

Machine Learning
Research Group



Asynchronous Batch Bayesian Optimisation with Improved Local Penalisation

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ICML 2019

Talk Overview

- Bayesian optimisation (BO) recap
- Synchronous vs asynchronous BO
- Our Method
 - Design of penaliser
 - Locally estimated Lipschitz constant
- Empirical results

1. Bayesian Optimisation (BO)

- To solve the global optimisation

$$\mathbf{x}^* = \arg \min_{\mathbf{x} \in \mathcal{X}} f(\mathbf{x})$$

- The objective function

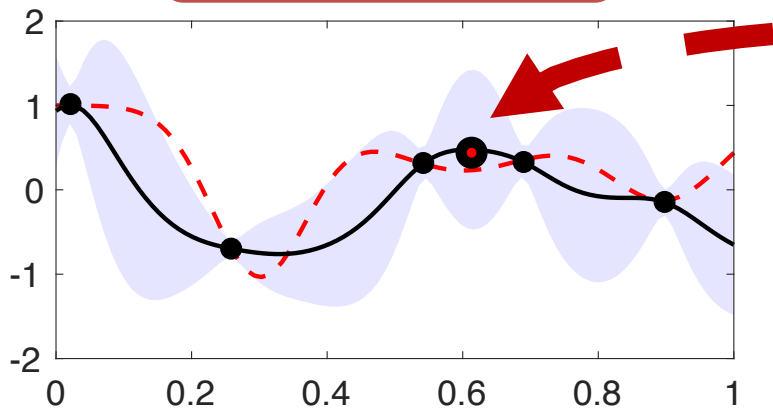


1. Bayesian Optimisation (BO)

$$\mathbf{x}^* = \arg \min_{\mathbf{x} \in \mathcal{X}} f(\mathbf{x})$$

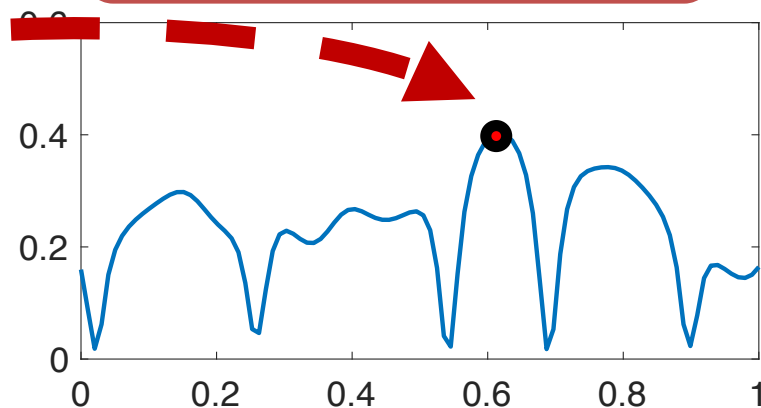


$$f \sim \mathcal{GP}(\mu_t, K_t)$$



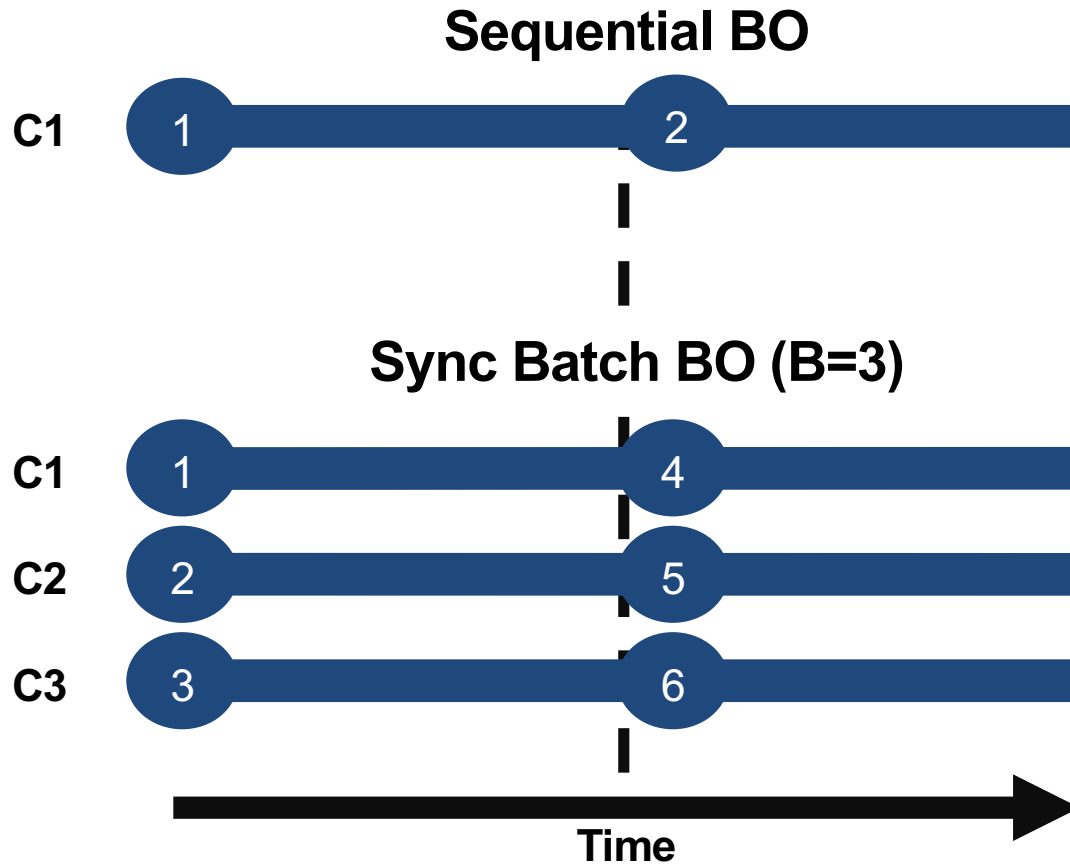
$$\mathbf{x}^* = \arg \min_{\mathbf{x} \in \mathcal{X}} f(\mathbf{x})$$

$$\mathbf{x}_{t+1} = \arg \max_{\mathbf{x} \in \mathcal{X}} \alpha_t(\mathbf{x})$$



