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## Towards Accurate Post-training Network Quantization via Bit-split and Stitching

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# Outline

- Background
- Motivation
- Approach
- Experiments



## Background

#### • Low-bit quantization has emerged as a promising compression technique

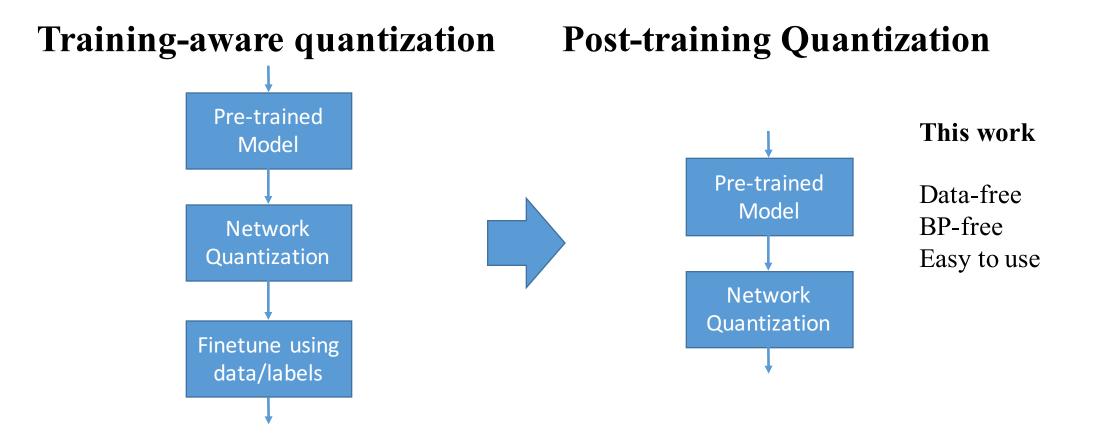
- Robustness to network architectures
- Hardware friendly

#### • Problems: low-bit quantization relies on

- Training data
- Large computational resources (CPUs, GPUs)
- Quantization skills and expertise

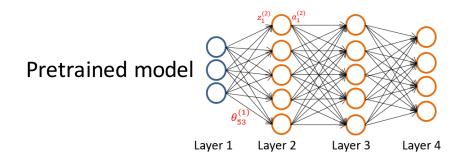
## Background



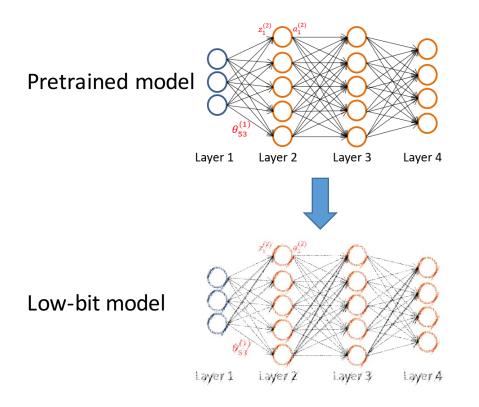


Krishnamoorthi, Raghuraman. "Quantizing deep convolutional networks for efficient inference: A whitepaper." arXiv preprint arXiv:1806.08342 (2018).

