

ICML | 2019

Thirty-sixth International Conference
on Machine Learning

Neurally-Guided Structure Inference

<http://ngsi.csail.mit.edu>

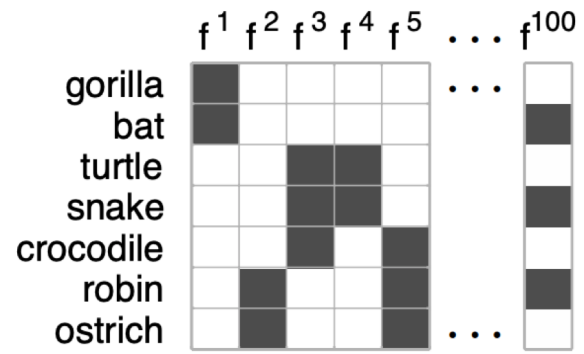
Sidi Lu*, Jiayuan Mao*, Josh Tenenbaum, and Jiajun Wu

(* indicates equal contributions)

Structure Inference

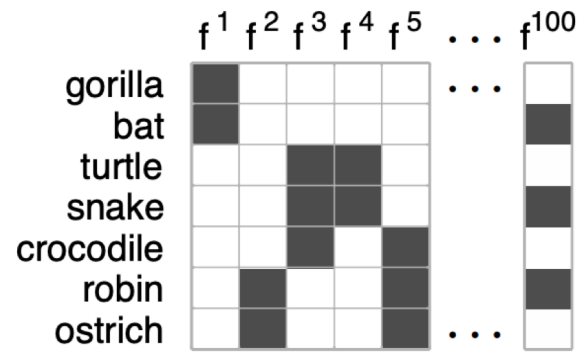
Structure Inference

Data

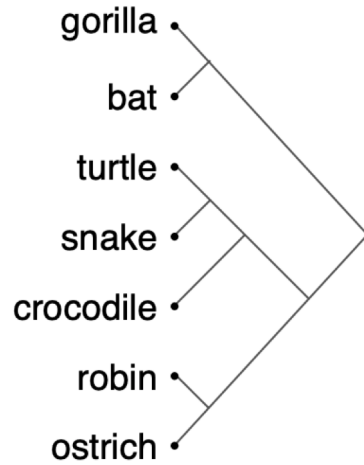


Structure Inference

Data



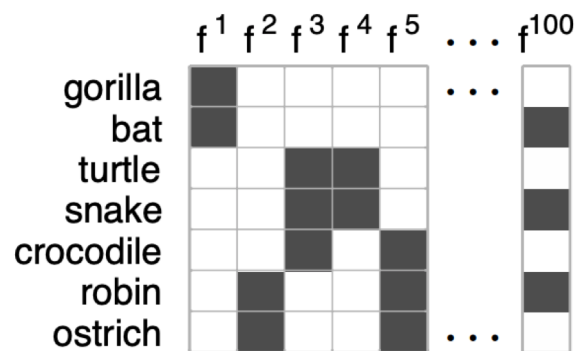
Structure



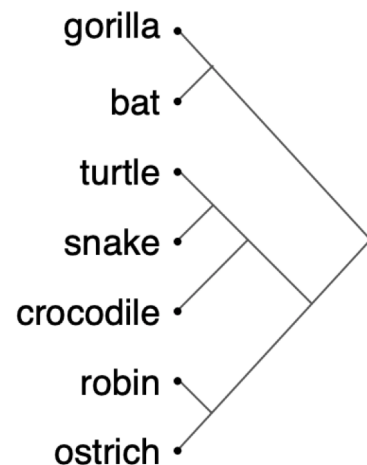
[Kemp et al. 2008]

Structure Inference

Data



Structure



[Kemp et al. 2008]

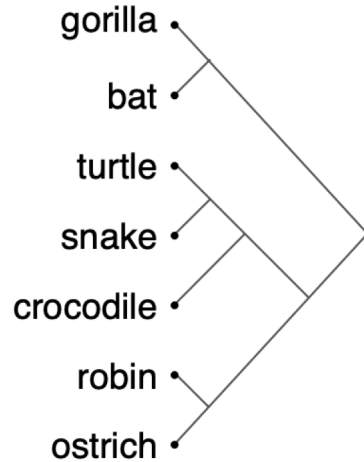
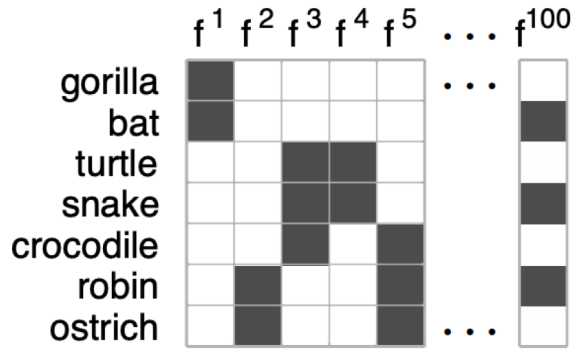
[LeCun et al. 1998]

Structure Inference

Data

Structure Inference

Structure



[Kemp et al. 2008]



[LeCun et al. 1998]



[Chen et al. 2016]

Matrix Decomposition Models

- Clustering $MG+G$
- Low-Rank Approximation $GG+G$
- Binary Features $BG+G$
- Random Walk $CG+G$
- Co-Clustering $M(GM^T+G)+G$
- Clustered Matrix Decomp. $(MG+G)(GM^T+G)+G$
- Binary Matrix Factorization $(BG+G)(GB^T+G)+G$
- Dependent GSM $(\exp(GG+G)\circ G)+G$
-