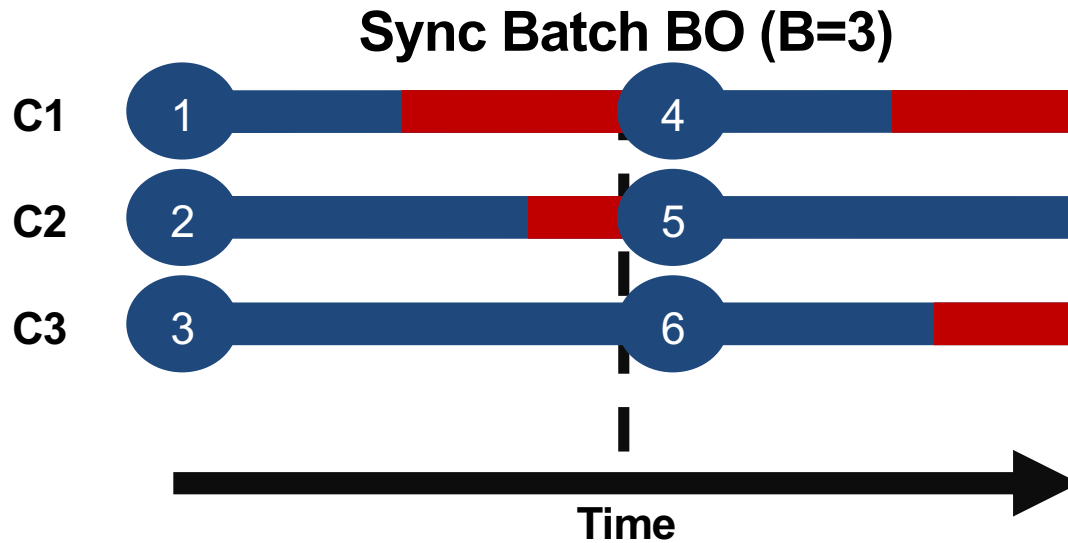
2. Synchronous Batch BO

- Enable *multiple* evaluations in parallel



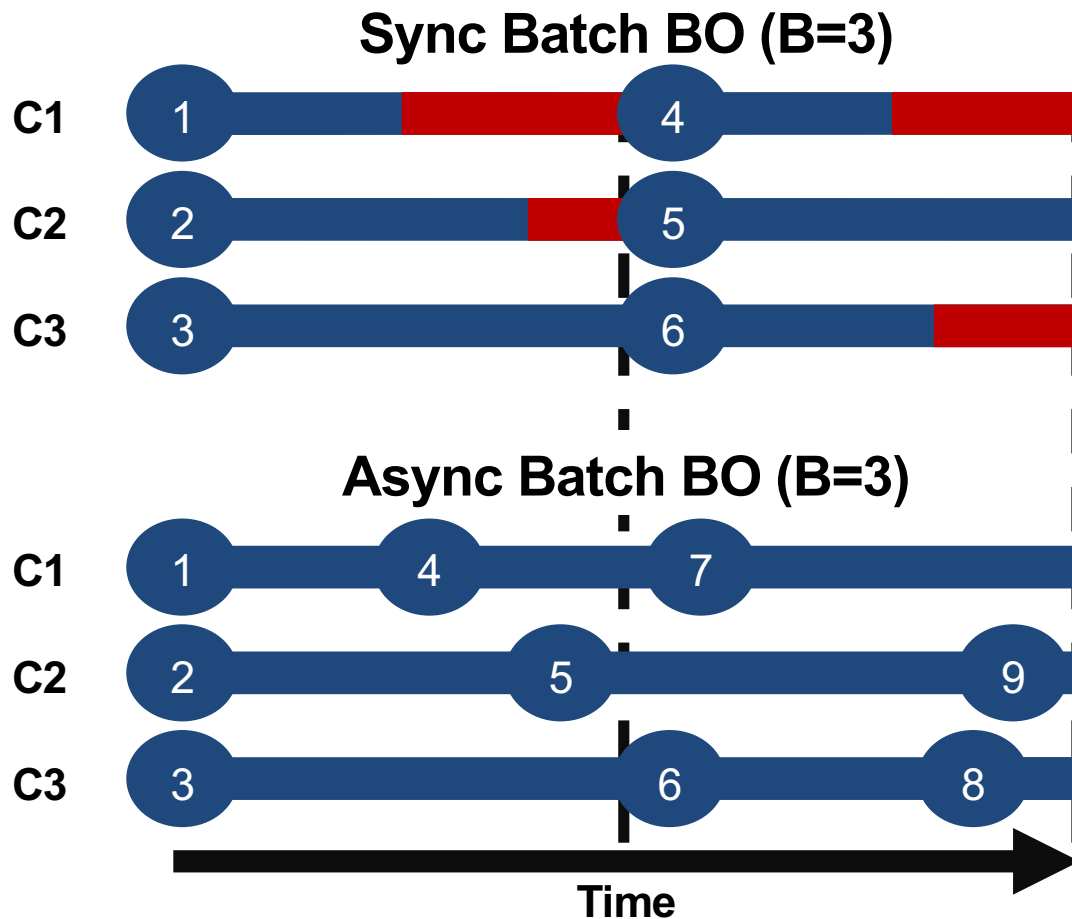
2. Asynchronous Batch BO

- Maximise utilisation of parallel workers



2. Asynchronous Batch BO

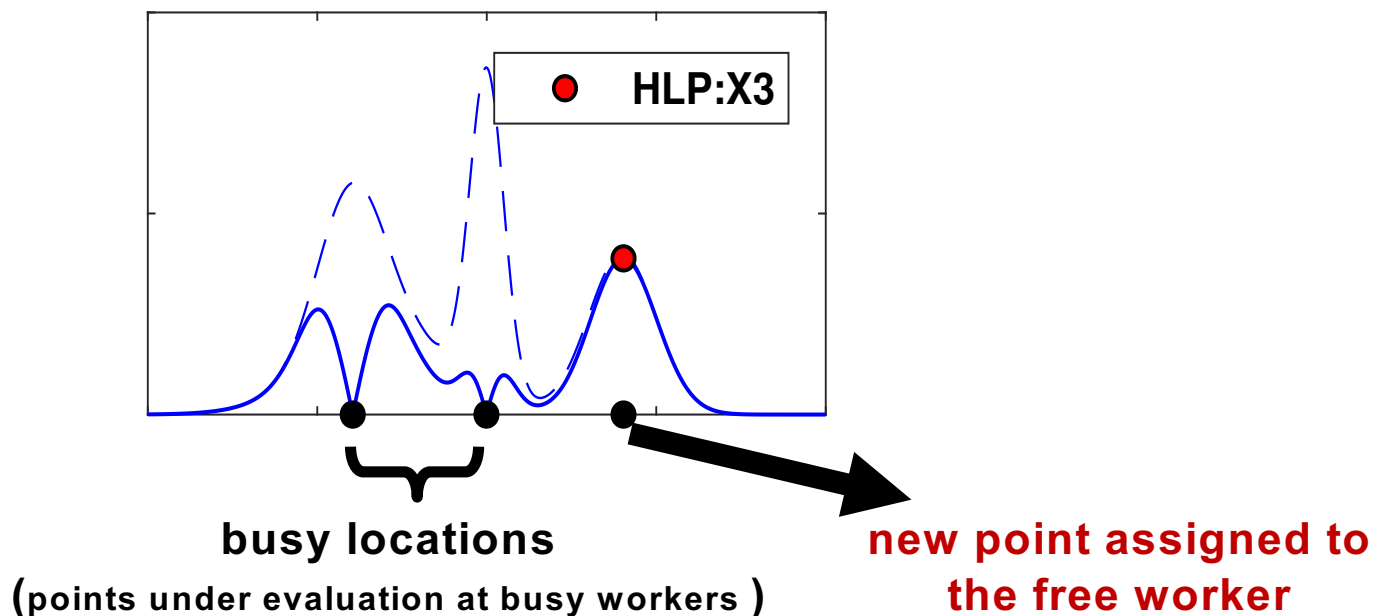
- Maximise utilisation of parallel workers



3. Our Method

- A new async batch BO: **Penalising Locally for Asynchronous Bayesian Optimisation on k Workers (PLAYBOOK)**

$$\mathbf{x}^q = \arg \max_{\mathbf{x} \in \mathcal{X}} \left\{ \alpha(\mathbf{x}) \prod_{i=1}^{q-1} \psi(\mathbf{x} | \mathbf{x}^i) \right\}$$



3. Our Method

- *Penalising Locally for **Asynchronous Bayesian Optimisation on k Workers (PLAyBOOK)***

$$\mathbf{x}^q = \arg \max_{\mathbf{x} \in \mathcal{X}} \left\{ \alpha(\mathbf{x}) \prod_{i=1}^{q-1} \psi(\mathbf{x} | \mathbf{x}^i) \right\}$$

- Empirically show: PLAyBOOK outperforms
 - other async BO methods
 - its sync. variants in both **time and sample** efficiency

