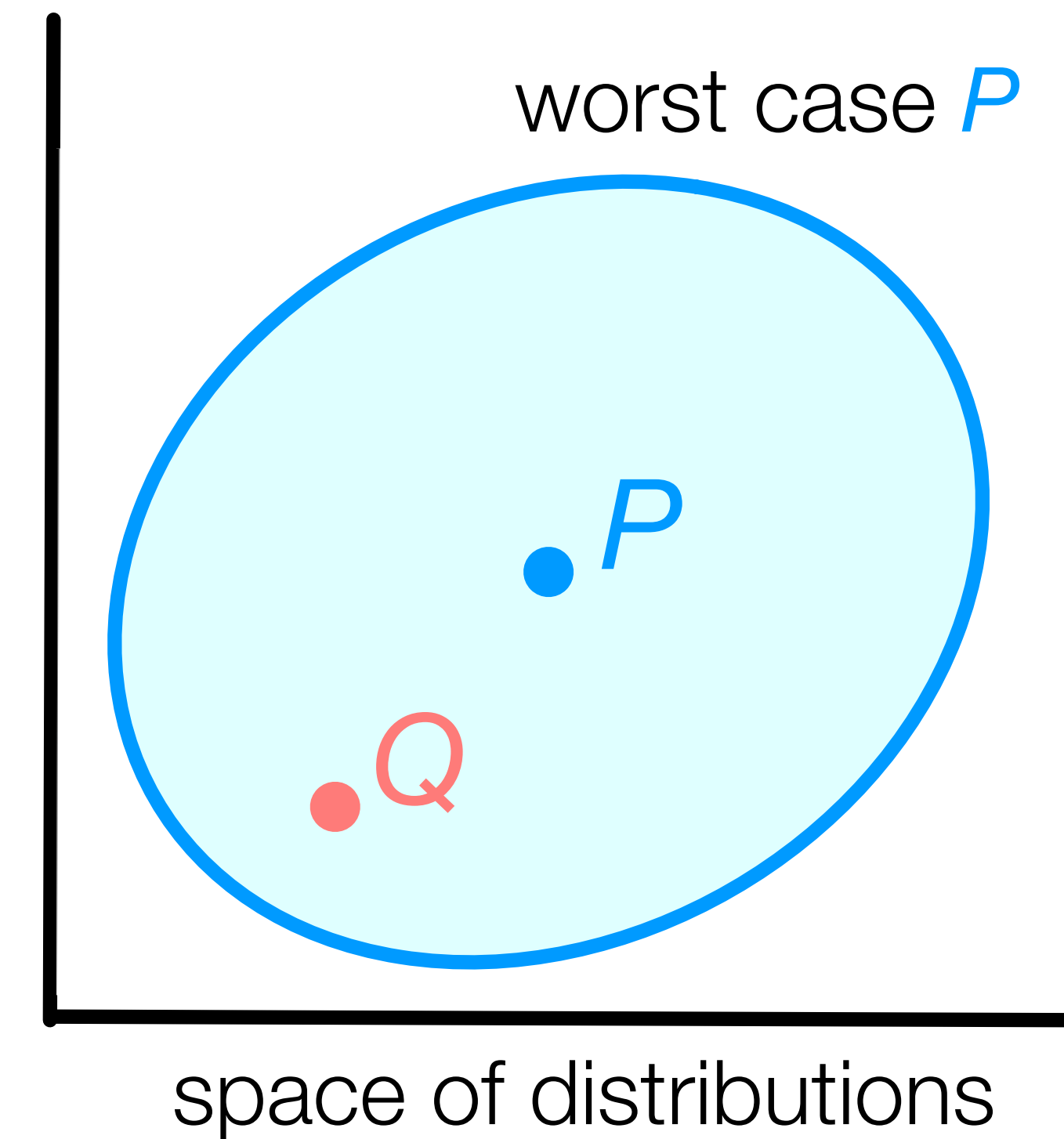
Existing paradigms

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution
- **Adversarial robustness**
 - Topological structure of the test distribution
 - Hard to describe, especially in high dimension

Certifying some distributional robustness with principled adversarial training
Sinha, Namkoong and Duchi, 2017

Towards deep learning models resistant to adversarial attacks
Madry, Makelov, Schmidt, Tsipras and Vladu, 2017

Adversarially robust generalization requires more data
Schmidt, Santurkar, Tsipras, Talwar and Madry, 2018



Existing paradigms **anticipate** the distribution shifts

- **Domain adaptation**
 - Data from the test distribution
 - Hard to know the test distribution
- **Domain generalization**
 - Data from the meta distribution
 - Hard to know the meta distribution
- **Adversarial robustness**
 - Topological structure of the test distribution
 - Hard to describe, especially in high dimension

Test-Time Training (TTT)

- Does not anticipate the test distribution

Test-Time Training (TTT)

$$\text{standard test error} = \mathbb{E}_Q[\ell(x, y); \theta]$$

- Does not anticipate the test distribution
- The test sample x gives us a hint about Q

Test-Time Training (TTT)

$$\text{standard test error} = \mathbb{E}_Q[\ell(x, y); \theta]$$

$$\text{our test error} = \mathbb{E}_Q[\ell(x, y); \theta(x)]$$

- Does not anticipate the test distribution
- The test sample x gives us a hint about Q
- No fixed model, but adapt at test time

Test-Time Training (TTT)

$$\text{standard test error} = \mathbb{E}_Q[\ell(x, y); \theta]$$

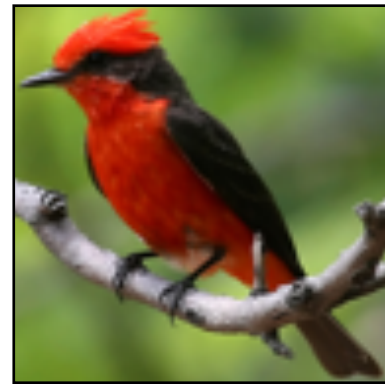
$$\text{our test error} = \mathbb{E}_Q[\ell(x, y); \theta(x)]$$

- Does not anticipate the test distribution
- The test sample x gives us a hint about Q
- No fixed model, but adapt at test time
- One sample learning problem
- No label? Self-supervision!

Rotation prediction as self-supervision

(Gidaris et al. 2018)

x



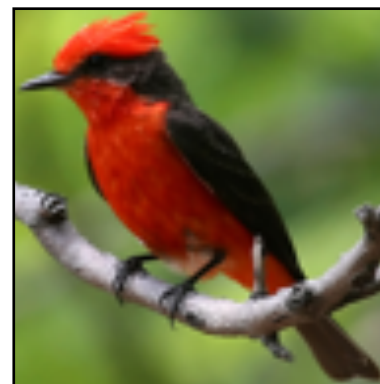
- Create labels from unlabeled input

Rotation prediction as self-supervision

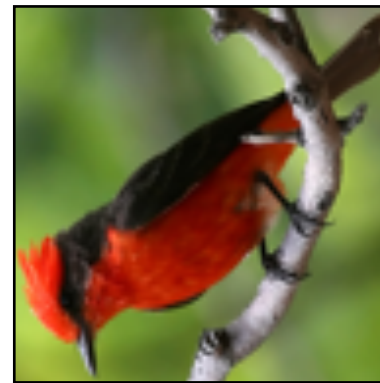
(Gidaris et al. 2018)

x

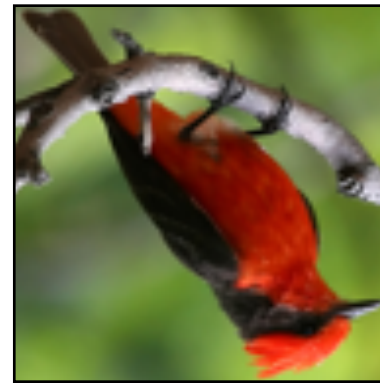
y_s



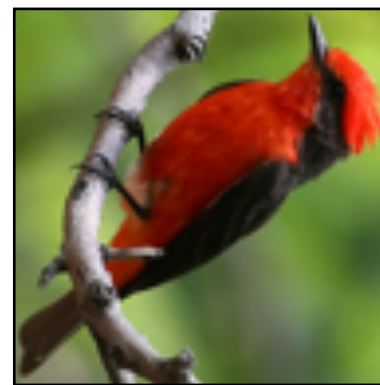
0°



90°



180°



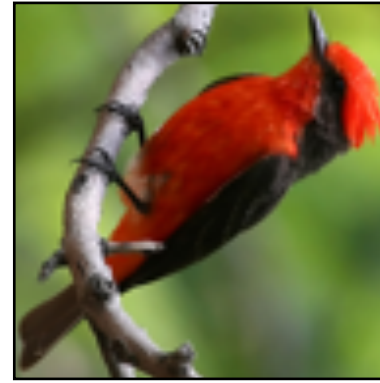
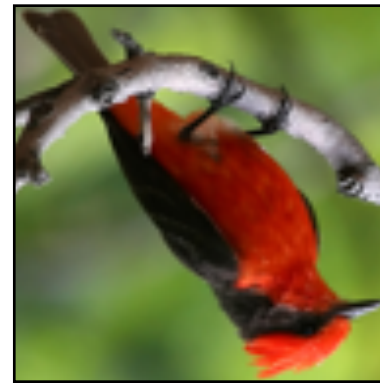
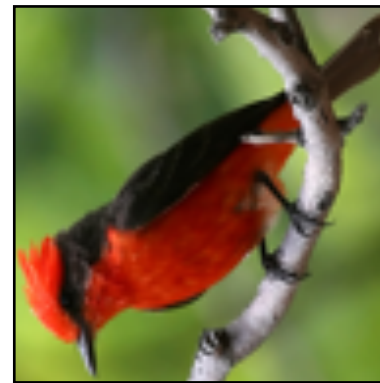
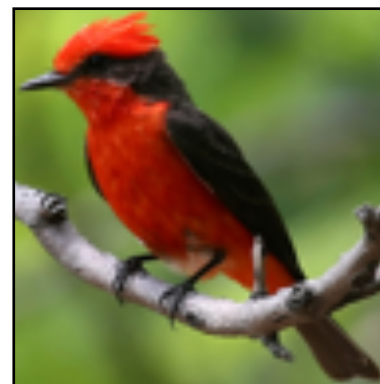
270°

- Create labels from unlabeled input
- Rotate input image by multiples of 90°

Rotation prediction as self-supervision

(Gidaris et al. 2018)

x



CNN

θ

y_s

0°

90°

180°

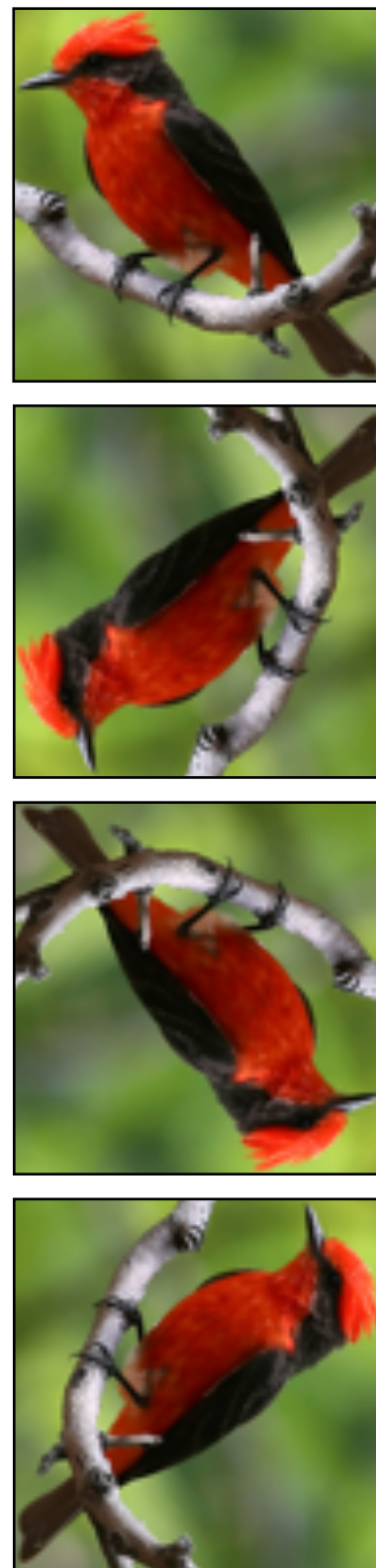
270°

- Create labels from unlabeled input
- Rotate input image by multiples of 90°
- Produce a four-way classification problem