Structure Inference with Matrix Decomposition Models

Structure Inference with Matrix Decomposition Models

$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}$$

Input Matrix
20×3

Structure Inference with Matrix Decomposition Models

$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}$$

Input Matrix
20×3

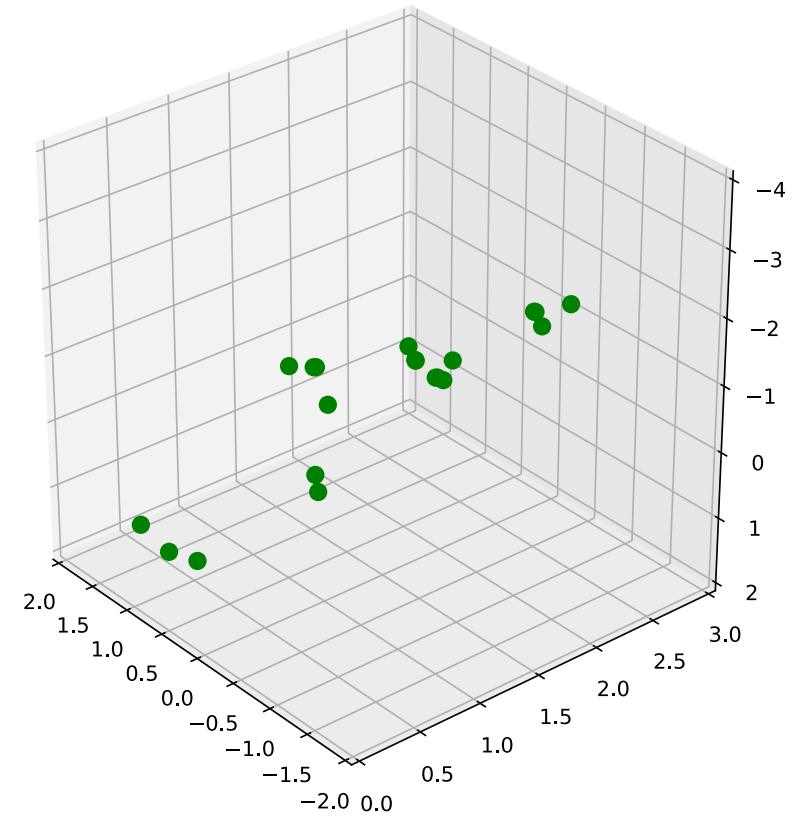
Structure G

Structure Inference with Matrix Decomposition Models

$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}$$

Input Matrix
20×3

Structure G

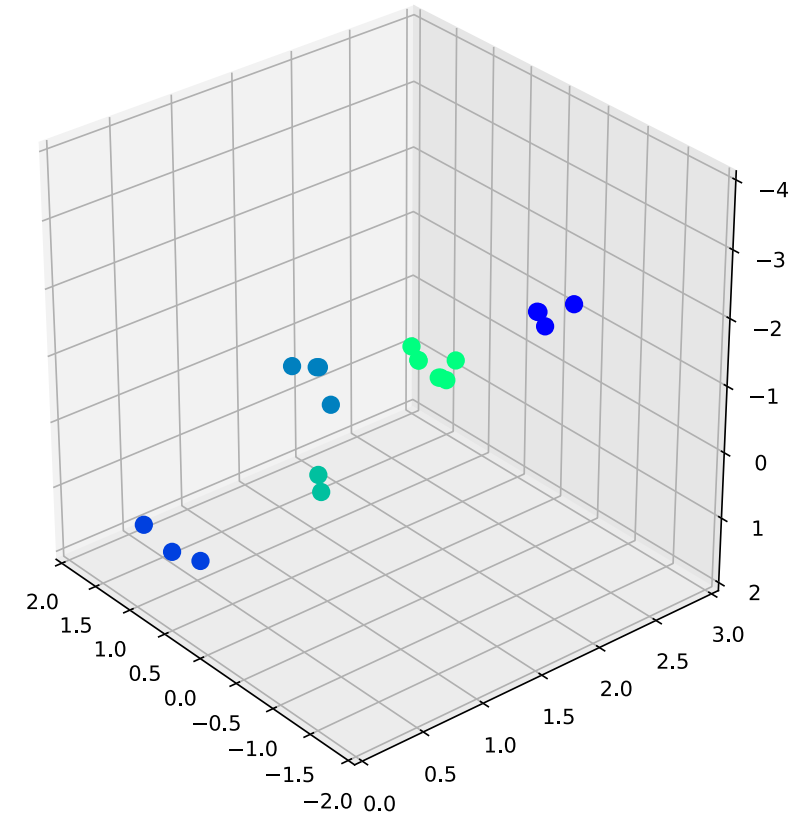


Structure Inference with Matrix Decomposition Models

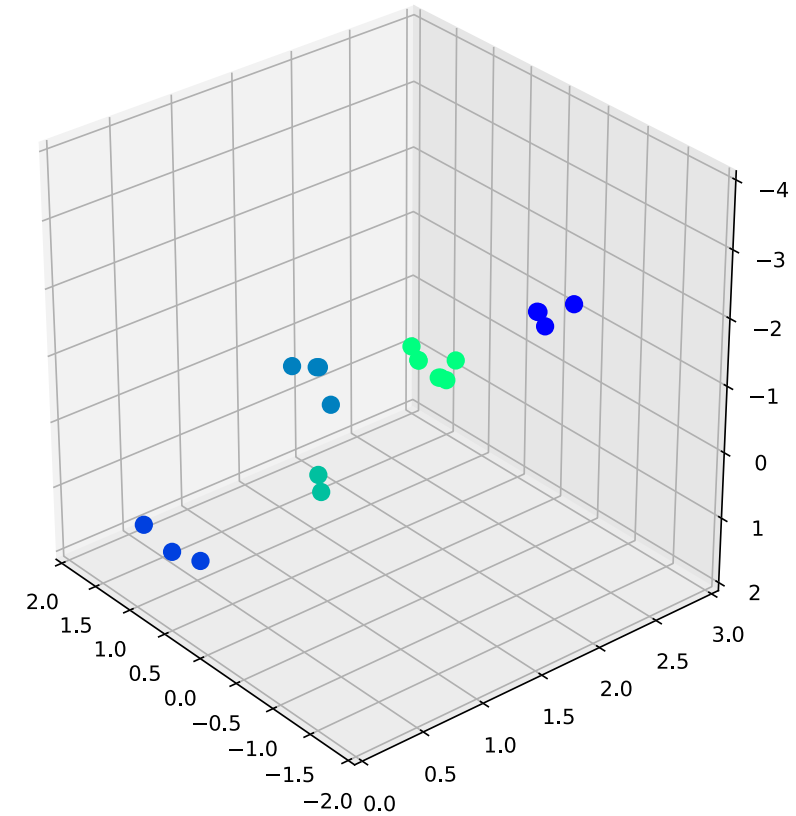
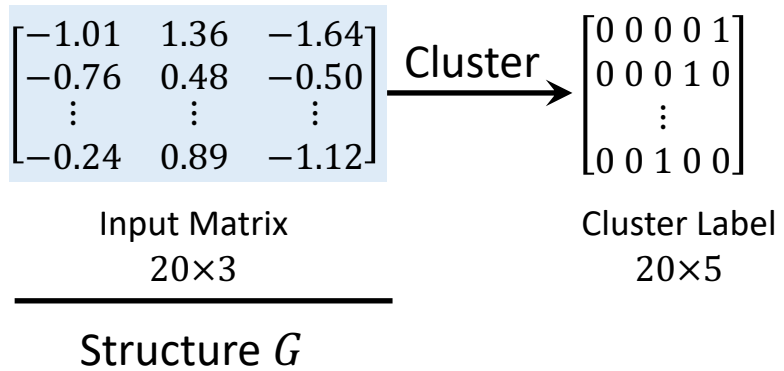
$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}}$$