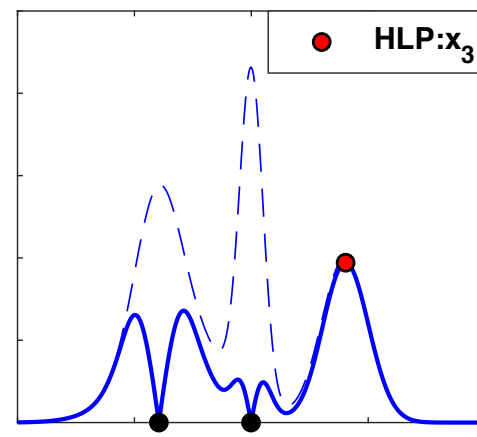
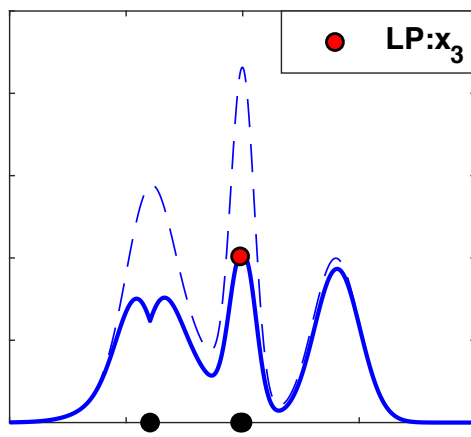
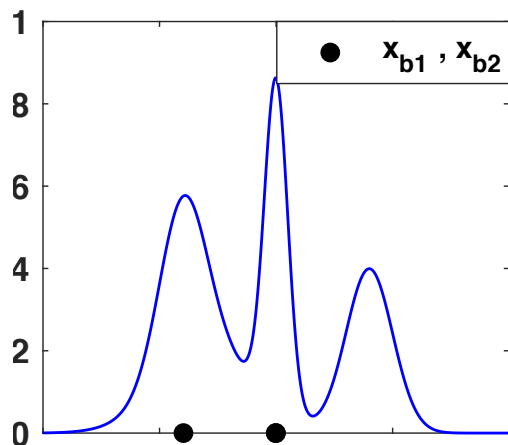
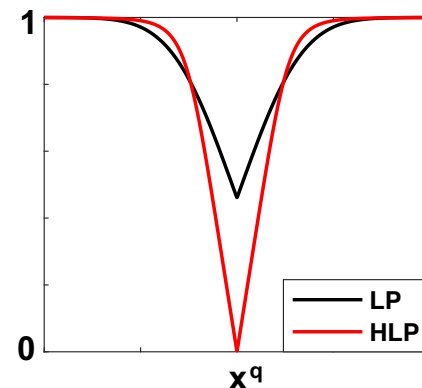
4. Penaliser design

- Our hard penaliser (HLP):

$$\psi_{HLP}(\mathbf{x}|\mathbf{x}^q) = \min \left\{ \frac{\hat{L} \|\mathbf{x} - \mathbf{x}^q\|}{|\mu(\mathbf{x}^q) - M| + \sigma(\mathbf{x}^q)}, 1 \right\}$$