Rotation prediction as self-supervision

(Gidaris et al. 2018)

x



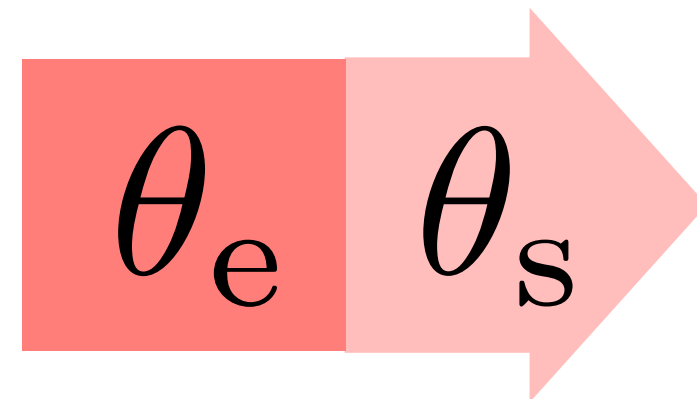
y_s

0°

90°

180°

270°



- Create labels from unlabeled input
- Rotate input image by multiples of 90°
- Produce a four-way classification problem
- Usually a pre-training step

Rotation prediction as self-supervision

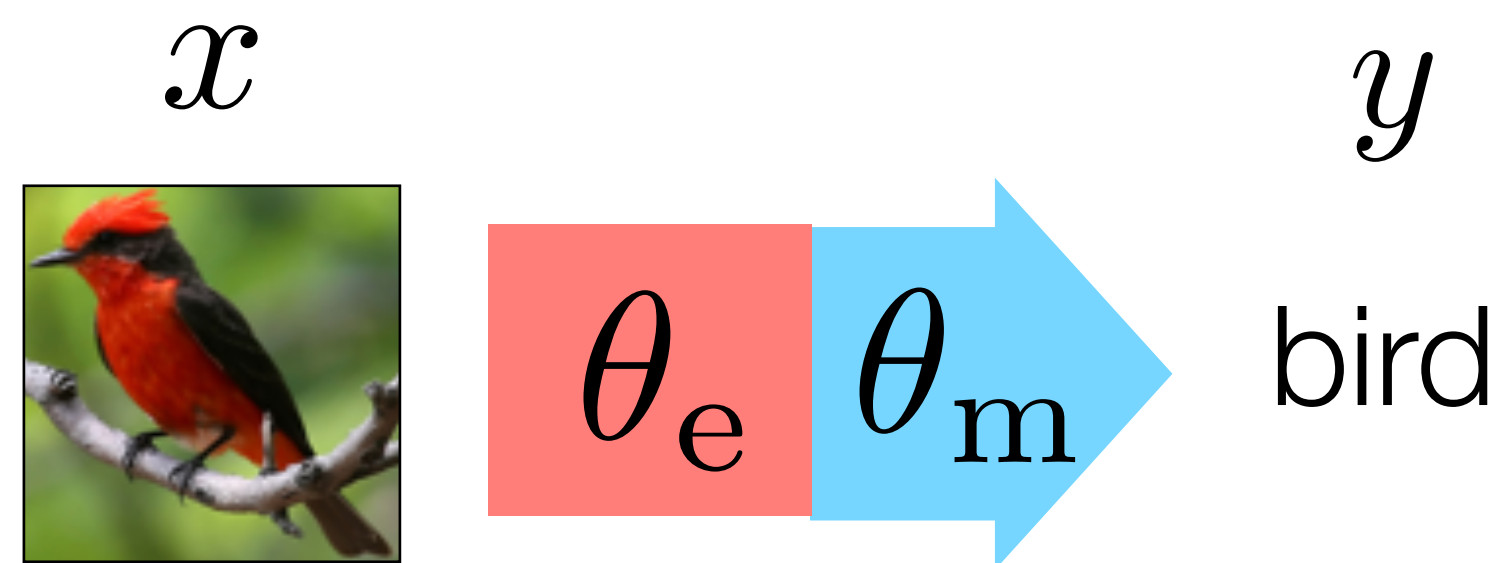
(Gidaris et al. 2018)



- Create labels from unlabeled input
- Rotate input image by multiples of 90°
- Produce a four-way classification problem
- Usually a pre-training step
 - After training, take feature extractor

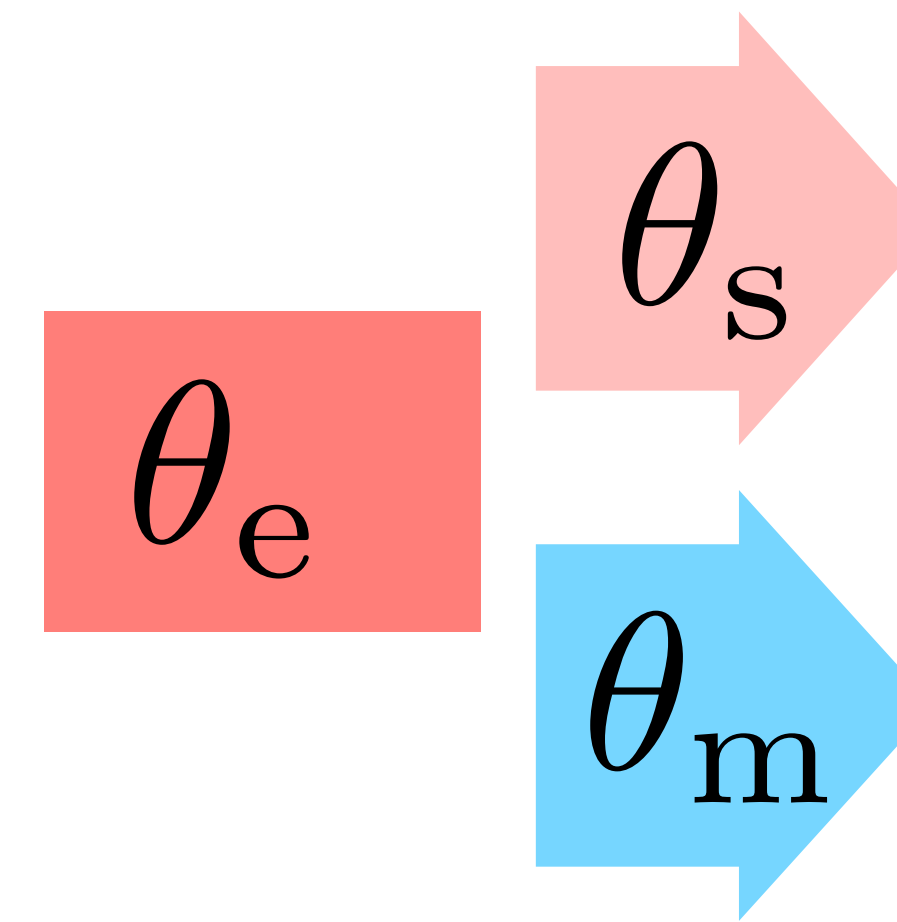
Rotation prediction as self-supervision

(Gidaris et al. 2018)



- Create labels from unlabeled input
- Rotate input image by multiples of 90°
- Produce a four-way classification problem
- Usually a pre-training step
 - After training, take feature extractor
 - Use it for a downstream main task