Input Matrix
20×3

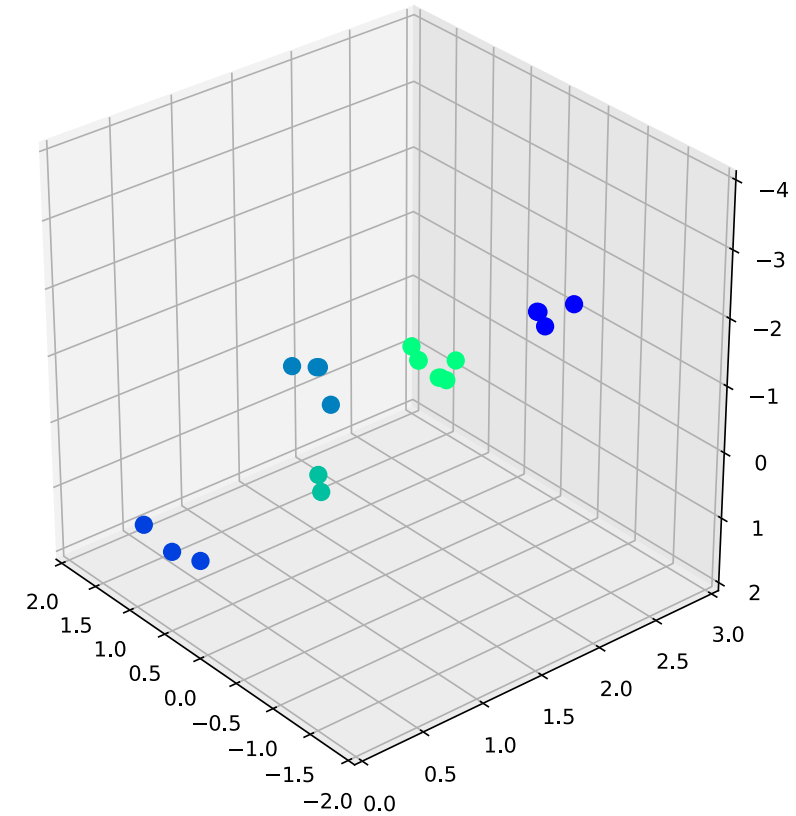
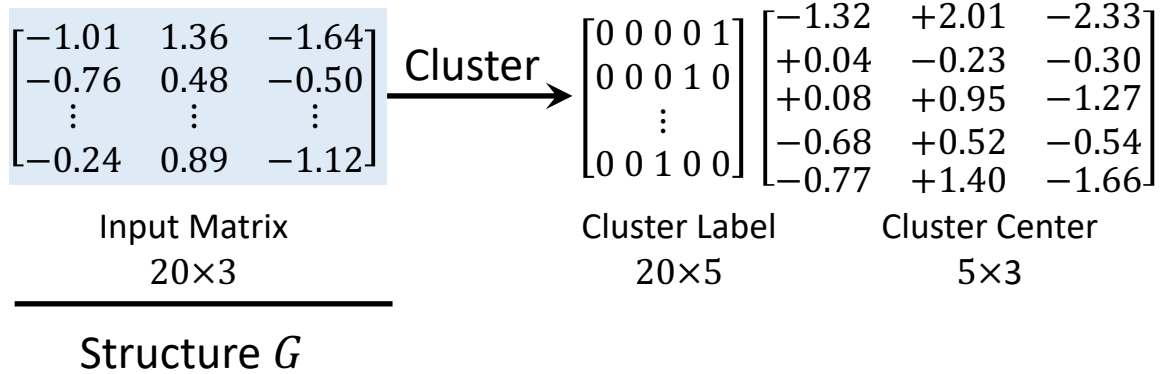
Structure G



Structure Inference with Matrix Decomposition Models

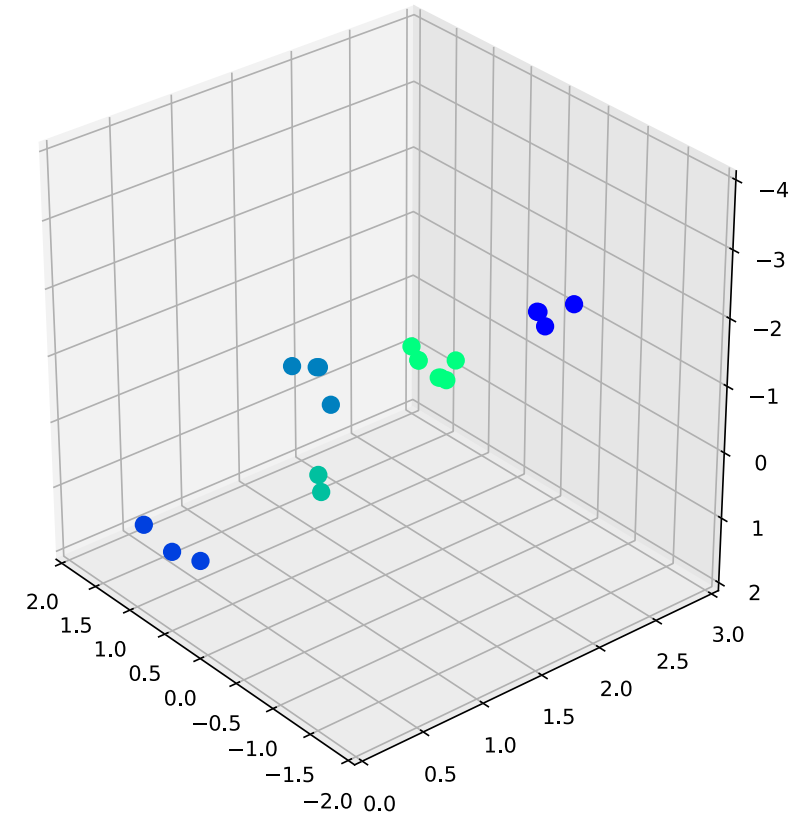


Structure Inference with Matrix Decomposition Models



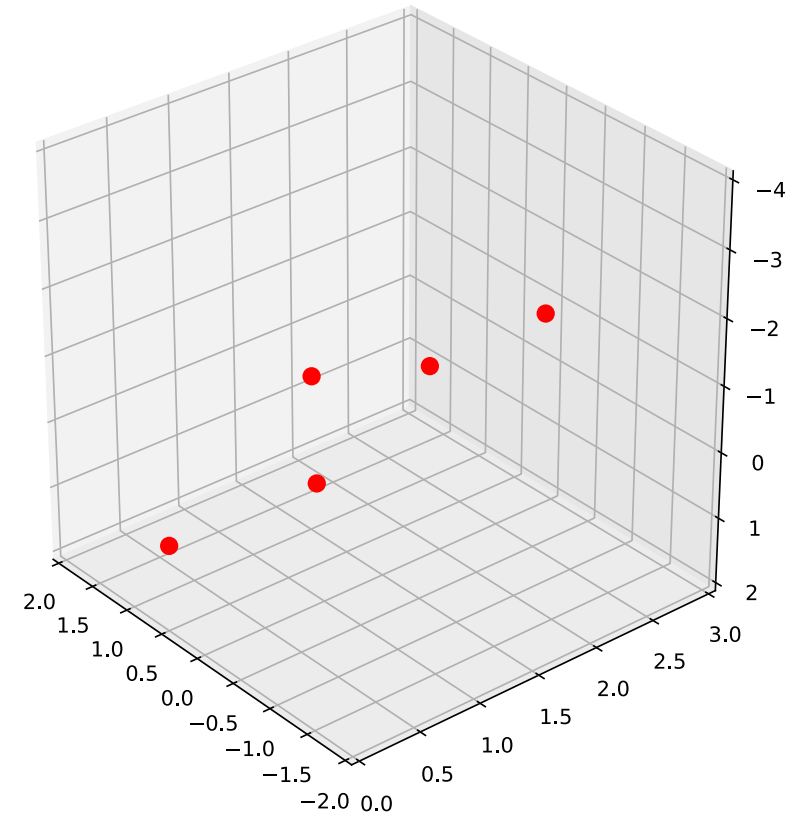
Structure Inference with Matrix Decomposition Models