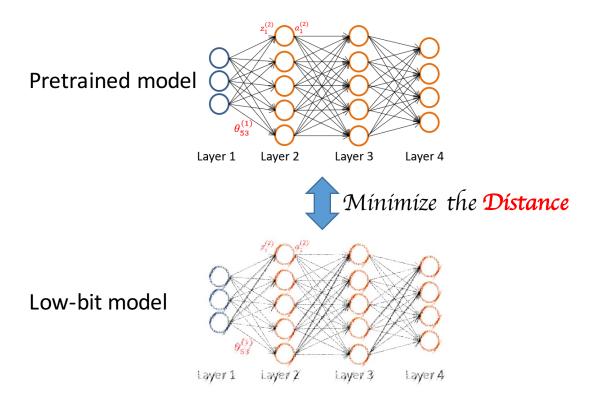


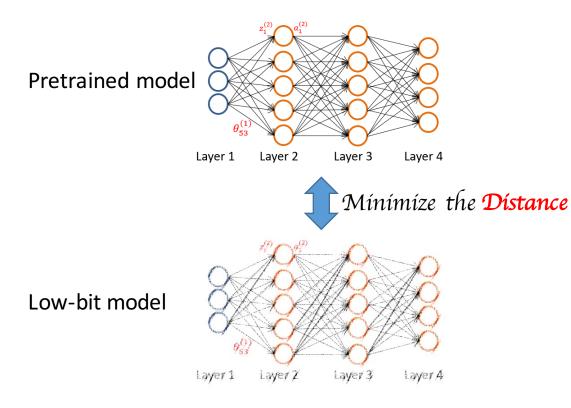














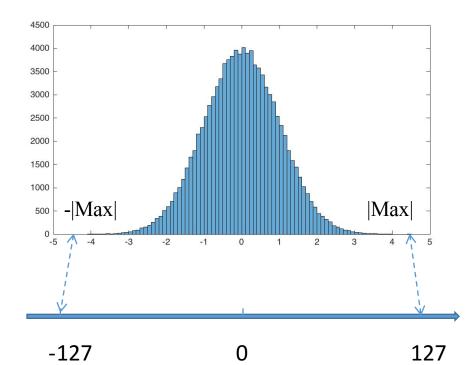
- I. Define the distance
- II. Minimize the distance



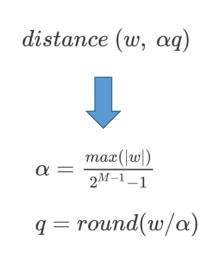


#### **Related works**

- I. Define the distance
- II. Minimize the distance



#### **TF-lite** Map the *maximum weighs (activations)* to the maximum low-bit number

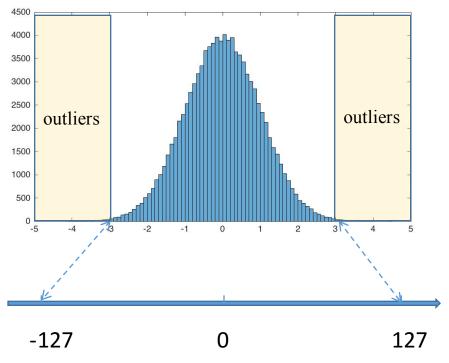


Krishnamoorthi, Raghuraman. "Quantizing deep convolutional networks for efficient inference: A whitepaper." arXiv preprint arXiv:1806.08342 (2018).



### **Related works**

- I. Define the distance
- II. Minimize the distance



Szymon Migacz. 8-bit Inference with TensorRT. GTC 2017

**TensorRT** Map the *clip value* to the maximum low-bit number

distance  $(clip(w), \alpha q)$ 

 $lpha = rac{ClipValue}{2^{M-1}-1}$ 

q = round(clip(w)/lpha)



### Method

I. **Define the distance** Minimize the distance II. Pretrained model Layer 1 Layer 2 Layer 4 Layer 3 Minimize the **Distance** Low-bit model Layer 2 Layer 3 Layer A Layer 1

#### Objective

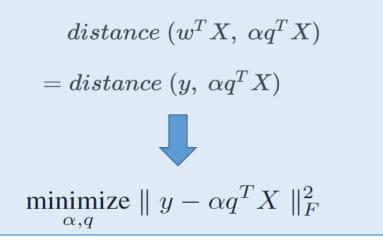
| minimize: | $f(x; \{w_l\}_{l=1}^L)$ | $\leftrightarrow \ f(x; \{q_l\}_{l=1}^L)$ |
|-----------|-------------------------|---|
|-----------|-------------------------|---|

**Previous work** 

minimize:  $w_l \leftrightarrow q_l$ 

#### This work

Learns *a low-bit mapping* from input to the output of every convolution.