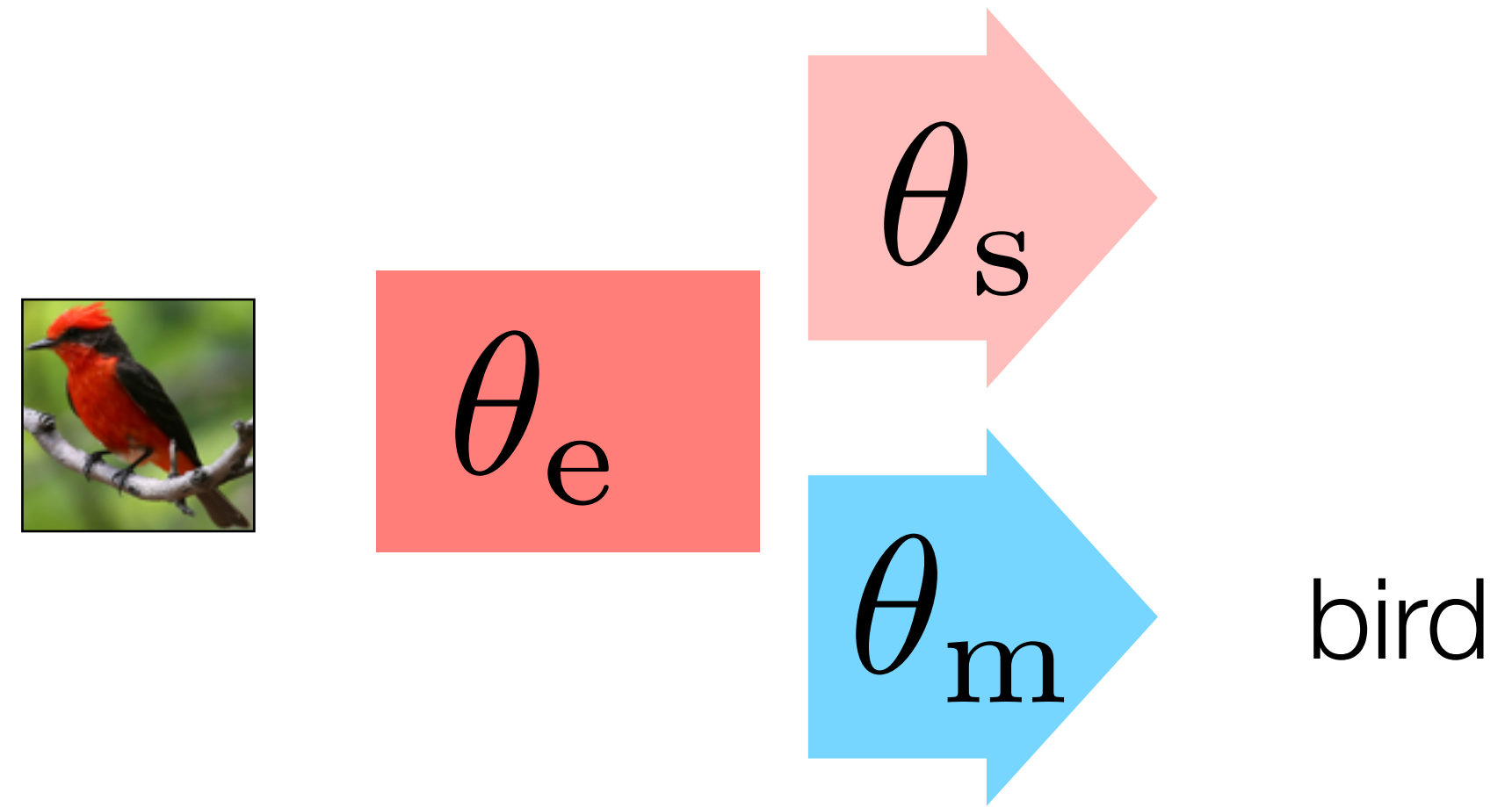
Algorithm for TTT



network
architecture

Algorithm for TTT

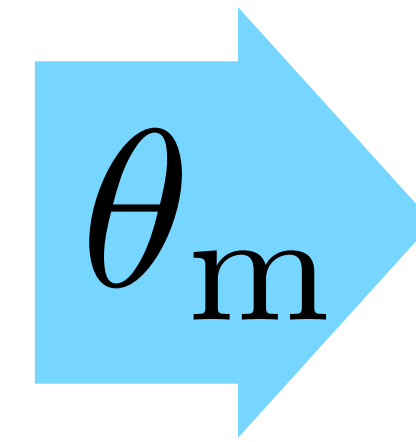
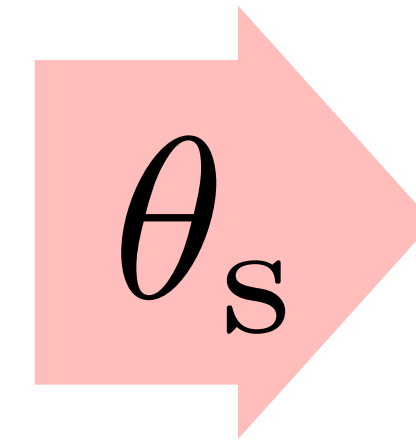
training



Algorithm for TTT

training

$$l_m(x, y; \theta_e, \theta_m)$$

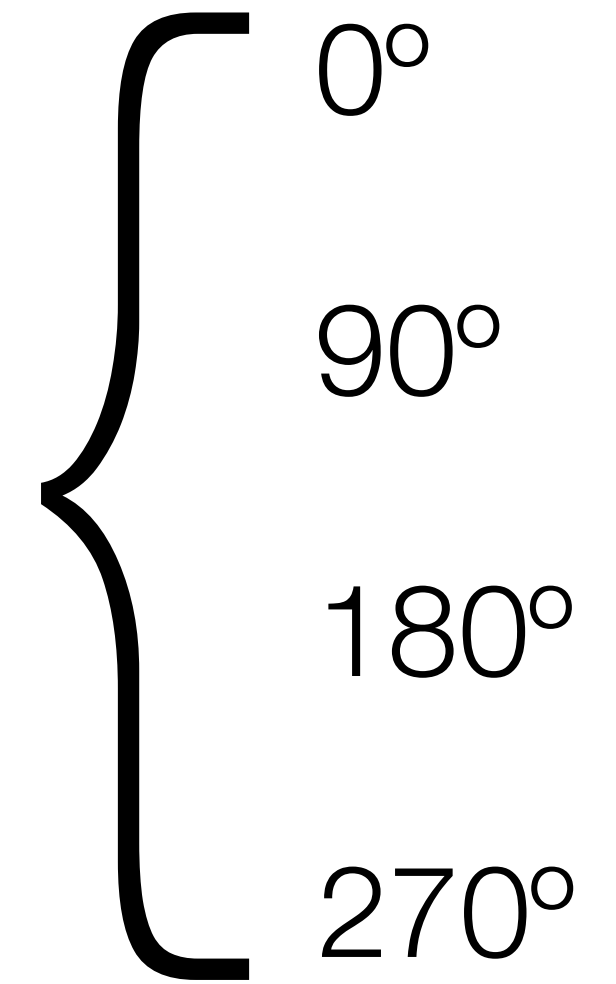
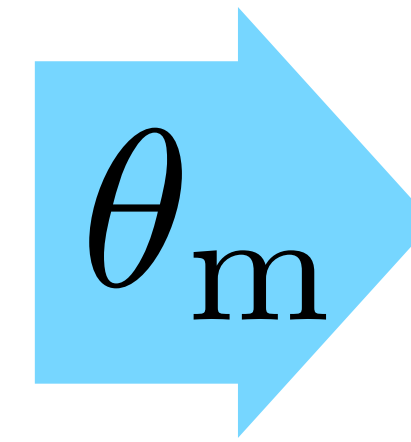
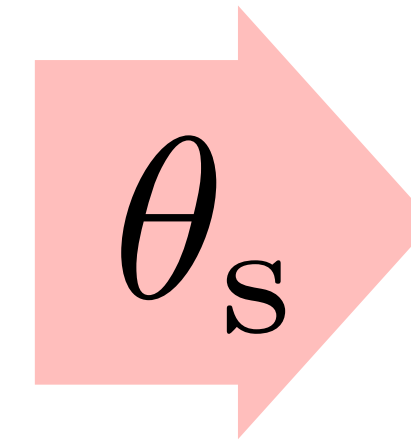
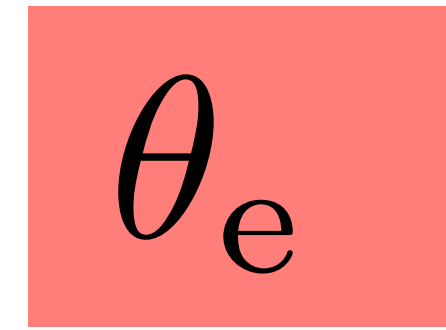
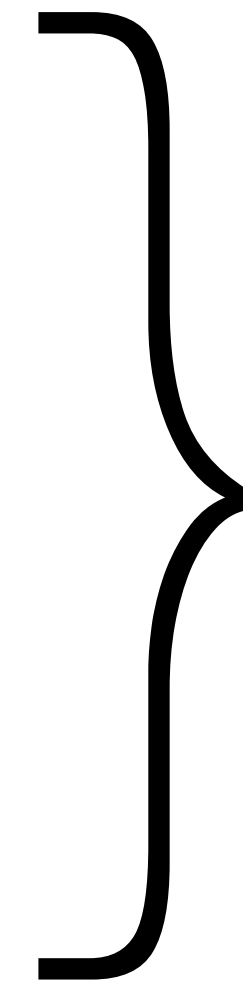
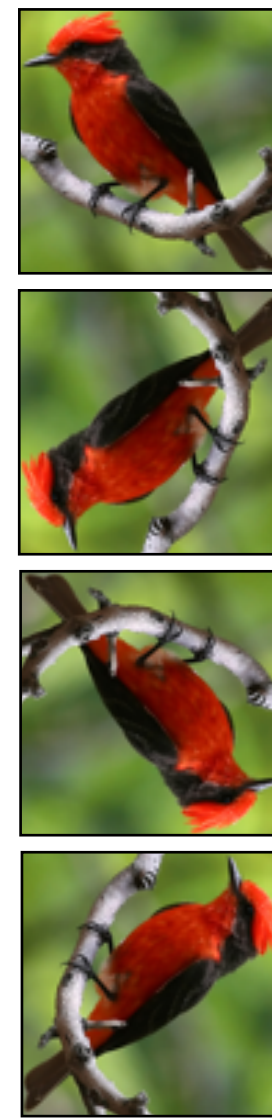


bird

Algorithm for TTT

training

$$l_m(x, y; \theta_e, \theta_m)$$

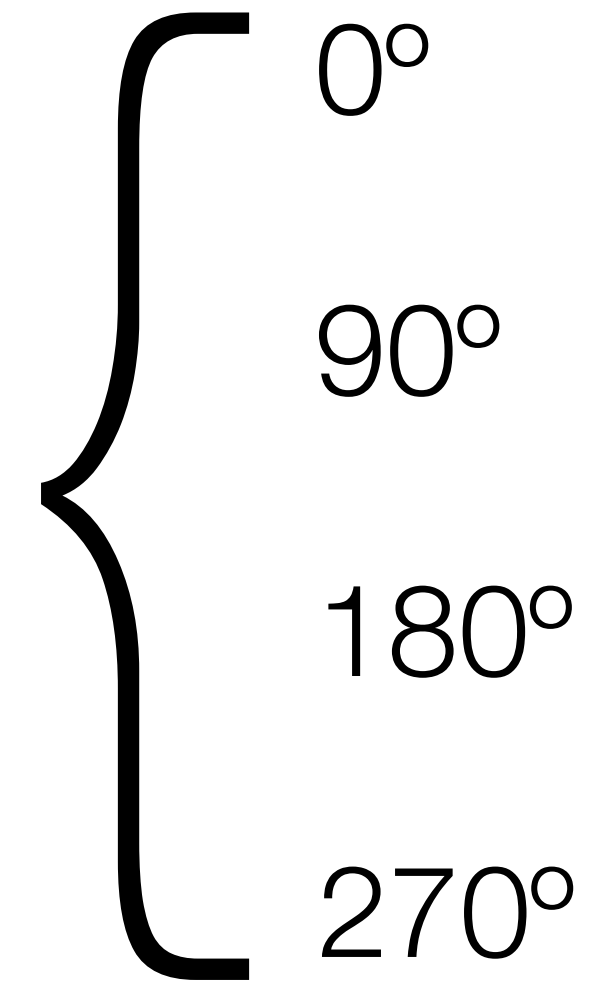
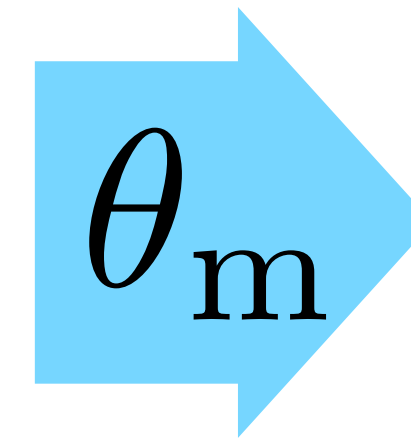
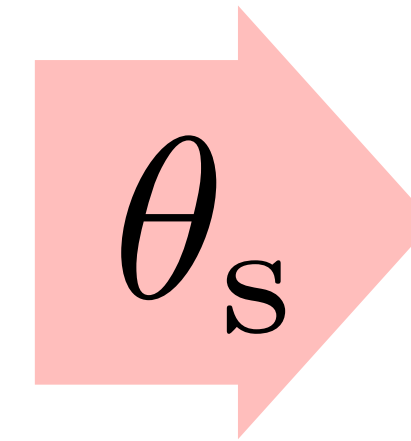
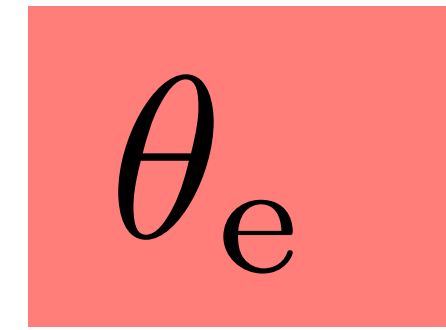
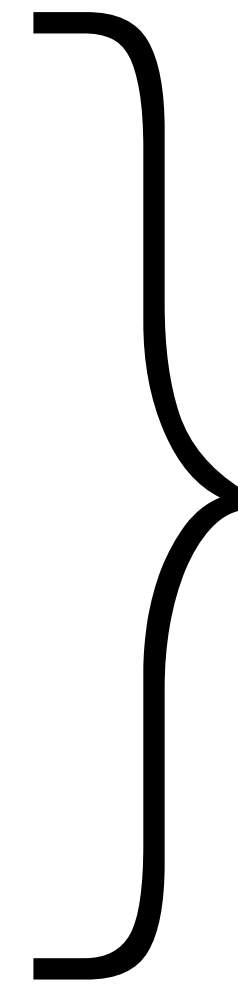
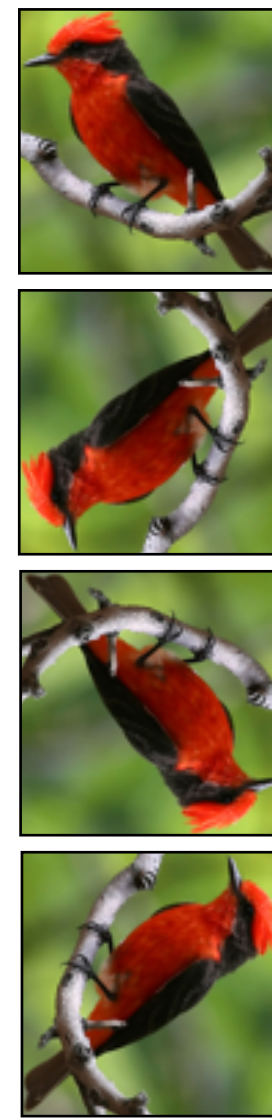