$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix} & \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 3 & 20 \times 5 & 5 \times 3 & 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G & &
 \end{array}$$



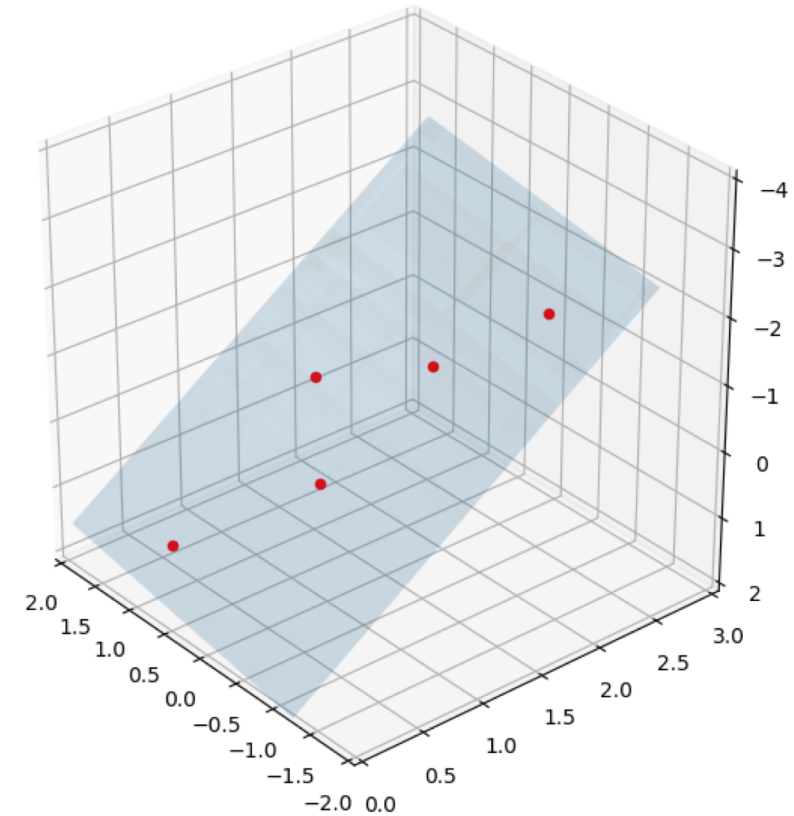
Structure Inference with Matrix Decomposition Models

$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix} & \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 3 & 20 \times 5 & 5 \times 3 & 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G & &
 \end{array}$$



Structure Inference with Matrix Decomposition Models

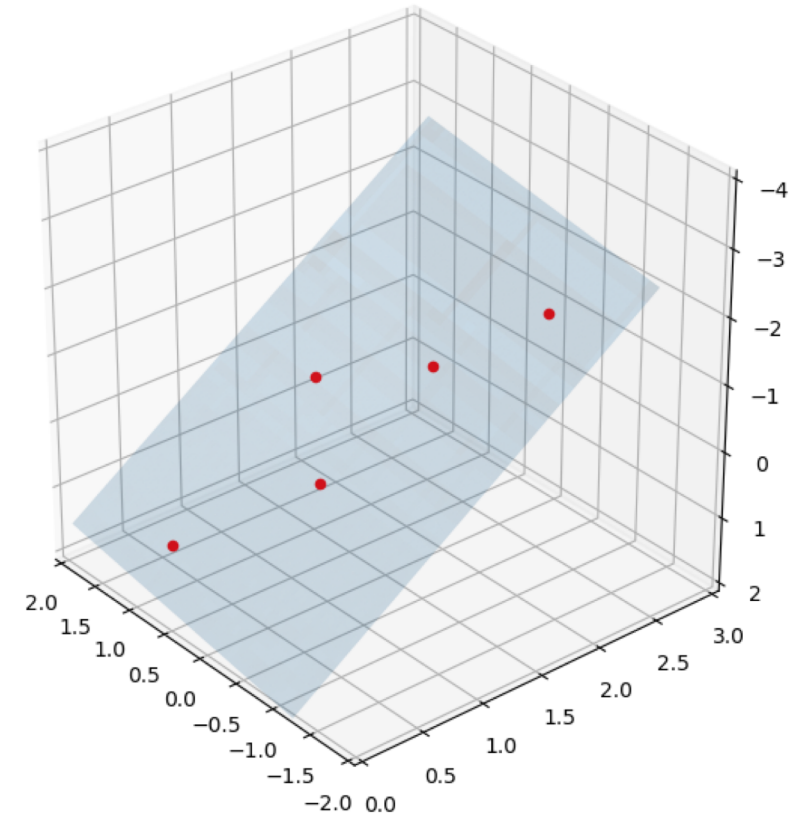
$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix} & \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 3 & 20 \times 5 & 5 \times 3 & 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G & &
 \end{array}$$



Structure Inference with Matrix Decomposition Models

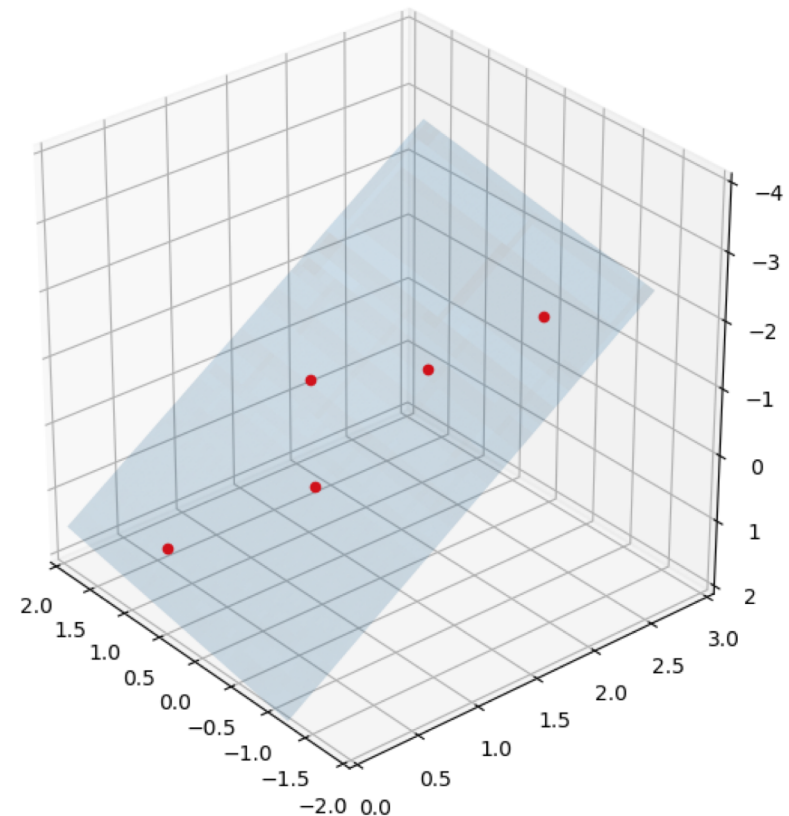
$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix} & \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 3 & 20 \times 5 & 5 \times 3 & 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G & &
 \end{array}$$