### Method

I. Define the distance

 $\underset{\alpha,q}{\text{minimize}} \parallel y - \alpha q^T X \parallel_F^2$ 

II. Minimize the distance (Bit-split)

$$\min_{\alpha, \{q_1, \cdots, q_{M-1}\}} \| y - \alpha (2^0 q_1^T + \dots + 2^{M-2} q_{M-1}^T) X \|_F^2,$$
  
s.t.  $q_m \in \{-1, 0, +1\}^{(C \cdot K_h \cdot K_w)}$ for  $m = 1, \dots, M-1$ 

 $2^{M-2}$   $2^1$   $2^0$  $q_M q_{M-1}$  ...  $q_2 q_1$ 



## Method

#### **Optimize** $\alpha$

#### **Optimize m-th bit**

$$\min_{\substack{\alpha, \{q_1, \cdots, q_{M-1}\}}} \| y - \alpha (2^0 q_1^T + \dots + 2^{M-2} q_{M-1}^T) X \|_F^2,$$
  
s.t.  $q_m \in \{-1, 0, +1\}^{(C \cdot K_h \cdot K_w)}$  for  $m = 1, \dots, M-1$ 

$$\begin{array}{l} \underset{q_m}{\text{minimize}} \parallel y_m - \alpha_m q_m^T X \parallel_F^2, \\ s.t. \ q_m \in \{-1, 0, +1\}^{(C \cdot K_h \cdot K_w)} \end{array}$$

$$\begin{cases} y_m = y - \alpha \sum_{i \neq m} 2^{m-1} q_i^T X, \\ \alpha_m = \alpha 2^{m-2} \end{cases}$$

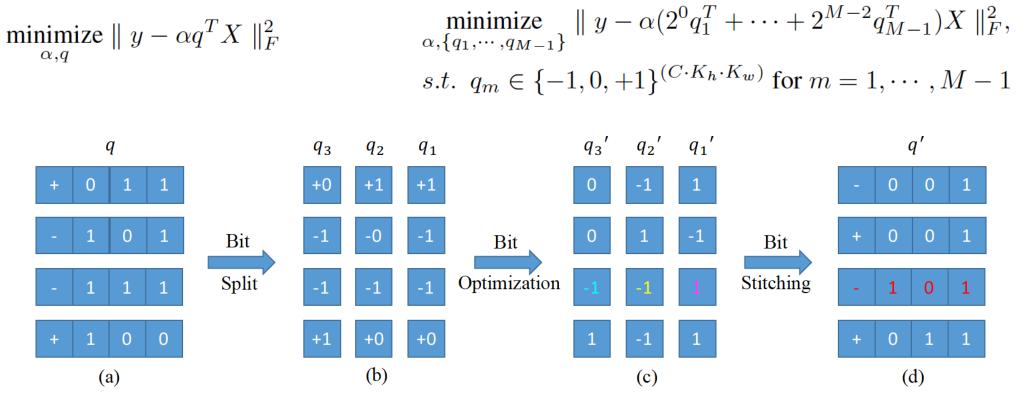
Wang, P., Hu, Q., Zhang, Y., Zhang, C., Liu, Y. and Cheng, J., 2018. Two-step quantization for low-bit neural networks. In Proceedings of the IEEE Conference on computer vision and pattern recognition (pp. 4376-4384).



## **Bit-Split for Post-training Network Quantization**

**Problem:** 

#### **Optimization:**



*Figure 1.* An illustration of Bit-Split and Stitching (Bit-split) framework for 4-bit weight quantization. In the first step of bit-split stage, each 4-bit value is split into 3 ternary values, which can be optimized separately in the second bit-optimization stage. The third stage stitching optimized bits back into integers, taking the third value for example,  $2^0 \cdot 1 + 2^1 \cdot (-1) + 2^2 \cdot (-1) = -5 = -101b$ .