Algorithm for TTT

training

$$l_m(x, y; \theta_e, \theta_m)$$

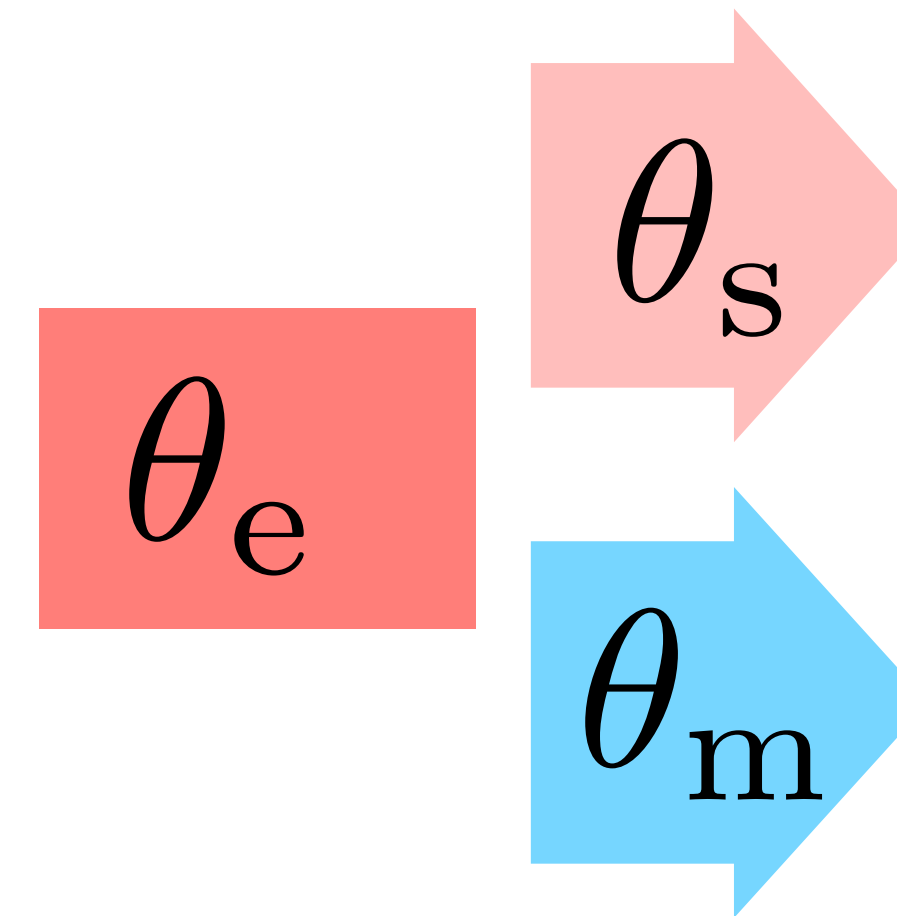
$$+ l_s(x, y_s; \theta_e, \theta_s)$$



Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

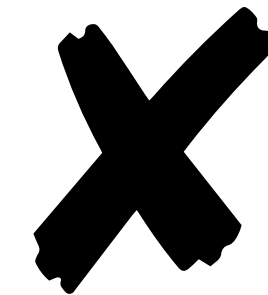
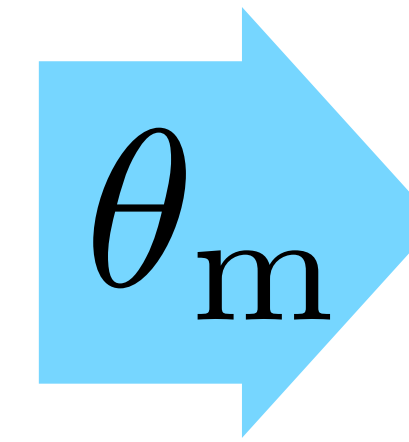
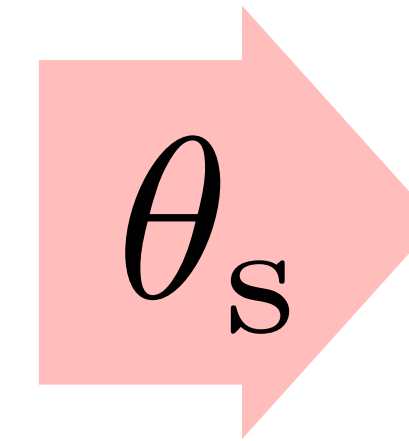
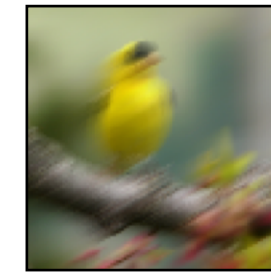


Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

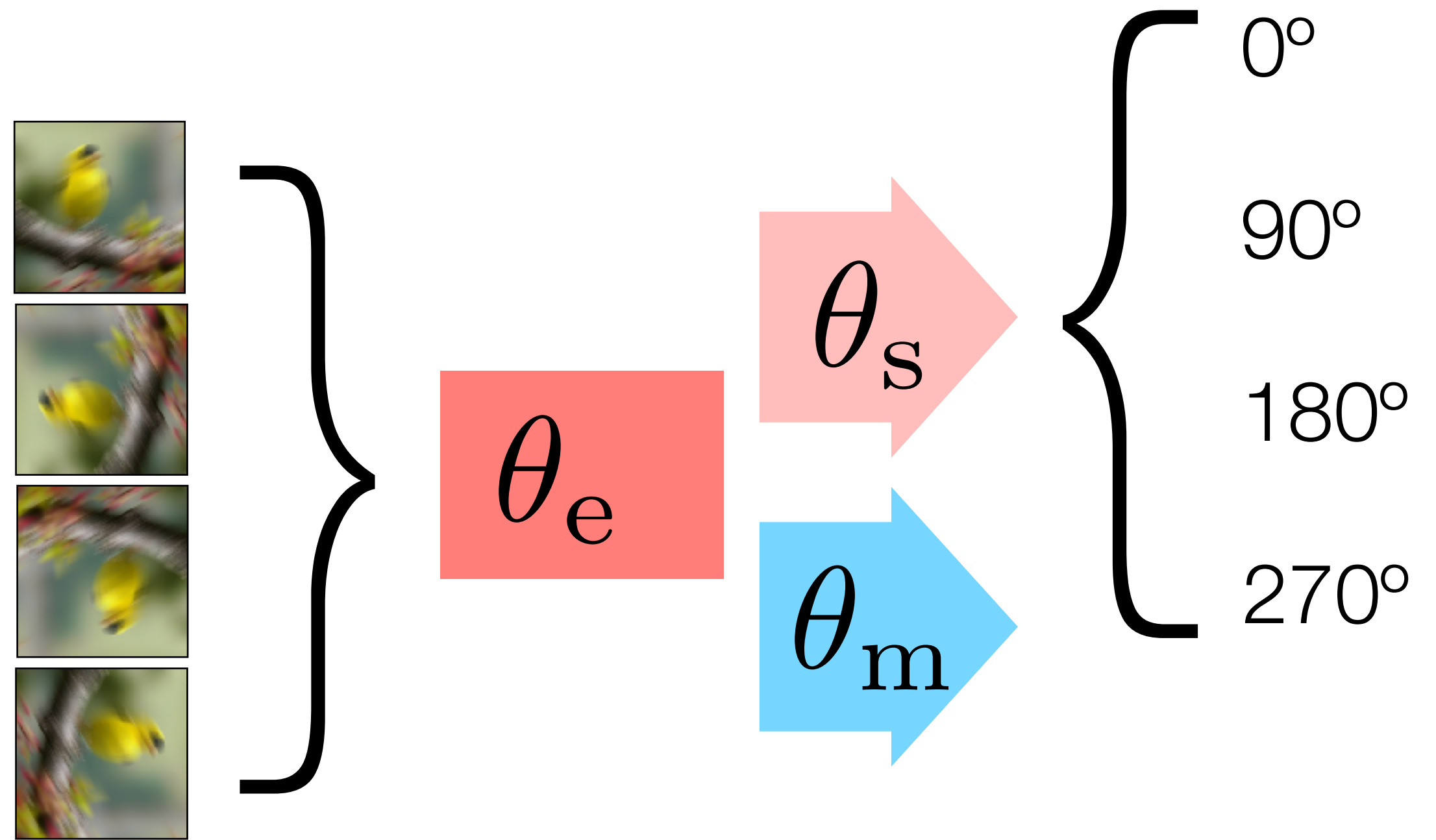
testing



Algorithm for TTT

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \text{training} \\ \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing



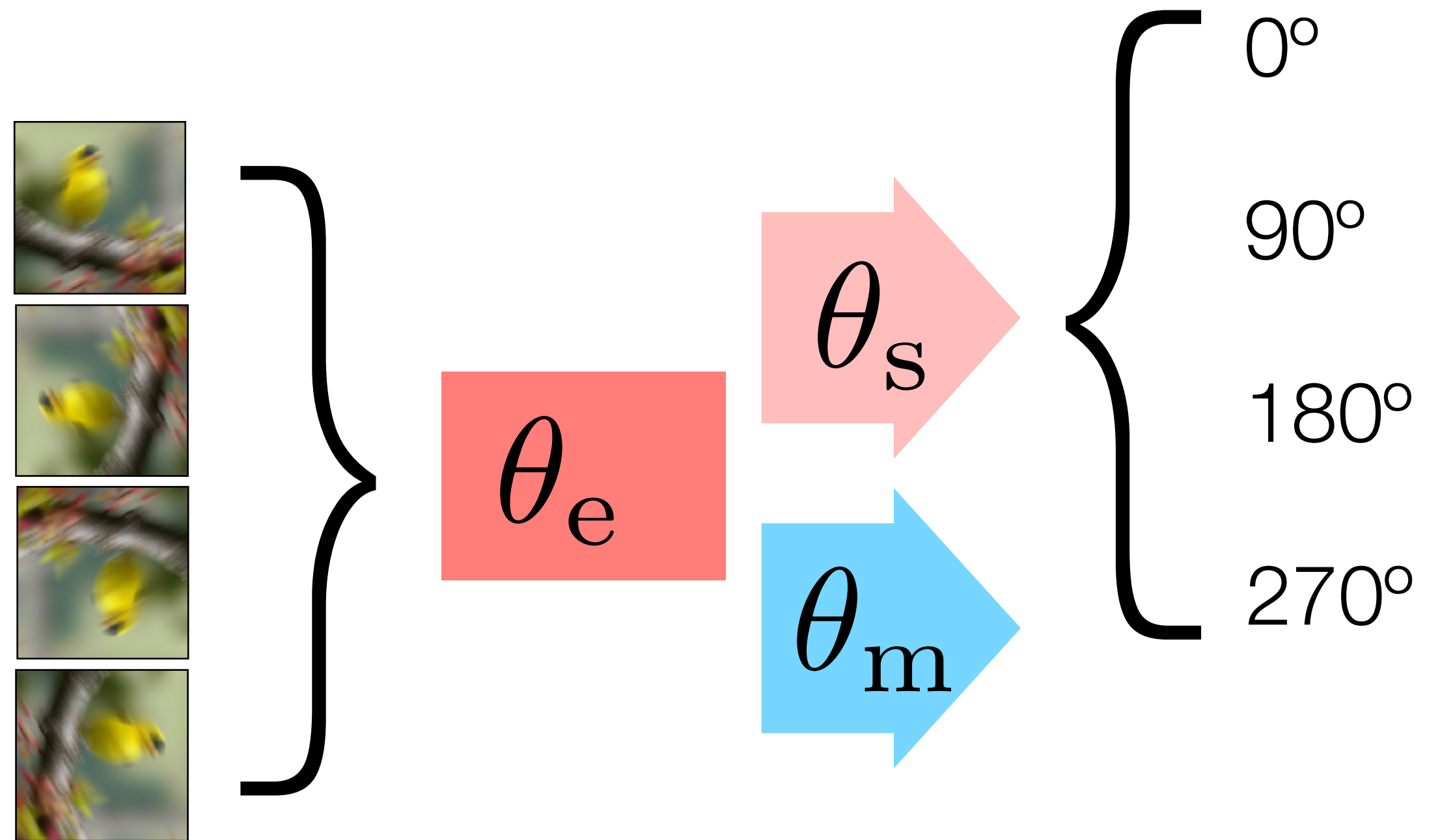
Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing

$$\min_{\theta_e, \theta_s} \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$



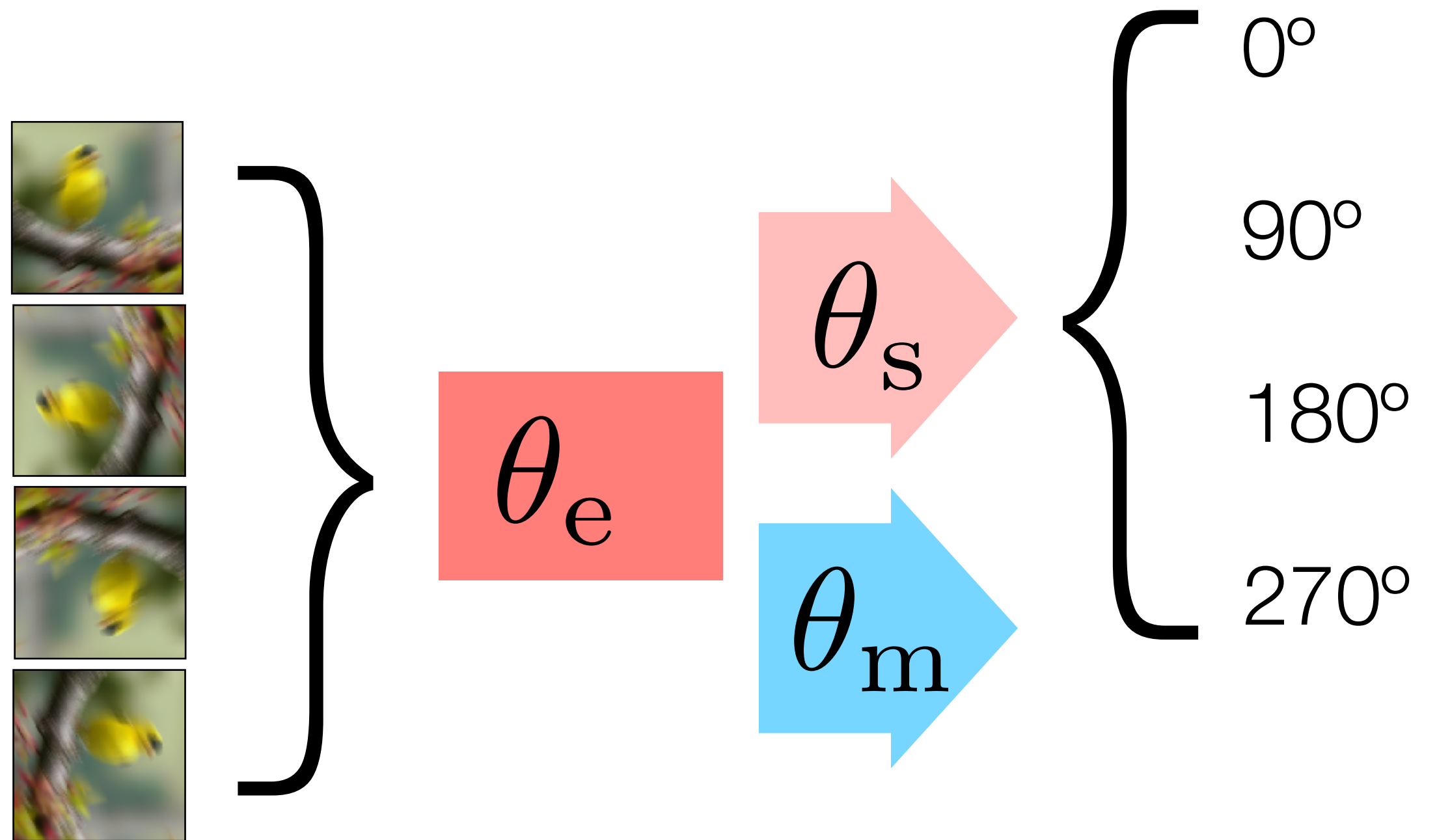
Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{aligned} & \ell_m(x, y; \theta_e, \theta_m) \\ & + \ell_s(x, y_s; \theta_e, \theta_s) \end{aligned} \right]$$

testing

$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$



Algorithm for TTT

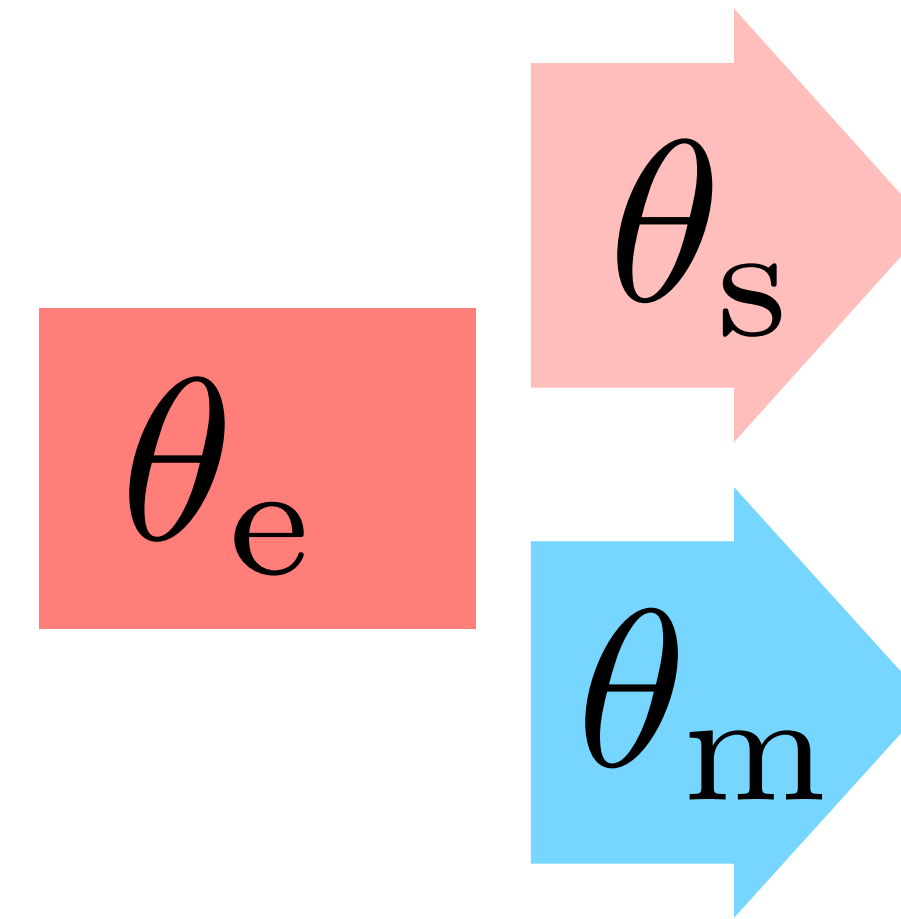
training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing

$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$

→ $\theta(x)$: make prediction on x



Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing

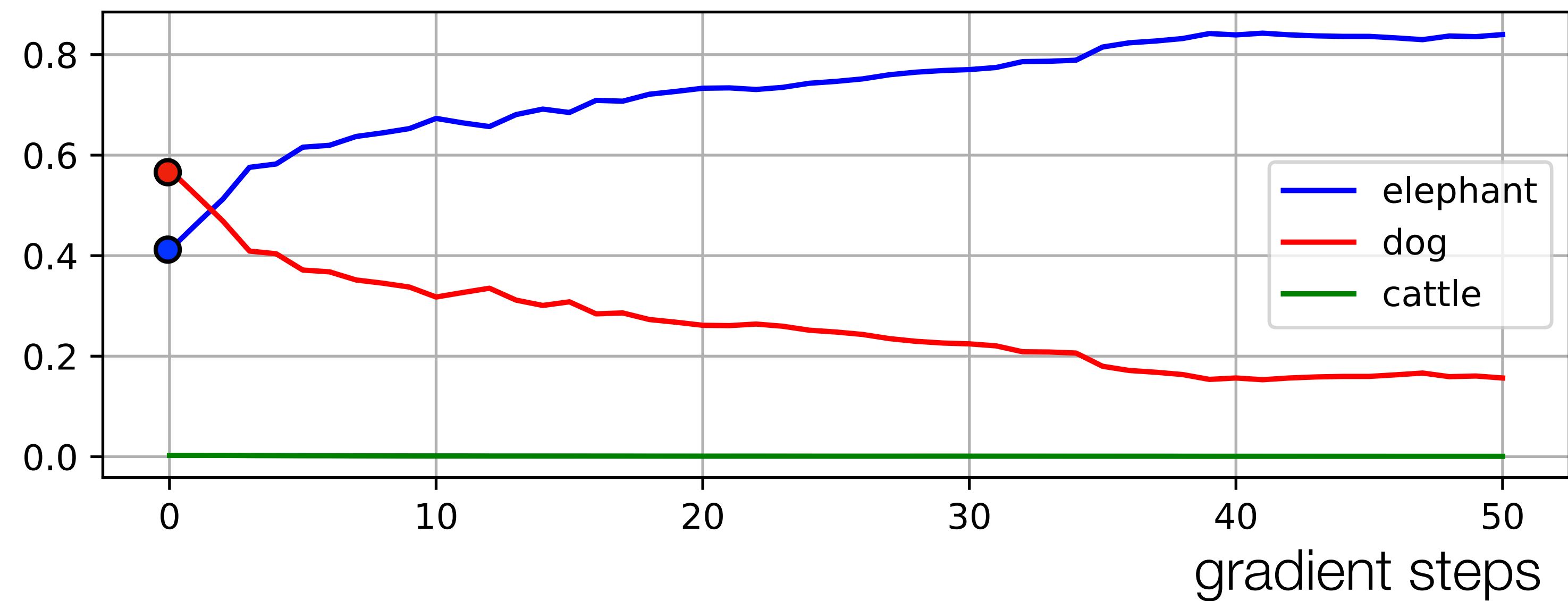
$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$