LowRank
 \longrightarrow



Structure Inference with Matrix Decomposition Models

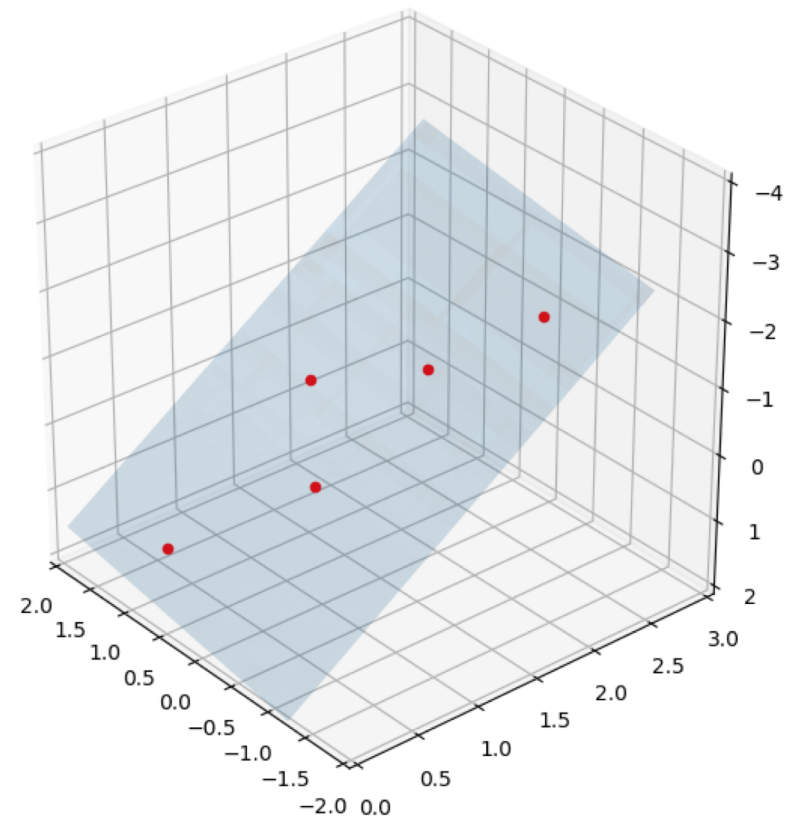
$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix } 20 \times 3 & \text{Cluster Label } 20 \times 5 & \text{Cluster Center } 5 \times 3 & \text{Cluster Noise } 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G
 \end{array}$$



$$\begin{array}{c}
 \xrightarrow{\text{LowRank}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \left(\begin{array}{c} \text{Cluster Label} \\ \text{Cluster Center} \end{array} \right) + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Cluster Label } 20 \times 5 & \text{Cluster Center } 5 \times 3 & \text{Cluster Noise } 20 \times 3
 \end{array}$$

Structure Inference with Matrix Decomposition Models

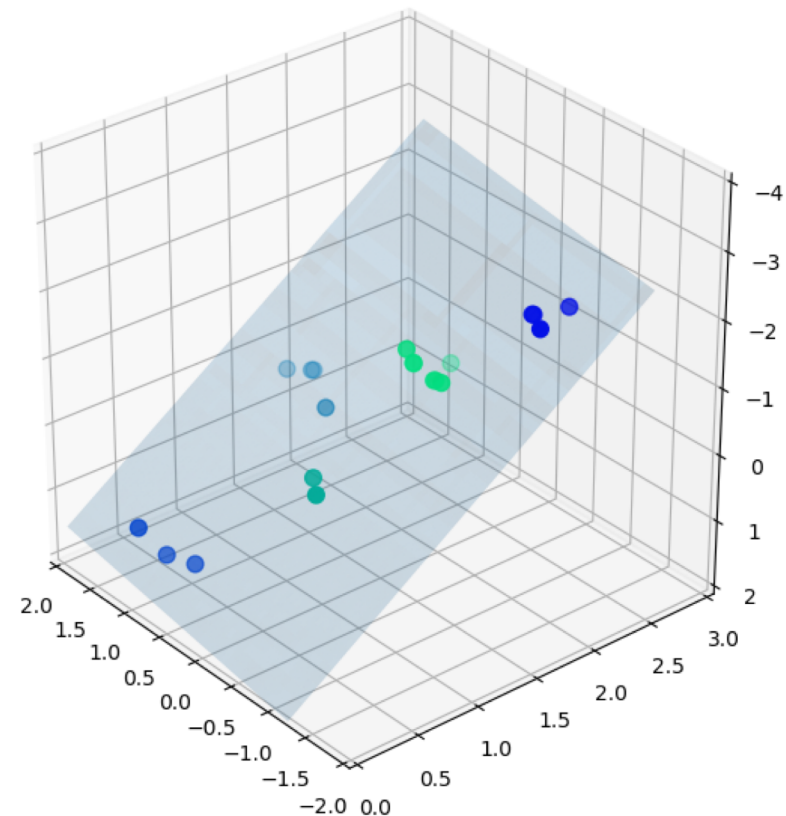
$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix } 20 \times 3 & \text{Cluster Label } 20 \times 5 & \text{Cluster Center } 5 \times 3 & \text{Cluster Noise } 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G
 \end{array}$$



$$\begin{array}{c}
 \xrightarrow{\text{LowRank}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \left(\begin{bmatrix} -1.32 & +2.01 \\ +0.04 & -0.23 \\ +0.08 & +0.95 \\ -0.68 & +0.52 \\ -0.77 & +1.40 \end{bmatrix} \begin{bmatrix} 1 & 0 & -0.22 \\ 0 & 1 & -1.30 \end{bmatrix} \right) + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Cluster Label } 20 \times 5 & \text{Cluster Center } (5 \times 2) @ (2 \times 3) & \text{Cluster Noise } 20 \times 3 \\
 \hline
 \text{Structure } M(GG + G) + G
 \end{array}$$

Structure Inference with Matrix Decomposition Models

$$\begin{array}{c}
 \begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix} \xrightarrow{\text{Cluster}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Input Matrix} & \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 3 & 20 \times 5 & 5 \times 3 & 20 \times 3 \\
 \hline
 \text{Structure } G & \text{Structure } MG + G & &
 \end{array}$$



$$\begin{array}{c}
 \xrightarrow{\text{LowRank}} \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix} \left(\begin{bmatrix} -1.32 & +2.01 \\ +0.04 & -0.23 \\ +0.08 & +0.95 \\ -0.68 & +0.52 \\ -0.77 & +1.40 \end{bmatrix} \begin{bmatrix} 1 & 0 & -0.22 \\ 0 & 1 & -1.30 \end{bmatrix} \right) + \begin{bmatrix} -0.24 & -0.04 & 0.01 \\ -0.61 & 0.76 & -0.04 \\ \vdots & \vdots & \vdots \\ -0.09 & 0.90 & -1.84 \end{bmatrix} \\
 \text{Cluster Label} & \text{Cluster Center} & \text{Cluster Noise} \\
 20 \times 5 & (5 \times 2) @ (2 \times 3) & 20 \times 3 \\
 \hline
 \text{Structure } M(GG + G) + G & &
 \end{array}$$