## **Bit-Split Results**

#### Weight Quantization:

| Model          |                | 8-    | bit   | 7-    | bit   | 6-    | bit   | 5-    | bit          | 4-    | bit   | 3-    | bit   |
|----------------|----------------|-------|-------|-------|-------|-------|-------|-------|--------------|-------|-------|-------|-------|
|                | uei            | Top-1 | Top-5 | Top-1 | Top-5 | Top-1 | Top-5 | Top-1 | Top-5        | Top-1 | Top-5 | Top-1 | Top-5 |
| ResNet-18      | TF-Lite        | 69.63 | 88.96 | 69.67 | 89.02 | 69.06 | 88.72 | 66.81 | 87.39        | 55.53 | 79.21 | 0.85  | 2.68  |
| (69.76, 89.08) | Bit-split      | 69.79 | 89.15 | 69.84 | 89.15 | 69.83 | 89.12 | 69.70 | 88.93        | 69.11 | 88.69 | 66.76 | 87.45 |
|                | Bit-split (A8) | 69.82 | 89.15 | 69.82 | 89.05 | 69.80 | 89.12 | 69.64 | <b>88.98</b> | 69.10 | 88.69 | 66.75 | 87.46 |
| ResNet-50      | TF-Lite        | 76.12 | 92.88 | 76.07 | 92.86 | 75.87 | 92.82 | 75.17 | 92.50        | 70.14 | 89.57 | 4.22  | 11.53 |
| (76.15, 92.87) | Bit-split      | 76.20 | 92.97 | 76.16 | 92.91 | 76.17 | 92.90 | 76.05 | 92.82        | 75.58 | 92.57 | 73.64 | 91.61 |
| ResNet-101     | TF-Lite        | 77.32 | 93.57 | 77.28 | 93.51 | 77.06 | 93.47 | 76.25 | 93.05        | 72.67 | 90.87 | 9.19  | 20.05 |
| (77.47, 93.56) | Bit-split      | 77.55 | 93.59 | 77.44 | 93.59 | 77.51 | 93.60 | 77.55 | 93.59        | 76.89 | 93.31 | 74.98 | 92.42 |
| VGG-16-BN      | TF-Lite        | 73.36 | 91.51 | 73.34 | 91.48 | 73.12 | 91.36 | 72.37 | 90.86        | 66.36 | 87.26 | 1.16  | 4.49  |
| (73.37, 91.50) | Bit-split      | 73.43 | 91.61 | 73.37 | 91.52 | 73.22 | 91.53 | 73.37 | 91.50        | 72.97 | 91.35 | 72.11 | 90.77 |

#### **Both Weight and Activation Quantization:**

| Model          |           | 8-    | bit   | 7-    | bit   | 6-    | bit   | 5-    | bit          | 4-1   | bit   | 3-    | bit   |
|----------------|-----------|-------|-------|-------|-------|-------|-------|-------|--------------|-------|-------|-------|-------|
| Mode           | L         | Top-1 | Top-5 | Top-1 | Top-5 | Top-1 | Top-5 | Top-1 | Top-5        | Top-1 | Top-5 | Top-1 | Top-5 |
| ResNet-18      | TF-Lite   | 69.57 | 89.02 | 69.46 | 88.87 | 67.95 | 88.02 | 61.47 | 83.43        | 18.84 | 36.33 | 0.13  | 0.61  |
| (69.76, 89.08) | Bit-split | 69.74 | 89.09 | 69.68 | 89.07 | 69.58 | 88.96 | 69.28 | <b>88.77</b> | 67.56 | 87.76 | 61.30 | 83.47 |
| ResNet-50      | TF-Lite   | 76.05 | 92.93 | 75.75 | 92.70 | 73.83 | 91.66 | 65.46 | 86.34        | 10.40 | 22.36 | 0.11  | 0.54  |
| (76.15, 92.87) | Bit-split | 75.96 | 92.83 | 76.09 | 92.84 | 75.90 | 92.75 | 75.38 | 92.59        | 73.71 | 91.62 | 66.22 | 87.18 |
| ResNet-101     | TF-Lite   | 76.78 | 93.31 | 74.07 | 91.79 | 31.78 | 55.96 | 0.82  | 2.65         | 0.25  | 0.98  | 0.09  | 0.54  |
| (77.47, 93.56) | Bit-split | 77.23 | 93.55 | 77.20 | 93.47 | 76.93 | 93.42 | 76.07 | 92.95        | 74.68 | 92.18 | 63.96 | 85.65 |
| VGG-16-BN      | TF-Lite   | 73.31 | 91.53 | 72.94 | 91.25 | 70.65 | 89.77 | 54.45 | 78.18        | 3.41  | 10.17 | 0.18  | 0.78  |
| (73.37, 91.50) | Bit-split | 73.43 | 91.54 | 73.43 | 91.55 | 73.34 | 91.45 | 72.89 | 91.22        | 71.14 | 90.29 | 66.11 | 86.92 |