→ $\theta(x)$: make prediction on x

elephant



likelihood



Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

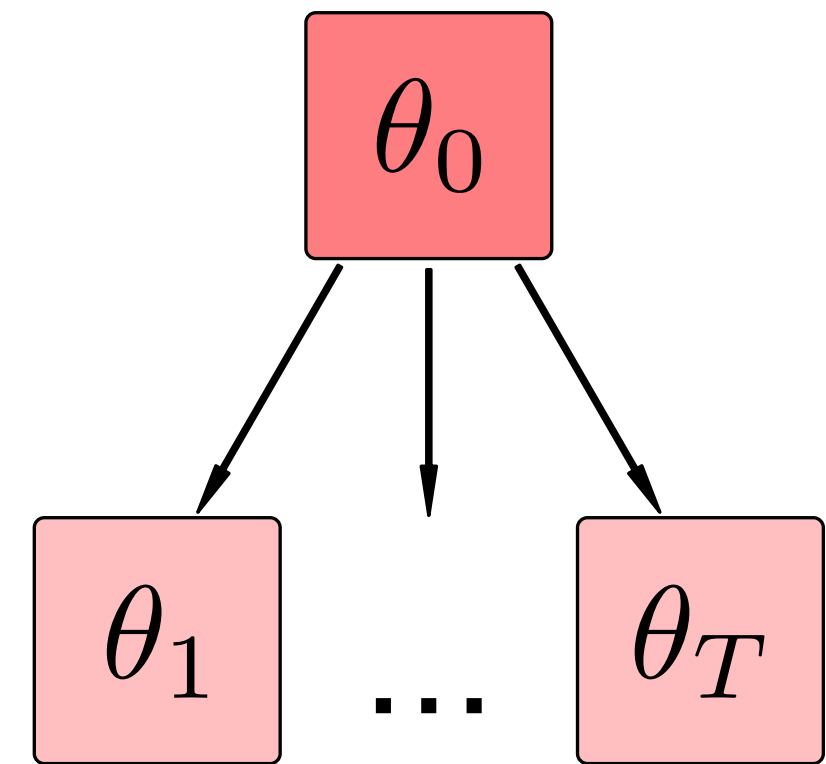
testing

$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$

→ $\theta(x)$: make prediction on x

multiple test samples x_1, \dots, x_T

θ_0 : parameters after joint training



Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing

$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$

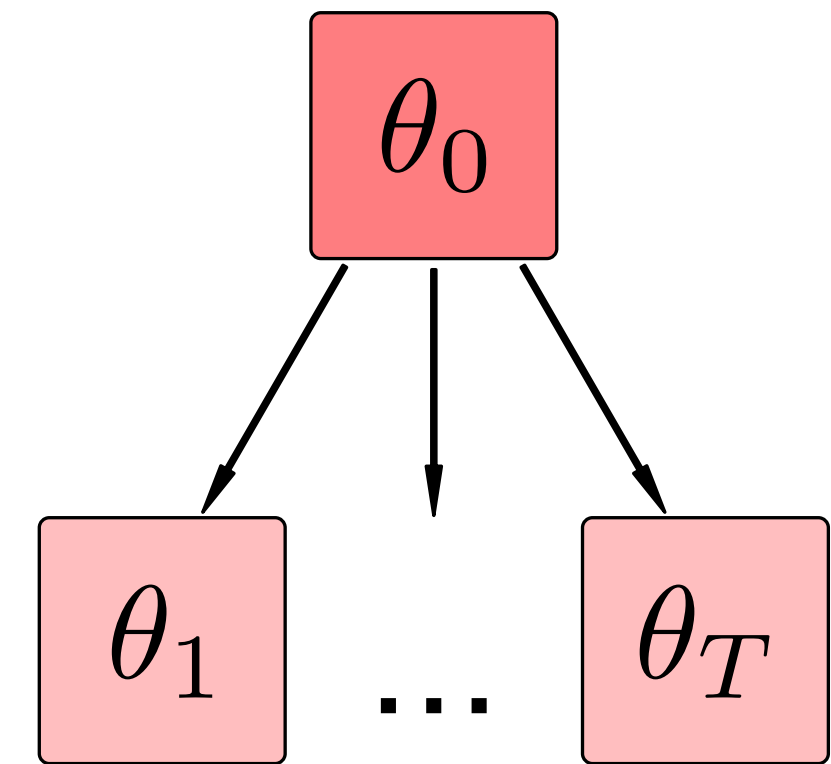
→ $\theta(x)$: make prediction on x

multiple test samples x_1, \dots, x_T

θ_0 : parameters after joint training

standard version

no assumption on
the test samples



Algorithm for TTT

training

$$\min_{\theta_e, \theta_s, \theta_m} \mathbb{E}_P \left[\begin{array}{l} \ell_m(x, y; \theta_e, \theta_m) \\ + \ell_s(x, y_s; \theta_e, \theta_s) \end{array} \right]$$

testing

$$\min_{\theta_e, \theta_s} \mathbb{E}_Q \left[\ell_s(x, y_s; \theta_e, \theta_s) \right]$$

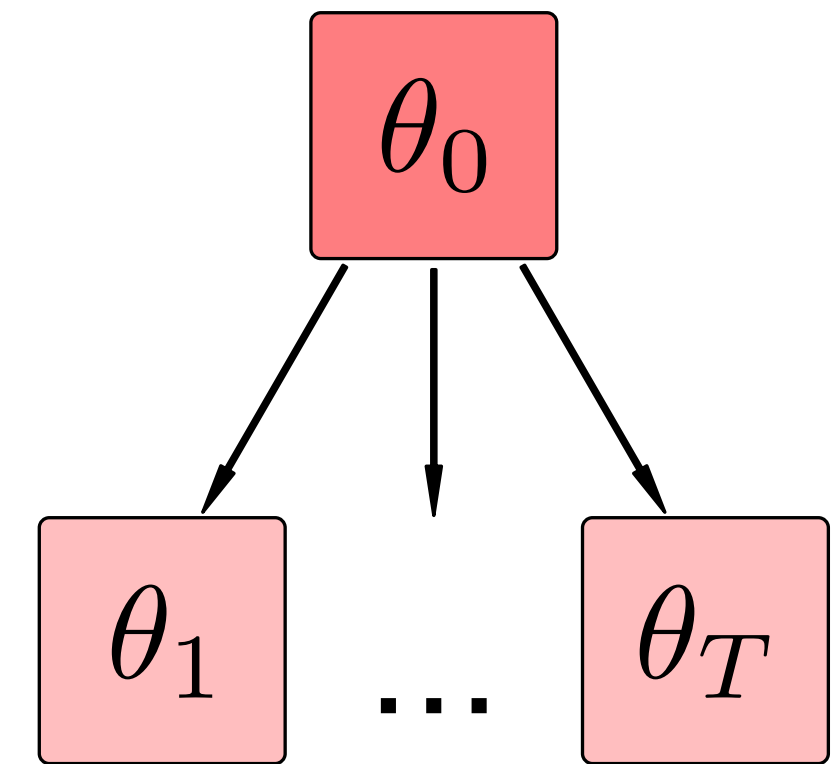
→ $\theta(x)$: make prediction on x

multiple test samples x_1, \dots, x_T

θ_0 : parameters after joint training

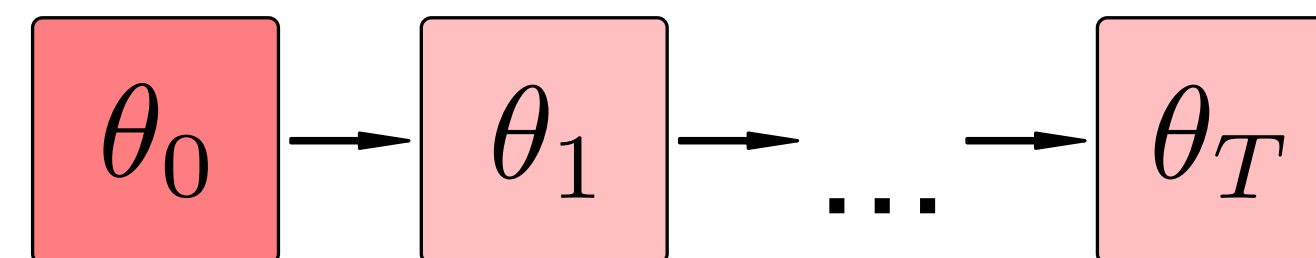
standard version

no assumption on
the test samples



online version

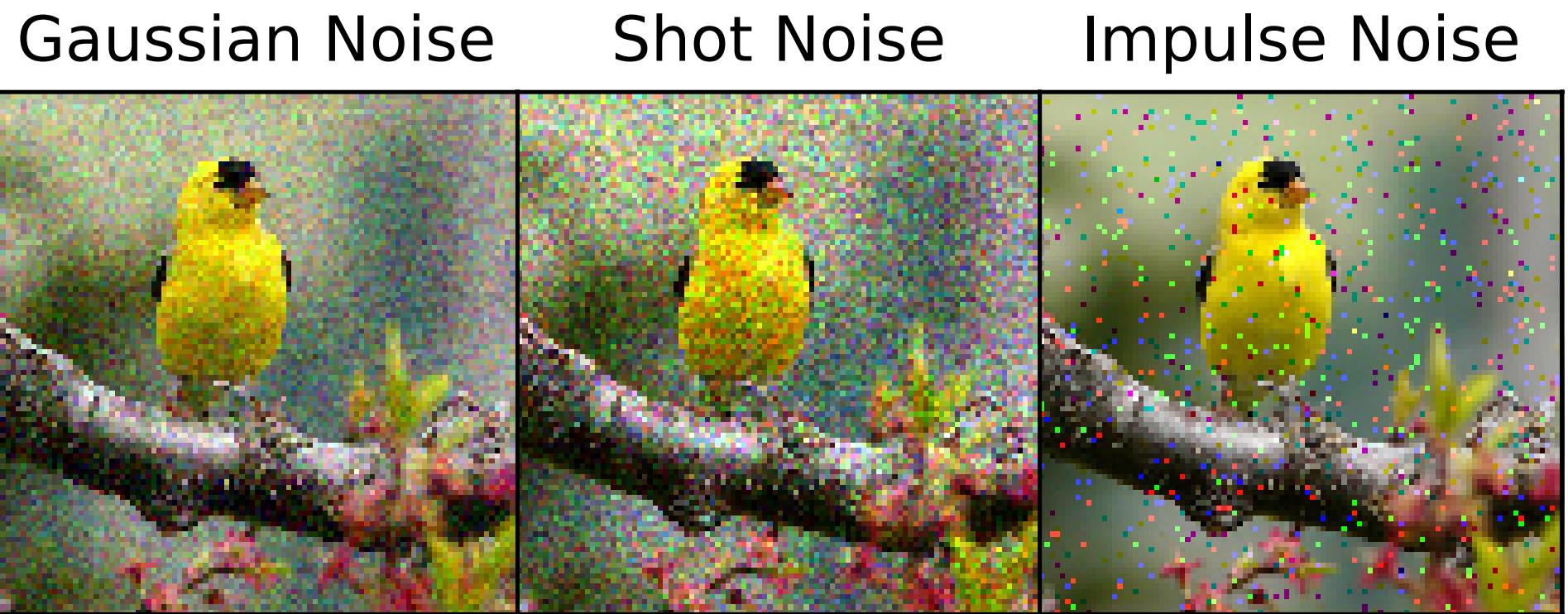
x_1, \dots, x_T come from the same Q
or smoothly changing Q_1, \dots, Q_T