Naïve Exhaustive Search

- Clustering $MG+G$
- Low-Rank Approximation $GG+G$
- Binary Features $BG+G$
- Random Walk $CG+G$
- Co-Clustering $M(GM^T+G)+G$
- Clustered Matrix Decomp. $(MG+G)(GM^T+G)+G$
- Binary Matrix Factorization $(BG+G)(GB^T+G)+G$
- Dependent GSM $(\exp(GG+G)\circ G)+G$
-

Naïve Exhaustive Search

• Clustering	$MG+G$
• Low-Rank Approximation	$GG+G$
• Binary Features	$BG+G$
• Random Walk	$CG+G$
• Co-Clustering	$M(GM^T+G)+G$
• Clustered Matrix Decomp.	$(MG+G)(GM^T+G)+G$
• Binary Matrix Factorization	$(BG+G)(GB^T+G)+G$
• Dependent GSM	$(\exp(GG+G)\circ G)+G$
•	

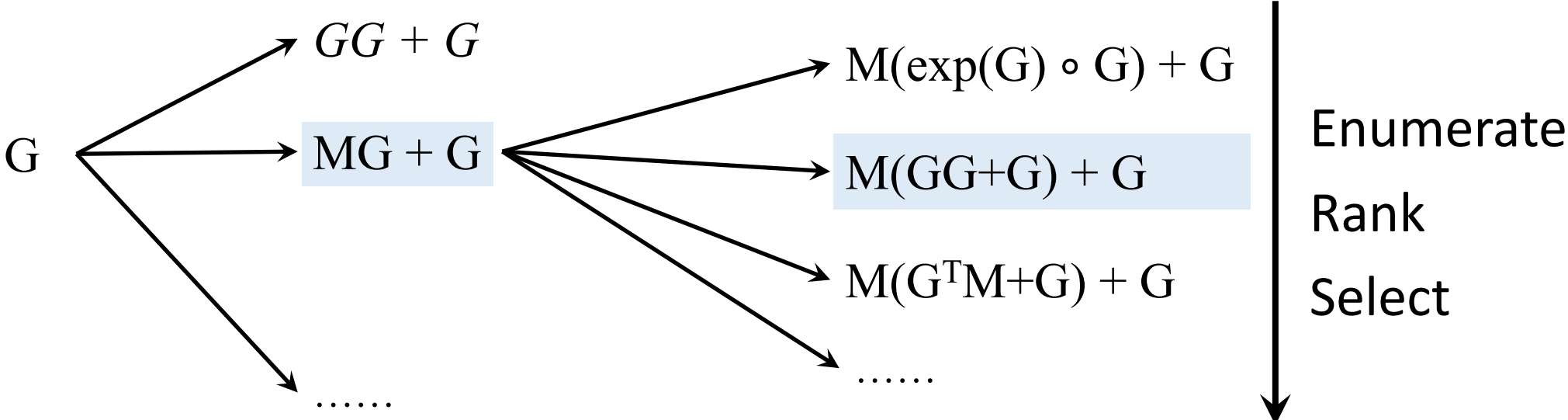
Enumerate

Rank

Select



Layer-wise Exhaustive Search



$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}
 \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + Noise$$

Input Matrix 20x3 Cluster Label 20x5 Cluster Center 5x3

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \left(\begin{bmatrix} -1.32 & +2.01 \\ +0.04 & -0.23 \\ +0.08 & +0.95 \\ -0.68 & +0.52 \\ -0.77 & +1.40 \end{bmatrix} \begin{bmatrix} 1 & 0 & -0.22 \\ 0 & 1 & -1.30 \end{bmatrix} \right) + Noise$$

Cluster Center (5x2)@(2x3)

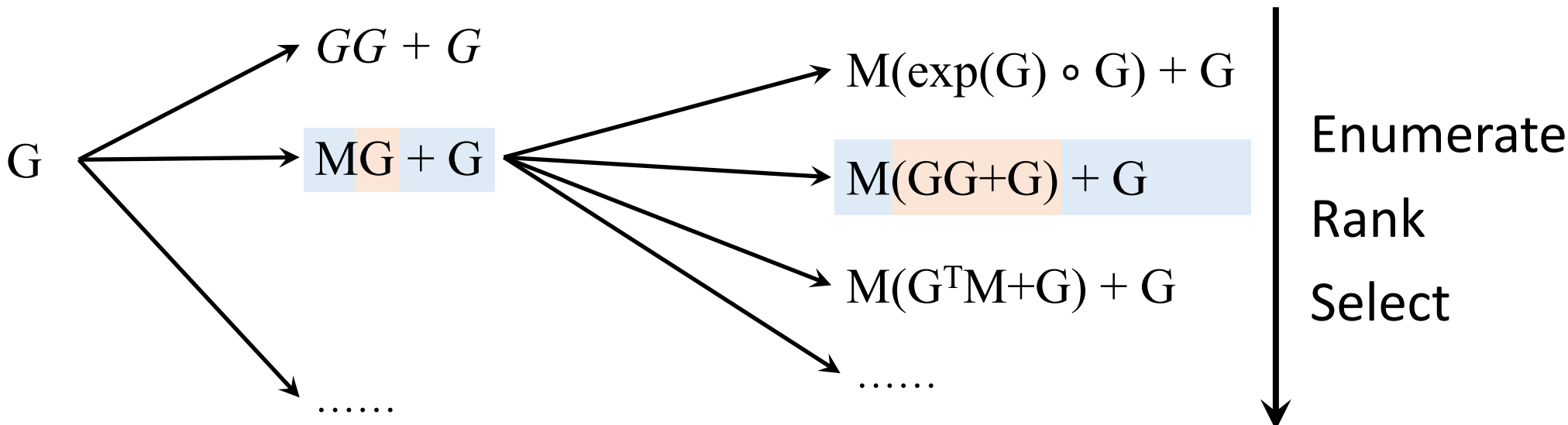
Structure G

Structure $MG + G$

Structure $M(GG + G) + G$

Layer-wise Exhaustive Search

Key Observation: Each step involves the same sub-problem.



$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}
 \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + Noise$$

Input Matrix 20x3 Cluster Label 20x5 Cluster Center 5x3

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \left(\begin{bmatrix} -1.32 & +2.01 \\ +0.04 & -0.23 \\ +0.08 & +0.95 \\ -0.68 & +0.52 \\ -0.77 & +1.40 \end{bmatrix} \begin{bmatrix} 1 & 0 & -0.22 \\ 0 & 1 & -1.30 \end{bmatrix} \right) + Noise$$

Cluster Center (5x2)@(2x3)