## **Comparison with State-of-the-arts**

| Tat    | Table 4. Comparison results of different post-training quantization approaches. Bold values indicate the best results. |              |                   |           |           |            |           |  |  |  |
|--------|--|--------------|-------------------|-----------|-----------|------------|-----------|--|--|--|
|        | Model  | Per-layer    | Unified-precision | ResNet-18 | ResNet-50 | ResNet-101 | VGG-16-BN |  |  |  |
|        | Full-precision   | -            | -                 | 69.76     | 76.15     | 77.47      | 73.37     |  |  |  |
| A8W4   | TF-Lite (Krishnamoorthi, 2018)   | $\checkmark$ |                   | 55.5      | 70.1      | 72.6       | 66.4      |  |  |  |
| Aow4   | ACIQ (Banner et al., 2019)   | ×            | $\checkmark$      | 67.4      | 74.8      | 76.3       | 71.7      |  |  |  |
|        | ACIQ-Mix (Banner et al., 2019)   | ×            | ×                 | 68.3      | 75.3      | 76.9       | 72.4      |  |  |  |
|        | Bit-split  | $\checkmark$ | $\checkmark$      | 69.1      | 75.6      | 76.9       | 73.0      |  |  |  |
| A4W4   | TF-Lite (Krishnamoorthi, 2018)   | $\checkmark$ | $\checkmark$      | 18.8      | 10.4      | 0.3        | 3.4       |  |  |  |
| A4 W 4 | TensorRT (Migacz, 2017)  | $\checkmark$ | $\checkmark$      | 31.9      | 46.2      | 49.9       | -         |  |  |  |
|        | LAPQ (Nahshan et al., 2019)  | $\checkmark$ | $\checkmark$      | 59.8      | 70.0      | 59.2       | -         |  |  |  |
|        | ACIQ-Mix (Banner et al., 2019)   | ×            | ×                 | 67.0      | 73.8      | 75.0       | 71.8      |  |  |  |
|        | Bit-split  | $\checkmark$ | $\checkmark$      | 67.6      | 73.7      | 74.7       | 71.1      |  |  |  |
|        | Bit-split-per-channel  | ×            | $\checkmark$      | 68.1      | 74.2      | 75.3       | 71.8      |  |  |  |

Table 4. Comparison regults of different post training quantization approaches. Bold values indicate the best regults



## **Results on Detection and Instance segmentation**

| tion (mask AP) results on COCO minival set. |                |                        |            |             |  |  |  |  |  |  |
|---|----------------|------------------------|------------|-------------|--|--|--|--|--|--|
| Mo  | del            | AP <sub>0.5:0.95</sub> | $AP_{0.5}$ | $AP_{0.75}$ |  |  |  |  |  |  |
| RetinaNet                                   | Full-precision | 30.7                   | 49.1       | 32.4        |  |  |  |  |  |  |
| (Box)                                       | A8W4           | 30.1                   | 48.2       | 31.8        |  |  |  |  |  |  |
|   | A6W4           | 30.2                   | 48.2       | 31.9        |  |  |  |  |  |  |
|   | A4W4           | 29.6                   | 47.6       | 31.0        |  |  |  |  |  |  |
| Mask R-CNN                                  | Full-precision | 33.1                   | 54.3       | 35.2        |  |  |  |  |  |  |
| (Box)                                       | A8W4           | 32.4                   | 53.5       | 34.4        |  |  |  |  |  |  |
|   | A6W4           | 32.3                   | 53.3       | 34.2        |  |  |  |  |  |  |
|   | A4W4           | 32.0                   | 52.9       | 34.0        |  |  |  |  |  |  |
| Mask R-CNN                                  | Full-precision | 30.7                   | 51.2       | 32.4        |  |  |  |  |  |  |
| (Mask)                                      | A8W4           | 30.1                   | 50.5       | 31.6        |  |  |  |  |  |  |
|   | A6W4           | 30.1                   | 50.4       | 31.5        |  |  |  |  |  |  |
|   | A4W4           | 29.6                   | 49.7       | 31.2        |  |  |  |  |  |  |

*Table 5.* Object detection (bounding box AP) and instance segmentation (mask AP) results on COCO minival set.



# Thanks for your attention.

Codes are available at <a href="https://github.com/wps712/BitSplit">https://github.com/wps712/BitSplit</a>

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