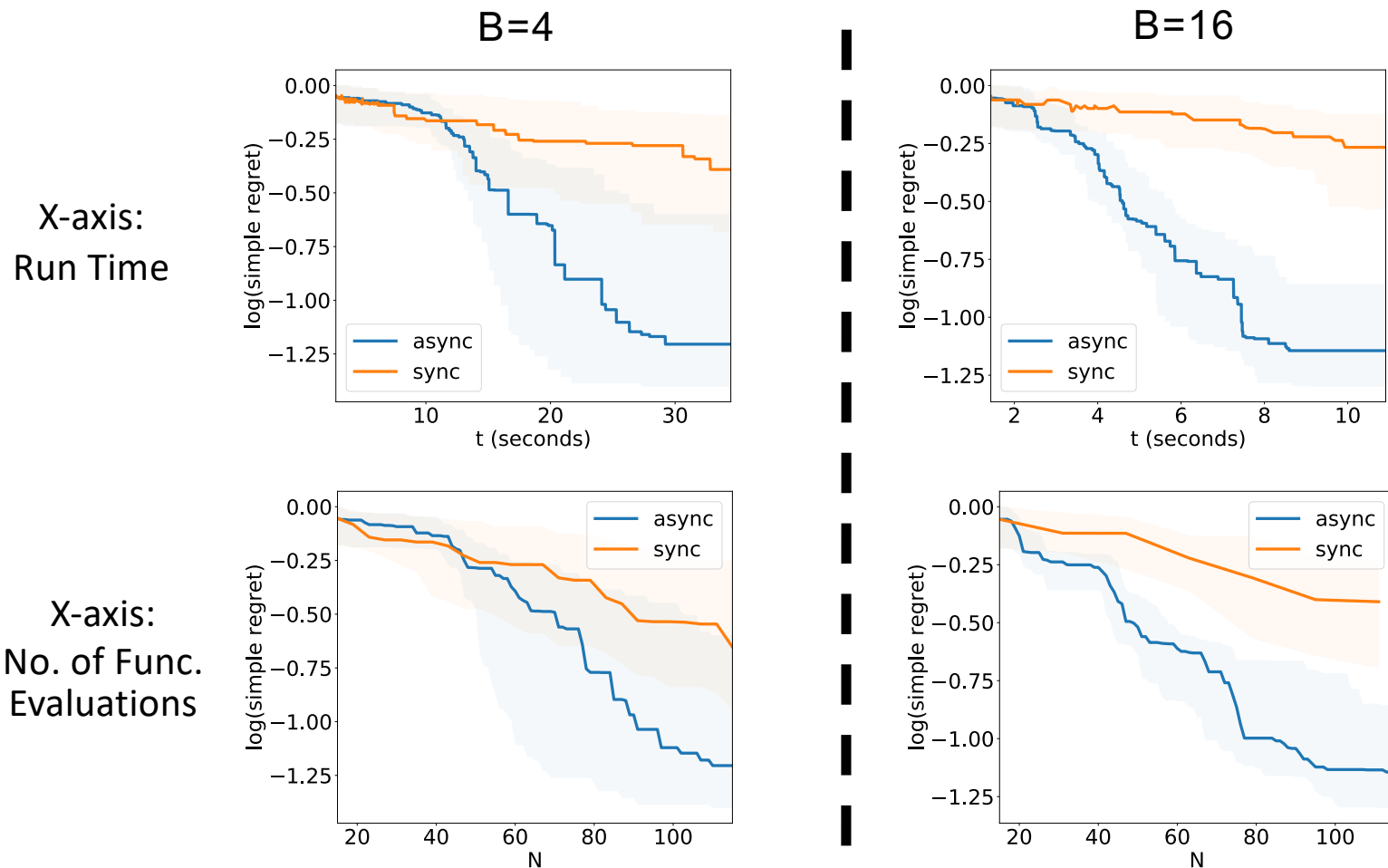
- LP (Gonzalez et al., 2016) :

$$\psi_{LP}(\mathbf{x}|\mathbf{x}^q) = \Phi \left(\frac{\hat{L} \|\mathbf{x} - \mathbf{x}^q\| - |\mu(\mathbf{x}^q) - M|}{\sigma(\mathbf{x}^q)} \right)$$