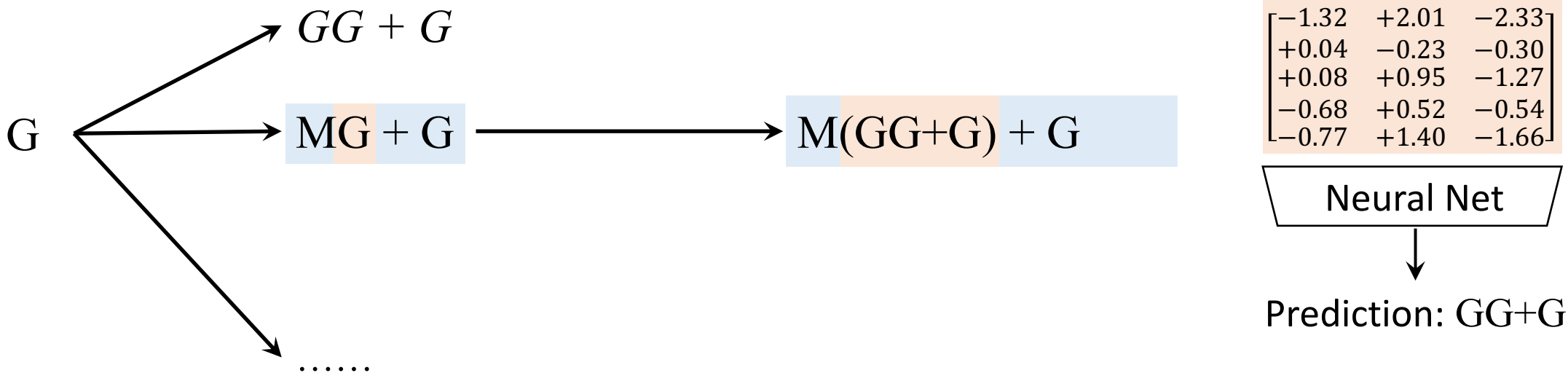
Structure G

Structure $MG + G$

Structure $M(GG + G) + G$

Neurally Guided Search

Use Neural Network for Layer-wise Amortized Inference.



$$\begin{bmatrix} -1.01 & 1.36 & -1.64 \\ -0.76 & 0.48 & -0.50 \\ \vdots & \vdots & \vdots \\ -0.24 & 0.89 & -1.12 \end{bmatrix}
 \begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \begin{bmatrix} -1.32 & +2.01 & -2.33 \\ +0.04 & -0.23 & -0.30 \\ +0.08 & +0.95 & -1.27 \\ -0.68 & +0.52 & -0.54 \\ -0.77 & +1.40 & -1.66 \end{bmatrix} + Noise$$

Input Matrix 20×3 Cluster Label 20×5 Cluster Center 5×3

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \\ \vdots & & & & \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}
 \left(\begin{bmatrix} -1.32 & +2.01 \\ +0.04 & -0.23 \\ +0.08 & +0.95 \\ -0.68 & +0.52 \\ -0.77 & +1.40 \end{bmatrix} \begin{bmatrix} 1 & 0 & -0.22 \\ 0 & 1 & -1.30 \end{bmatrix} \right) + Noise$$

Cluster Center $(5 \times 2) @ (2 \times 3)$

Structure G

Structure $MG + G$

Structure $M(GG + G) + G$

Experiment – Accuracy

Data	Ground Truth	Grosse et al. (2012)	Mat2Seq	NG-SI (ours)
Low-rank	$GG + G$	Correct	Correct	Correct
Clustering	$MG + G$	Correct	Correct	Correct
Binary latent features	$BG + G$	Correct	Correct	Correct
Random walk	$CG + G$	Correct	Correct	Correct
Co-clustering	$M(GM^T + G) + G$	Correct	$MG + G$	Correct
Binary matrix factorization	$B(GB^T + G) + G$	Correct	$BG + G$	Correct
BCTF	$(MG + G)(GM^T + G) + G$	Correct	$BG + G$	Correct
Sparse coding	$s(G)G + G$	Correct	$s(G)$	Correct
Dependent GSM	$s(GG + G)G + G$	$s(G)G + G$	$s(G)$	$s(G)G + G$
Linear dynamical system	$(CG + G)G + G$	Correct	$CG + G$	$B(s(G)G + G) + G$
Motion Capture - Level 1	-	$CG + G$	$CG + G$	$CG + G$
Motion Capture - Level 2	-	$C(GG + G) + G$	$CG + G$	$C(GG + G) + G / CG + G$
Image Patch - Level 1	-	$GG + G$	$GG + G$	$GG + G$
Image Patch - Level 2	-	$s(G)G + G$	$GG + G$	$s(G)G + G$
Image Patch - Level 3	-	$s(GG + G)G + G / s(G)G + G$	$GG + G$	$s(G)G + G$

Experiment – Accuracy

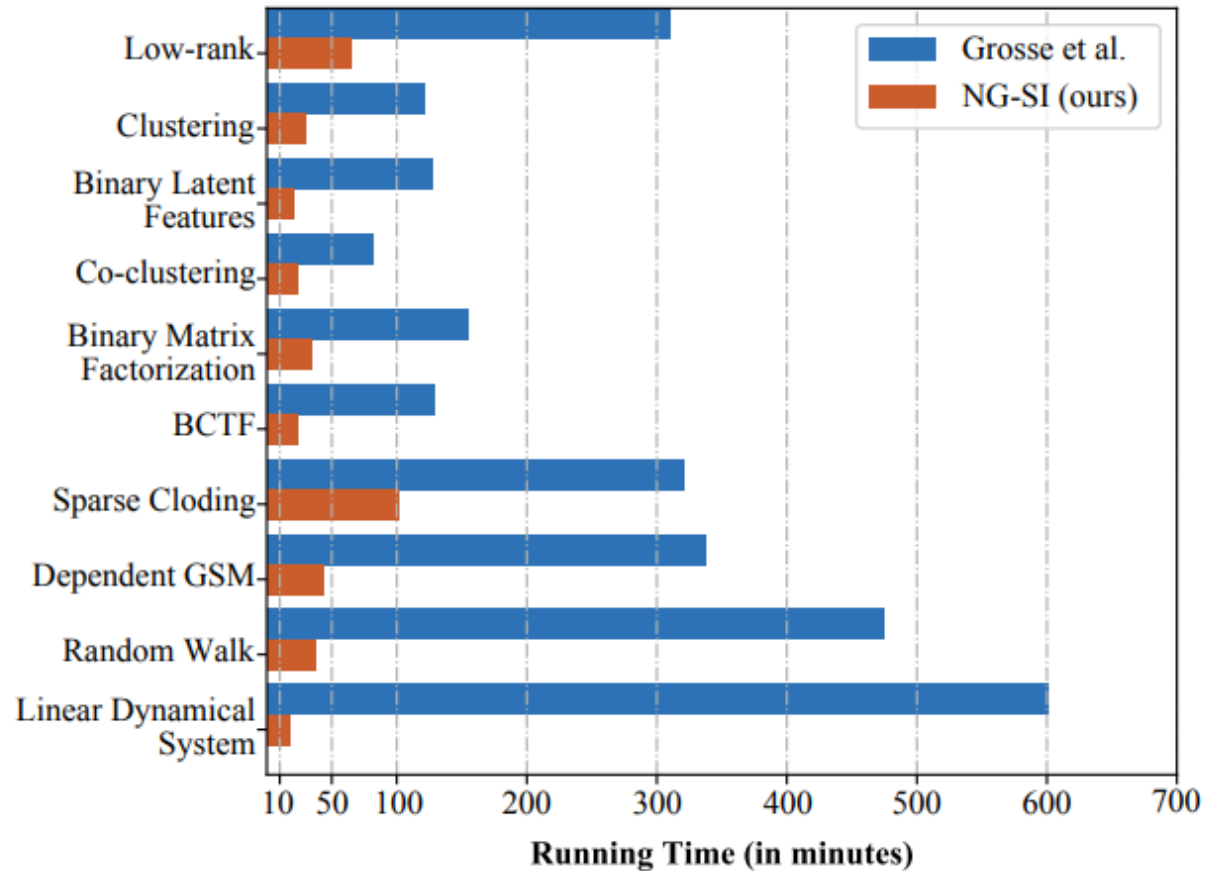
Data	Ground Truth	Grosse et al. (2012)	Mat2Seq	NG-SI (ours)
Low-rank	$GG + G$	Correct	Correct	Correct
Clustering	$MG + G$	Correct	Correct	Correct
Binary latent features	$BG + G$	Correct	Correct	Correct
Random walk	$CG + G$	Correct	Correct	Correct
Co-clustering	$M(GM^T + G) + G$	Correct	$MG + G$	Correct
Binary matrix factorization	$B(GB^T + G) + G$	Correct	$BG + G$	Correct
BCTF	$(MG + G)(GM^T + G) + G$	Correct	$BG + G$	Correct
Sparse coding	$s(G)G + G$	Correct	$s(G)$	Correct
Dependent GSM	$s(GG + G)G + G$	$s(G)G + G$	$s(G)$	$s(G)G + G$
Linear dynamical system	$(CG + G)G + G$	Correct	$CG + G$	$B(s(G)G + G) + G$
Motion Capture - Level 1	-	$CG + G$	$CG + G$	$CG + G$
Motion Capture - Level 2	-	$C(GG + G) + G$	$CG + G$	$C(GG + G) + G / CG + G$
Image Patch - Level 1	-	$GG + G$	$GG + G$	$GG + G$
Image Patch - Level 2	-	$s(G)G + G$	$GG + G$	$s(G)G + G$
Image Patch - Level 3	-	$s(GG + G)G + G / s(G)G + G$	$GG + G$	$s(G)G + G$