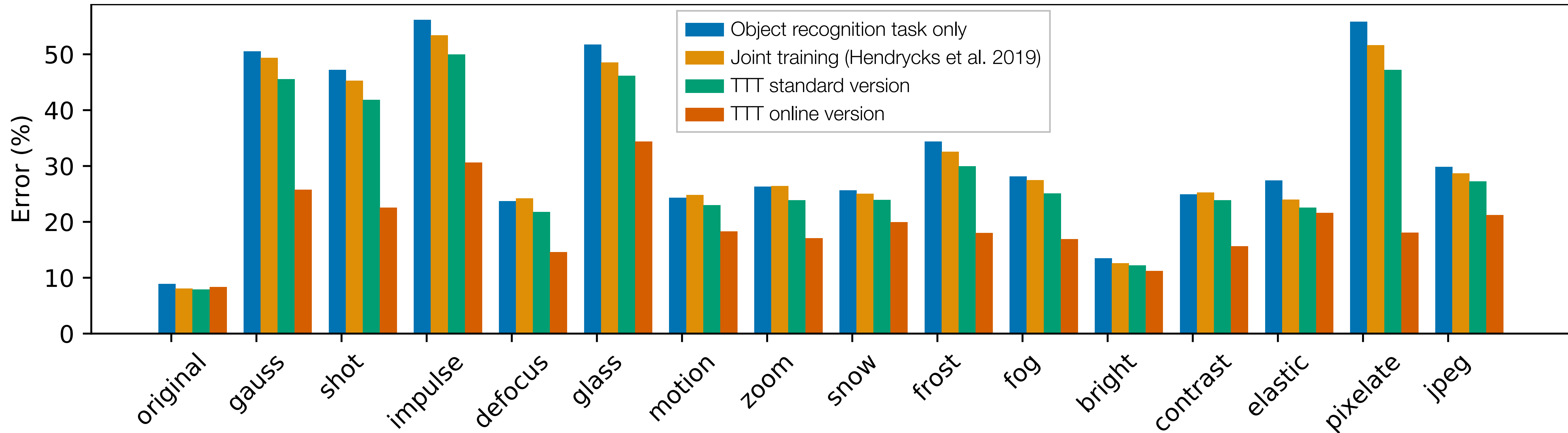
Results

Object recognition with corruptions

- 15 corruptions
- CIFAR-10: 10 classes
- ImageNet: 1000 classes
- No knowledge of the corruptions during training



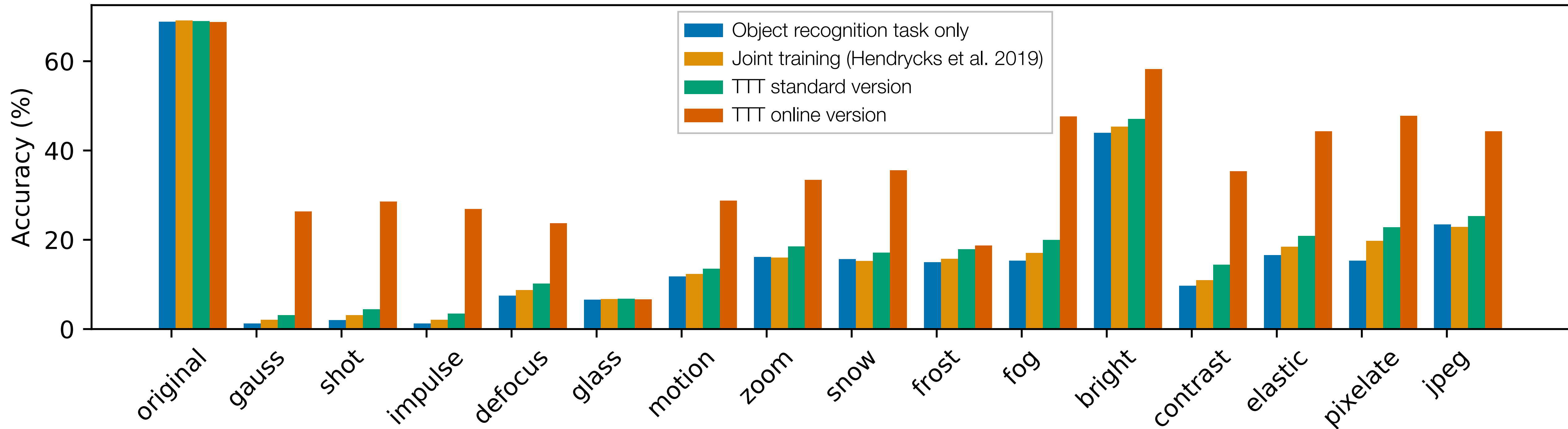
Results on CIFAR-10-C



Joint training reported here is our improved implementation of their method. Please see our paper for clarification, and their paper for their original results.

Using Self-Supervised Learning Can Improve Model Robustness and Uncertainty
Hendrycks, Mazeika, Kadavath and Song, 2019

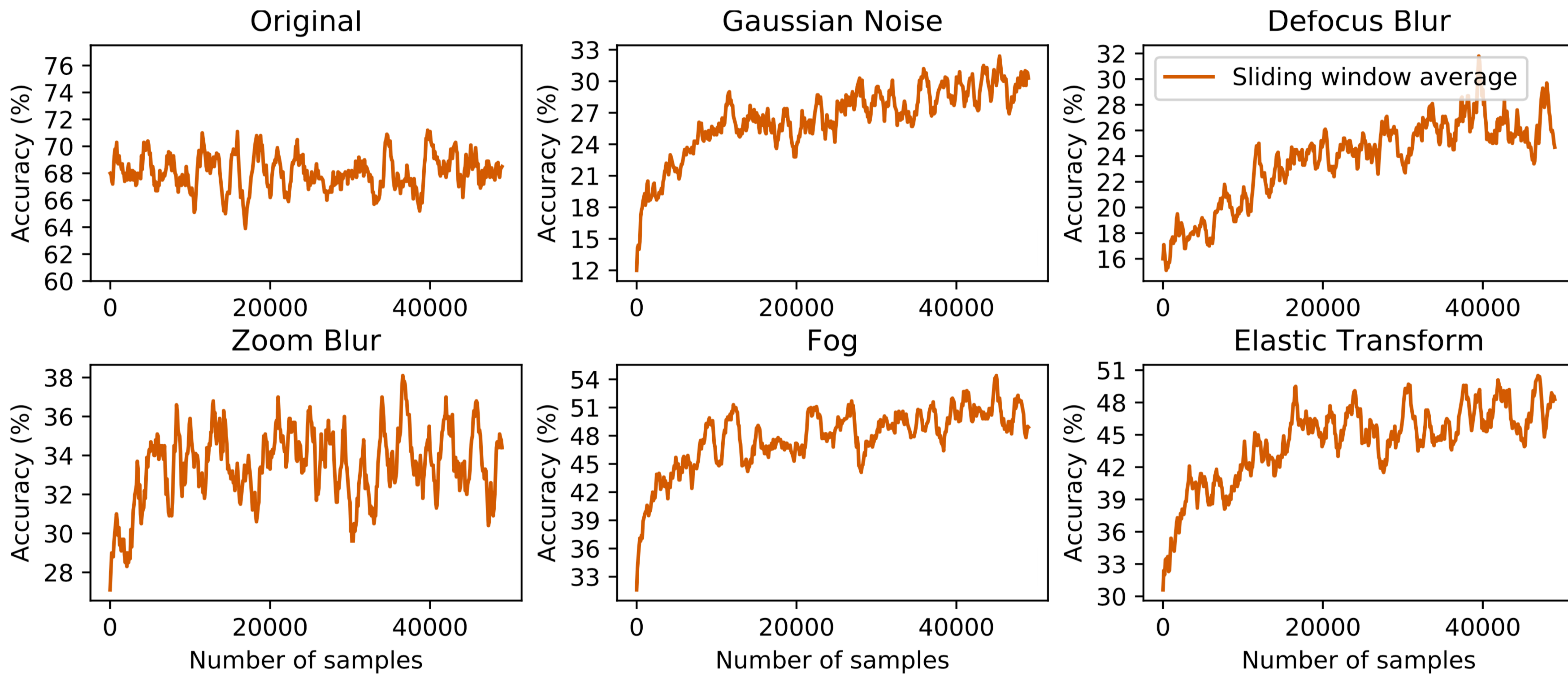
Results on ImageNet-C



Joint training reported here is our improved implementation of their method. Please see our paper for clarification, and their paper for their original results.

Using Self-Supervised Learning Can Improve Model Robustness and Uncertainty
Hendrycks, Mazeika, Kadavath and Song, 2019

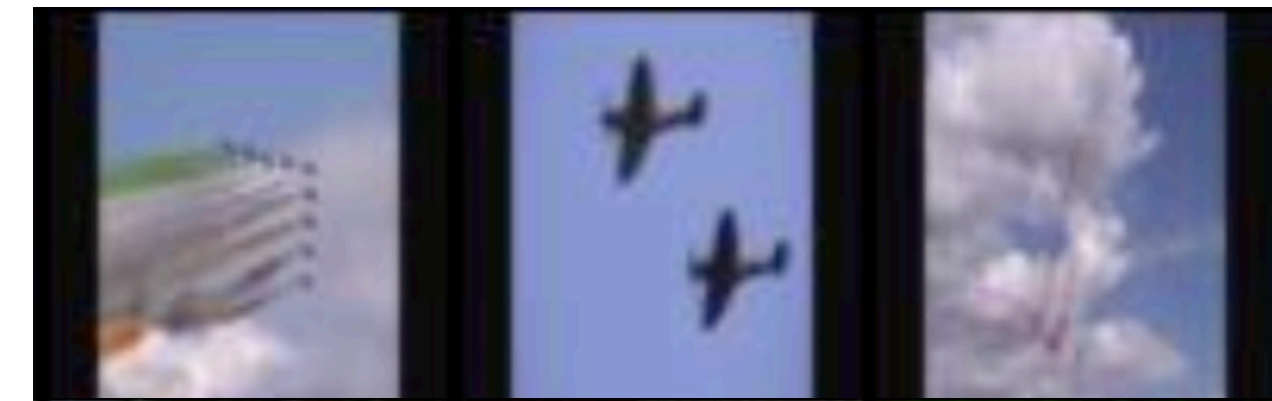
The online version on ImageNet-C



From still images to videos

- Videos of objects in motion
- 7 classes from CIFAR-10
- 30 classes from ImageNet
- Train on CIFAR-10 / ImageNet
- Test on video frames