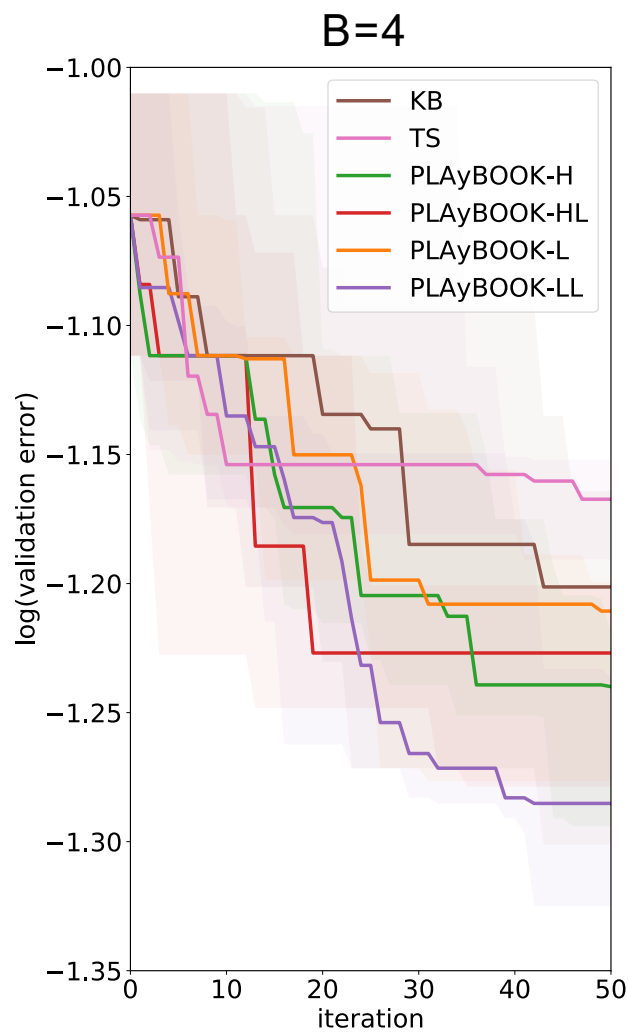
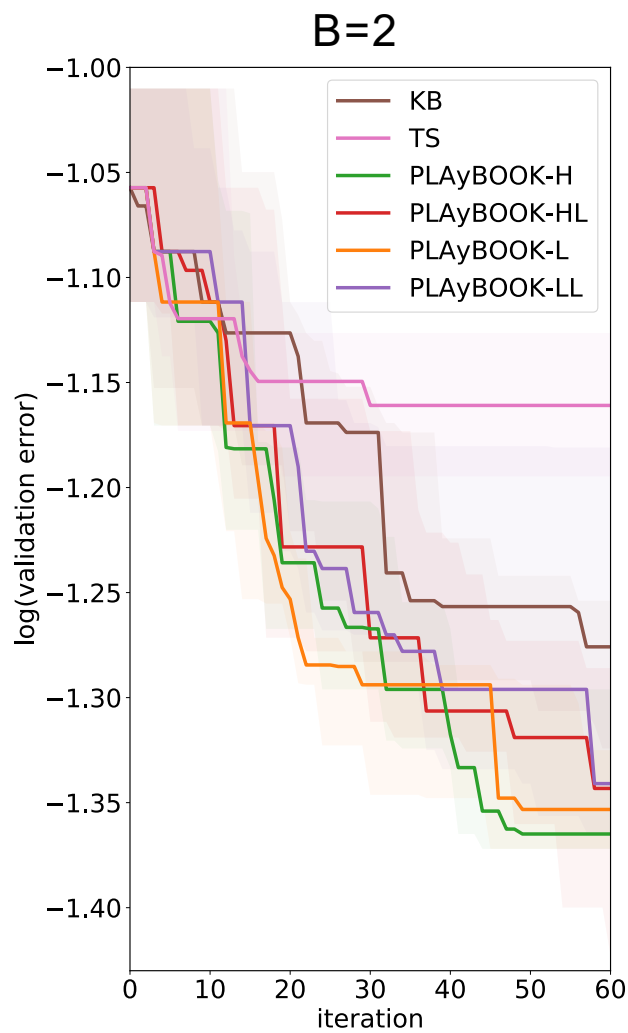
5. Empirical Results: Async. vs. Sync.

- PLAyBOOK-HL: Ackley 5-D: B=4 and B=16



5. Empirical Results: Async. methods

- Tuning 9 hyperparameters of a CNN for CIFAR-10



Thank you!

Meet us at poster #213!