} Train

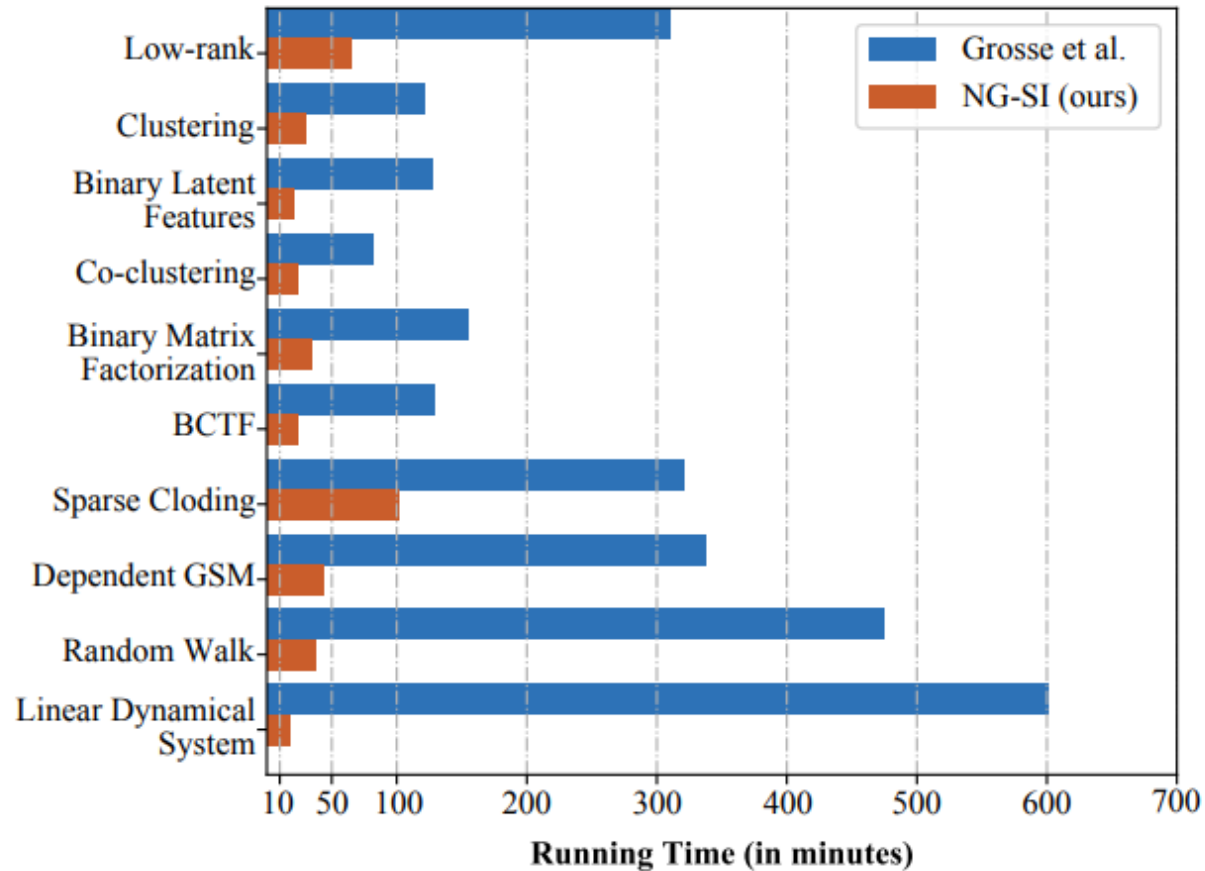
Experiment – Accuracy

Data	Ground Truth	Grosse et al. (2012)	Mat2Seq	NG-SI (ours)	
Low-rank	$GG + G$	Correct	Correct	Correct	} Train
Clustering	$MG + G$	Correct	Correct	Correct	
Binary latent features	$BG + G$	Correct	Correct	Correct	
Random walk	$CG + G$	Correct	Correct	Correct	
Co-clustering	$M(GM^T + G) + G$	Correct	$MG + G$	Correct	
Binary matrix factorization	$B(GB^T + G) + G$	Correct	$BG + G$	Correct	
BCTF	$(MG + G)(GM^T + G) + G$	Correct	$BG + G$	Correct	} Test
Sparse coding	$s(G)G + G$	Correct	$s(G)$	Correct	
Dependent GSM	$s(GG + G)G + G$	$s(G)G + G$	$s(G)$	$s(G)G + G$	
Linear dynamical system	$(CG + G)G + G$	Correct	$CG + G$	$B(s(G)G + G) + G$	
Motion Capture - Level 1	-	$CG + G$	$CG + G$	$CG + G$	
Motion Capture - Level 2	-	$C(GG + G) + G$	$CG + G$	$C(GG + G) + G / CG + G$	
Image Patch - Level 1	-	$GG + G$	$GG + G$	$GG + G$	
Image Patch - Level 2	-	$s(G)G + G$	$GG + G$	$s(G)G + G$	
Image Patch - Level 3	-	$s(GG + G)G + G / s(G)G + G$	$GG + G$	$s(G)G + G$	

Experiment – Running Time Comparison



Experiment – Running Time Comparison



Speed Up: $3\times \sim 39\times$.

Conclusion

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- Combine search-based algorithms and data-driven models.

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 - Efficient: c.f. data-driven models.
 - Combinatorial generalization.

Conclusion

Poster #233

- Combine search-based algorithms and data-driven models.
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Project Page