airplane



bird



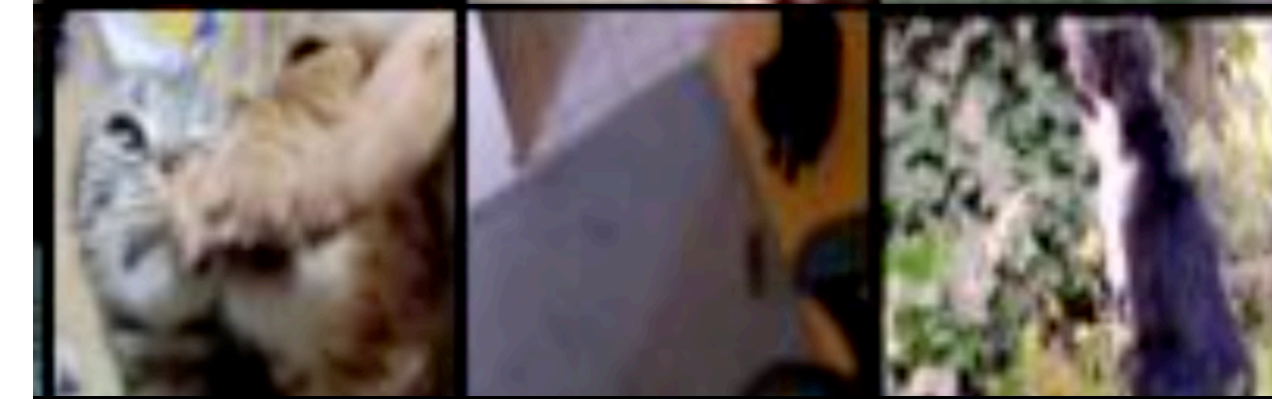
car



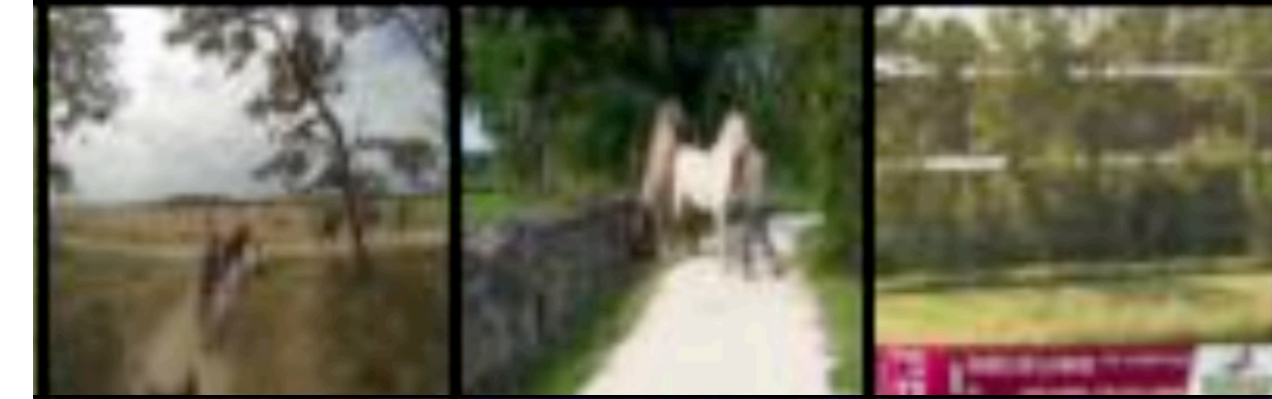
dog



cat



horse



ship



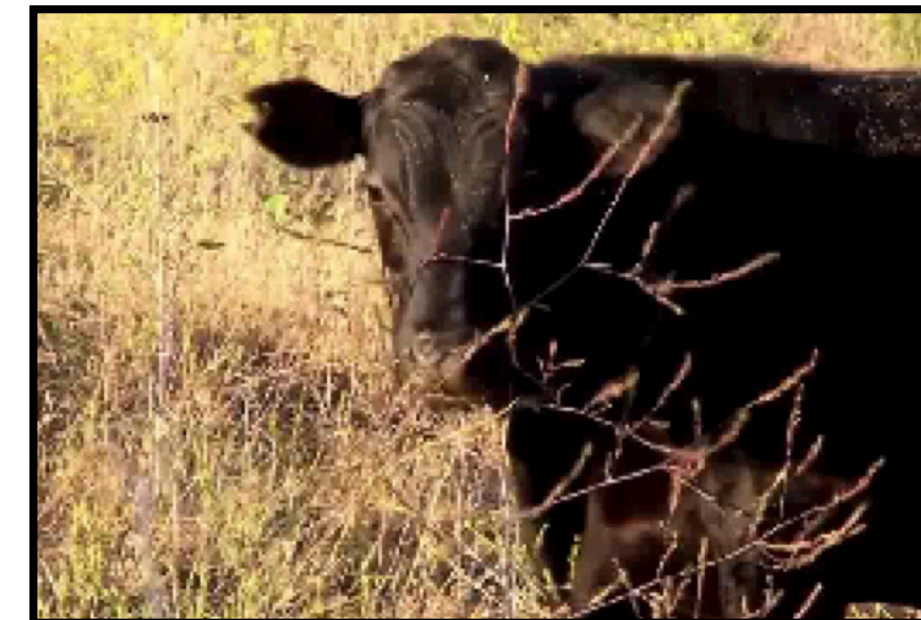
Results

Method	CIFAR-10 accuracy (%)	ImageNet accuracy (%)
Object recognition task only	41.4	62.7
Joint training (Hendrycks et al. 2019)	42.4	63.5
TTT standard	45.2	63.8
TTT online	45.4	64.3

Positive examples



Join training: **dog**
TTT: **elephant**



Join training: **dog**
TTT: **cattle**



Join training: **car**
TTT: **bus**

Results

Method	CIFAR-10 accuracy (%)	ImageNet accuracy (%)
Object recognition task only	41.4	62.7
Joint training (Hendrycks et al. 2019)	42.4	63.5
TTT standard	45.2	63.8
TTT online	45.4	64.3

Negative examples



Join training: hamster

TTT: cat



Join training: snake

TTT: lizard



Join training: turtle

TTT: lizard

Results

Method	CIFAR-10 accuracy (%)	ImageNet accuracy (%)
Object recognition task only	41.4	62.7
Joint training (Hendrycks et al. 2019)	42.4	63.5
TTT standard	45.2	63.8
TTT online	45.4	64.3

Negative examples



Joint training: [airplane](#)

TTT: [bird](#)



Joint training: [airplane](#)

TTT: [watercraft](#)

Rotation prediction is quite limiting!

CIFAR-10.1

- New test set on CIFAR-10
- Cannot notice the distribution shifts
- Still an open problem

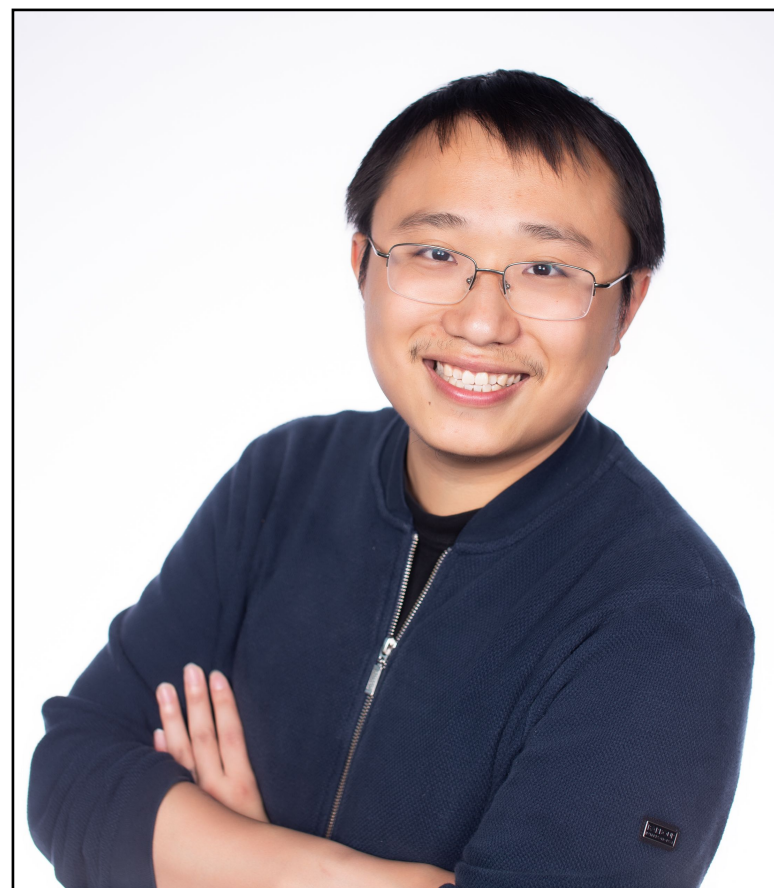


Results

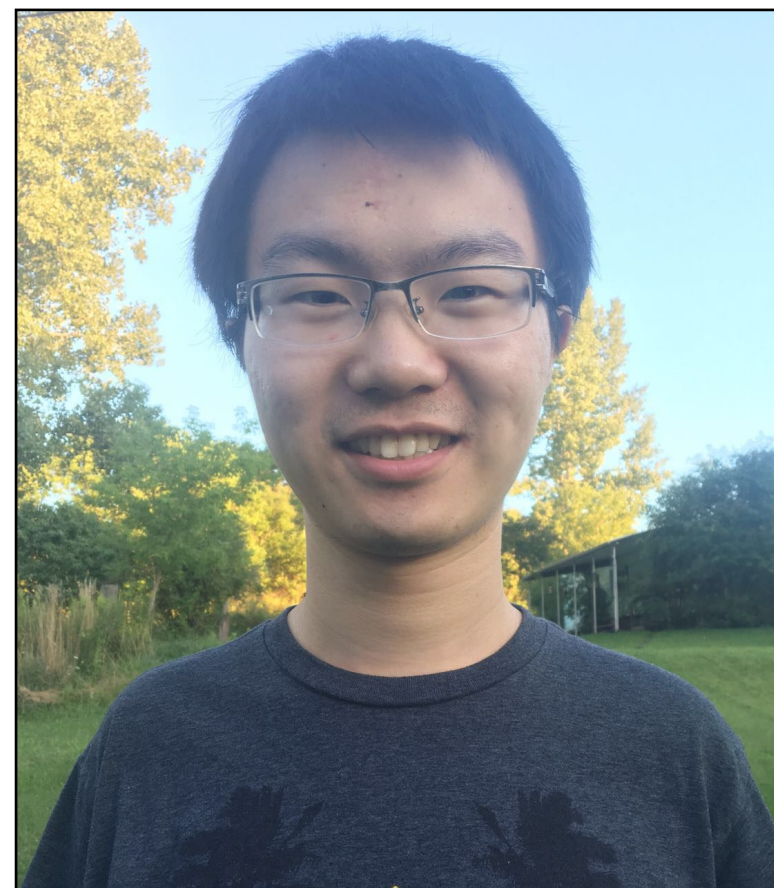
Method	Error (%)
Object recognition task only	17.4
Joint training (Hendrycks et al. 2019)	16.7
TTT standard	15.9

Conclusion

- Boundary between labeled and unlabeled samples
 - Broken down by self-supervision
- Boundary between training and testing
 - We are trying to break this down



Xiaolong Wang



Zhuang Liu



John Miller



Alyosha Efros



Moritz Hardt